Experimental signatures of subtelties in the Brout-Englert-Higgs mechanism

Axel Maas

23rd of March 2023 Moriond 23 Italy









Der Wissenschaftsfonds.



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- 1970^{ies}/1980^{ies}: Field theory of BEH effect
 - Electroweak symmetry breaking is not a physical effect
 - Special form of gauge-fixing
 - Confinement and BEH effect are qualitatively the same

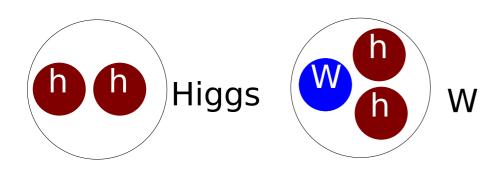
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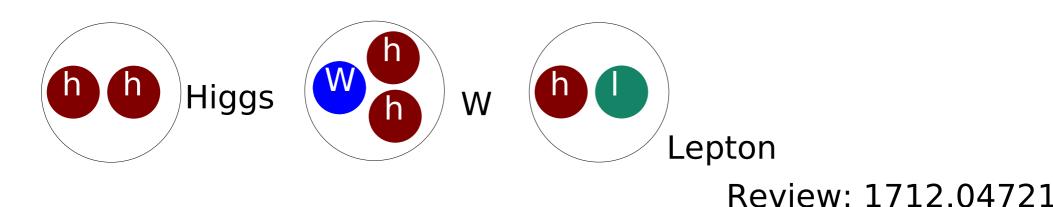
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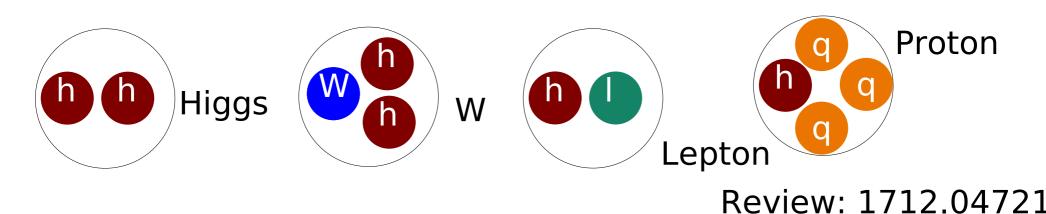


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 - Augments perturbation theory
 - Composite asymptotic states
 - Additional expansion in the Higgs vev

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Trivial two-particle state

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Standard Perturbation Theory

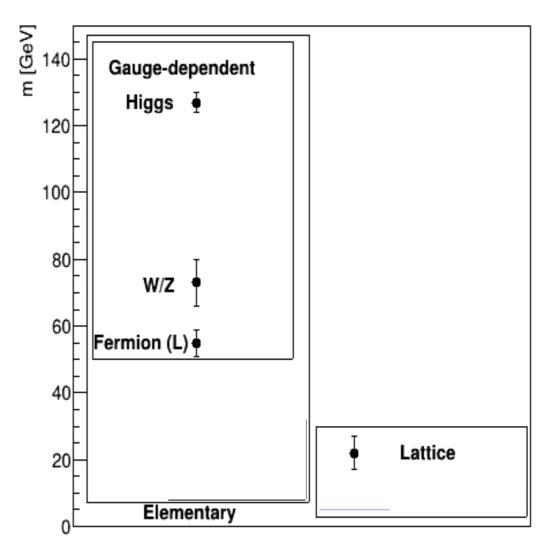
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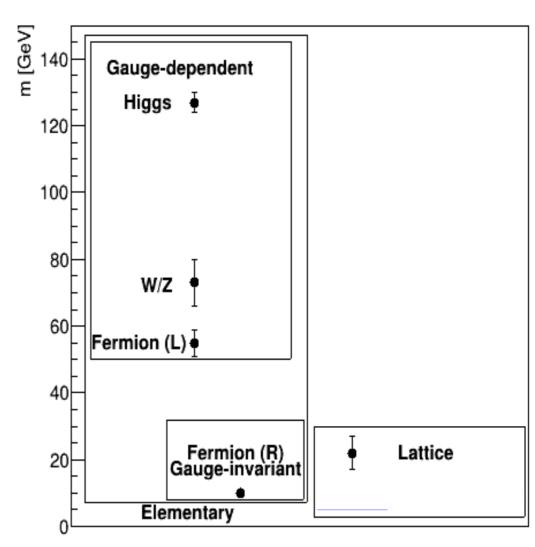
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Spectrum: Lattice and predictions

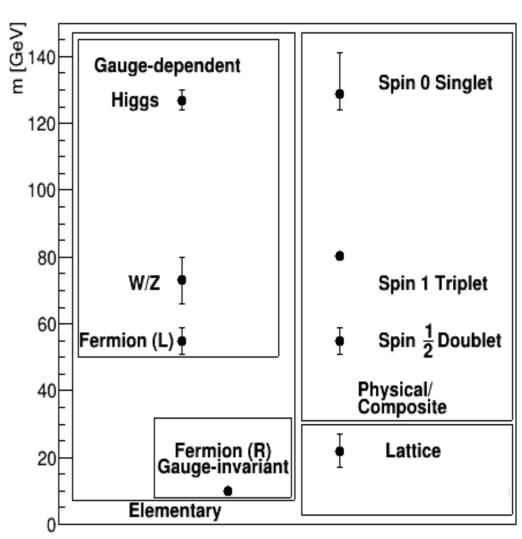


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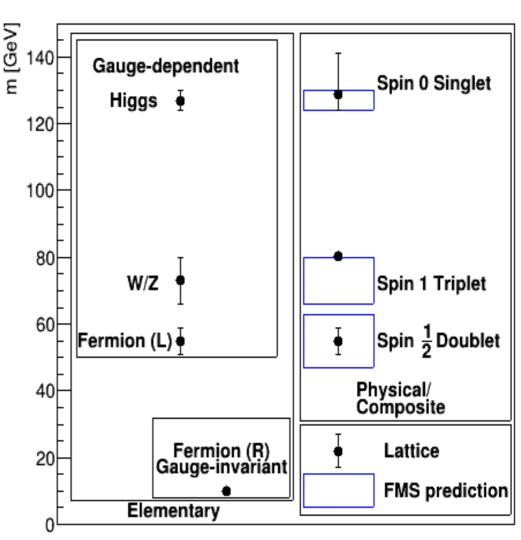


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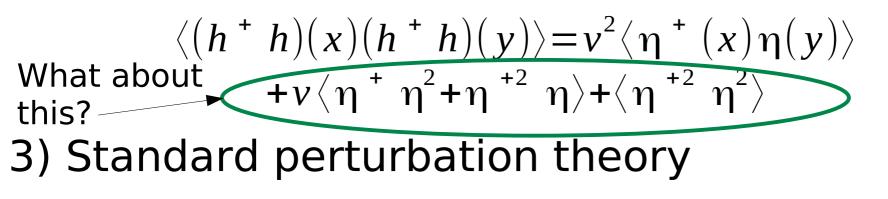
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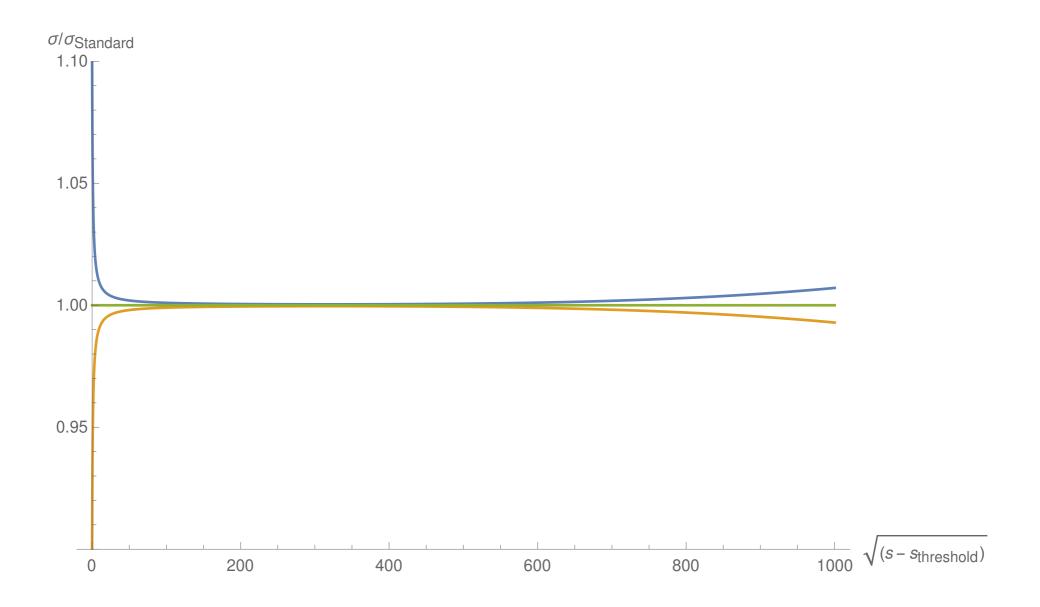
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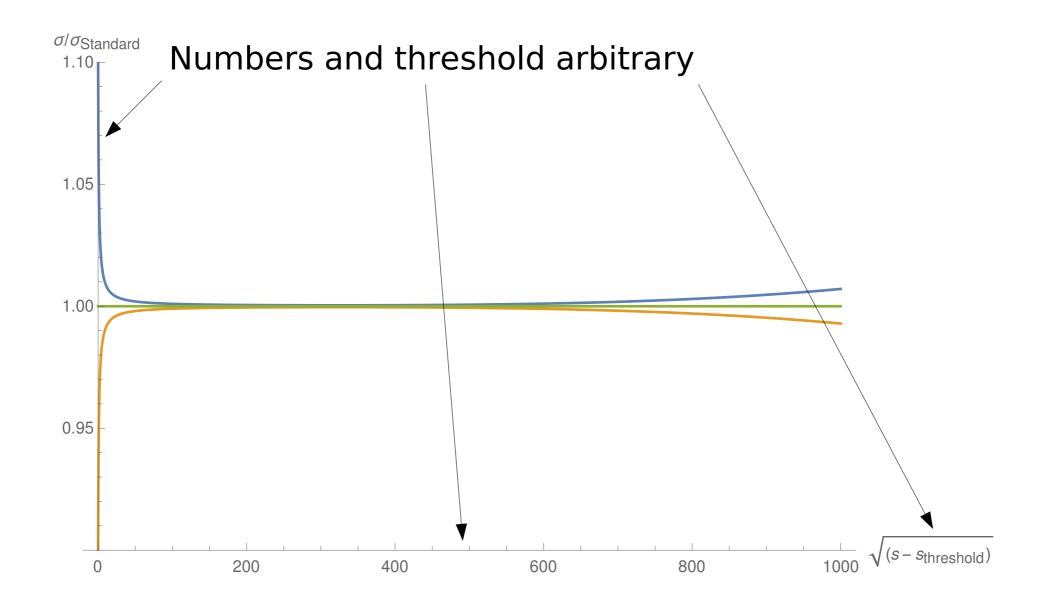
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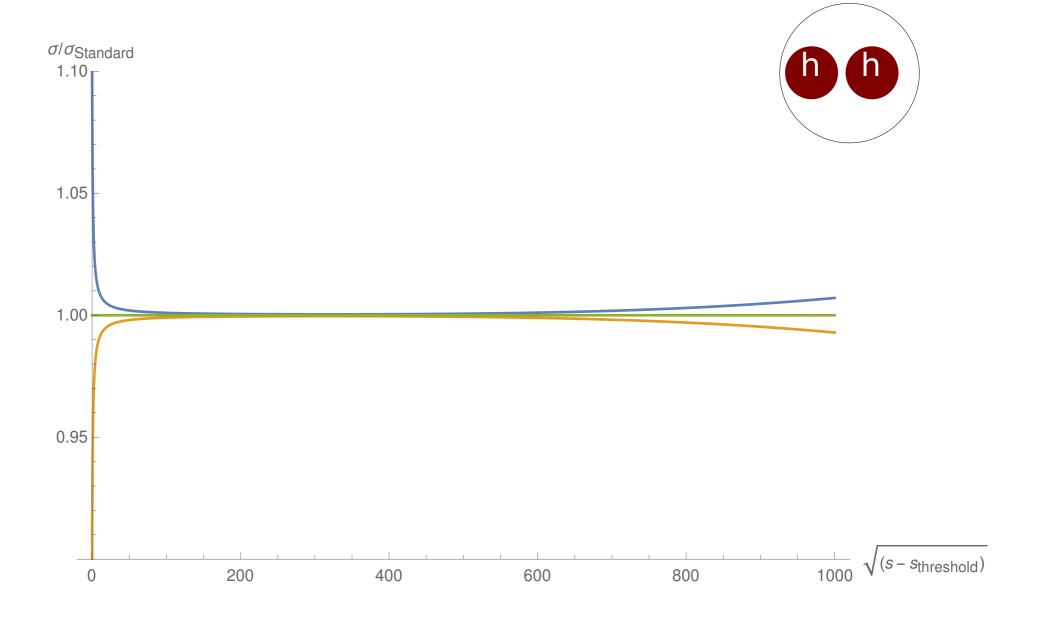
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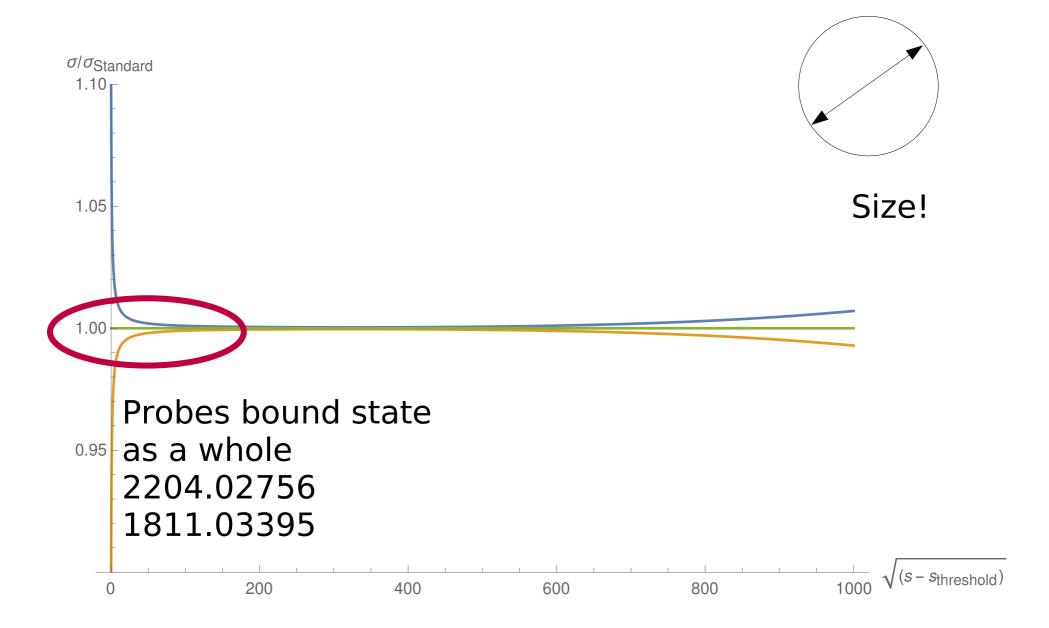


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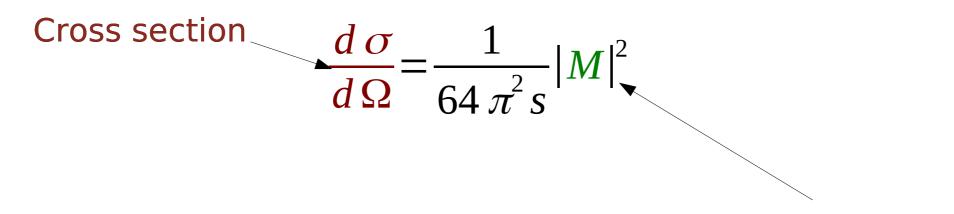
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$$s \to 4m_W^2$$

$$a_0 = \tan(\delta_J) / \sqrt{s - 4m_W^2}$$
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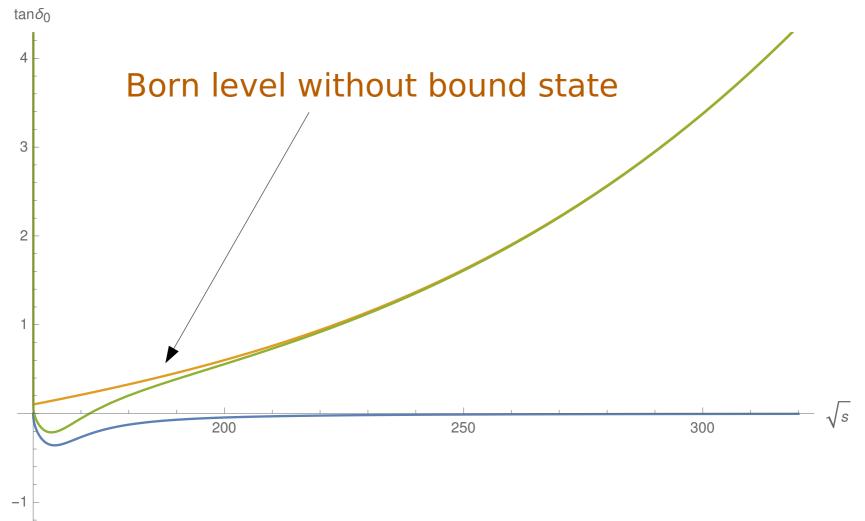
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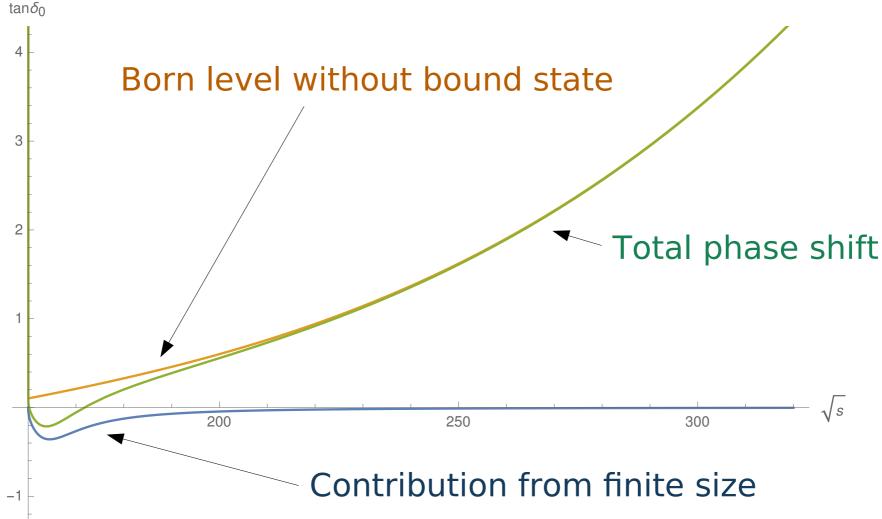
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Scattering length~"size" Phase shift

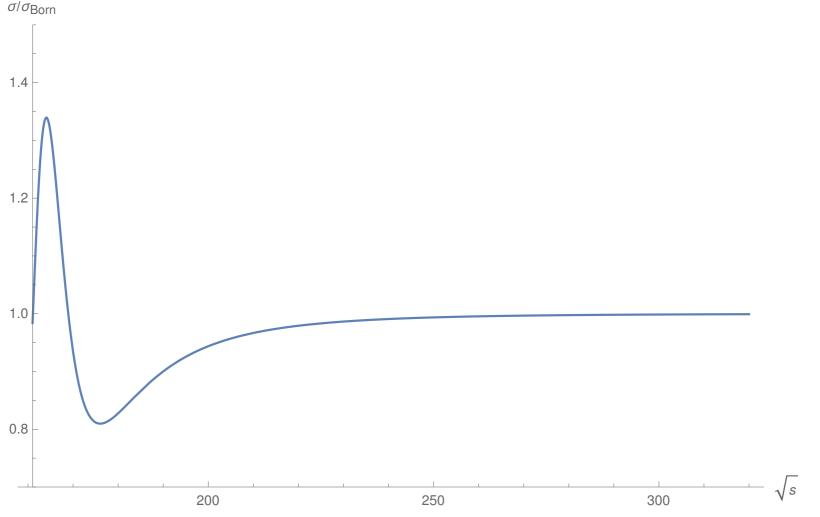
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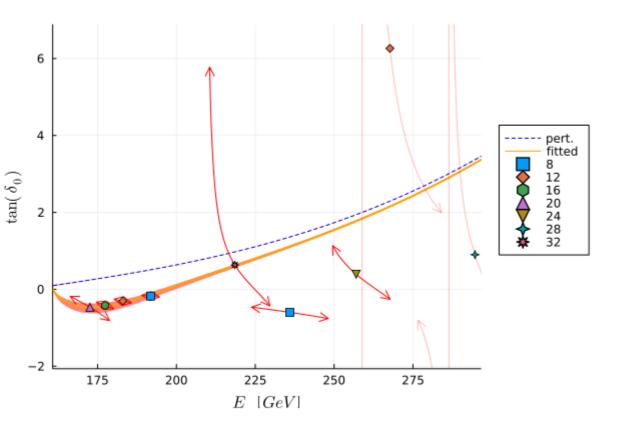


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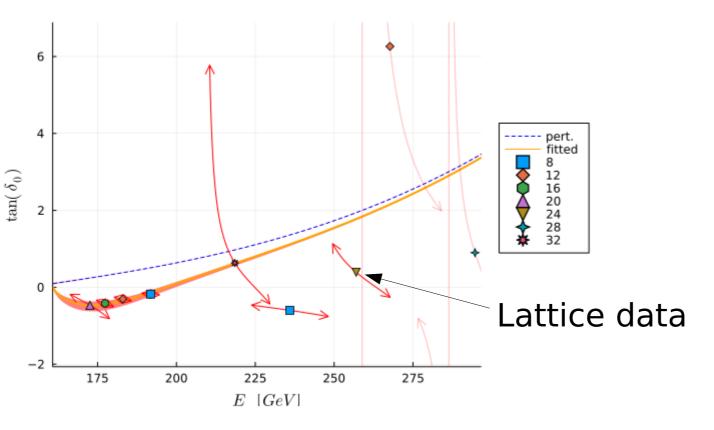


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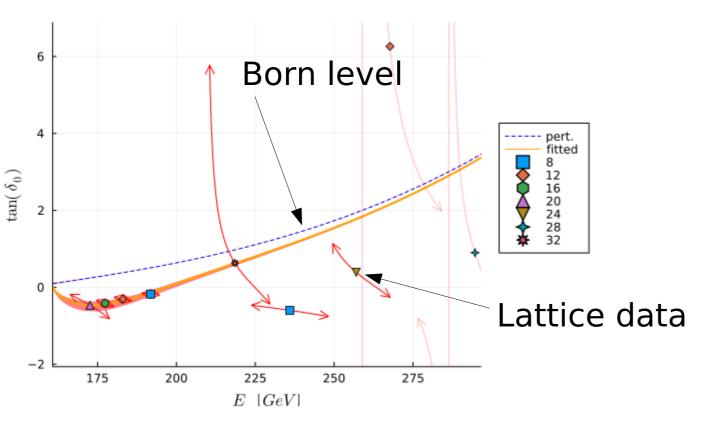
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 - Higgs too heavy and too strong weak coupling
 - Qualitatively but not quantitatively



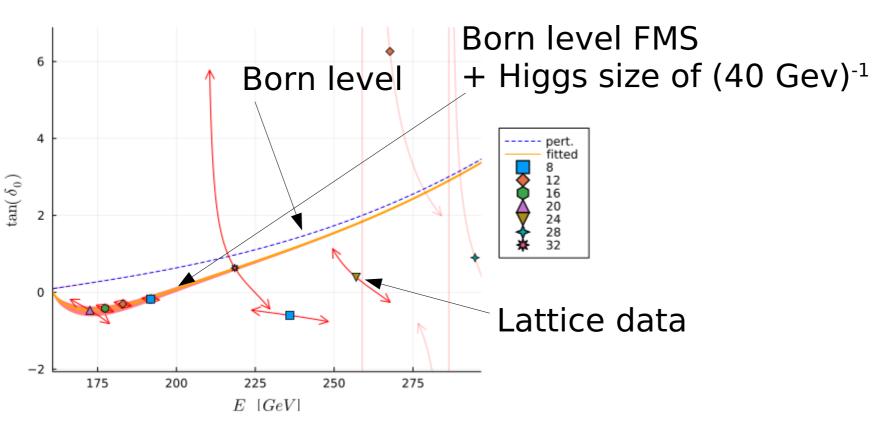
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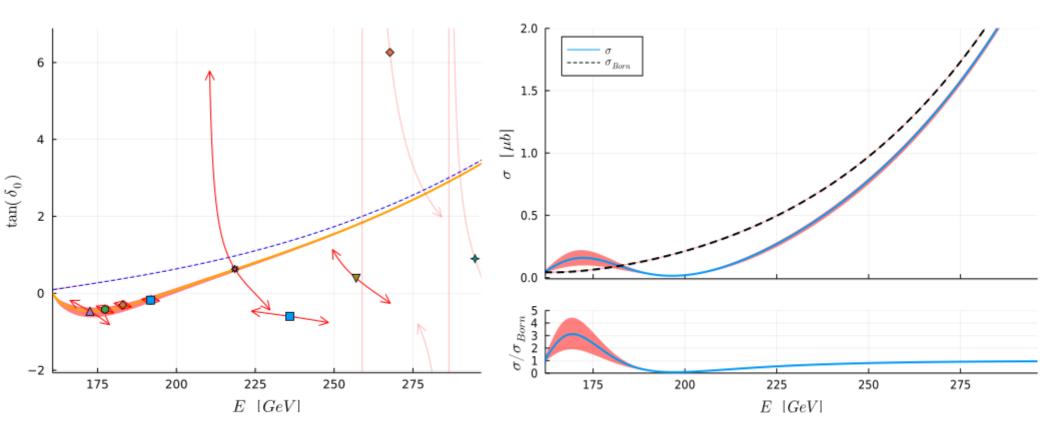
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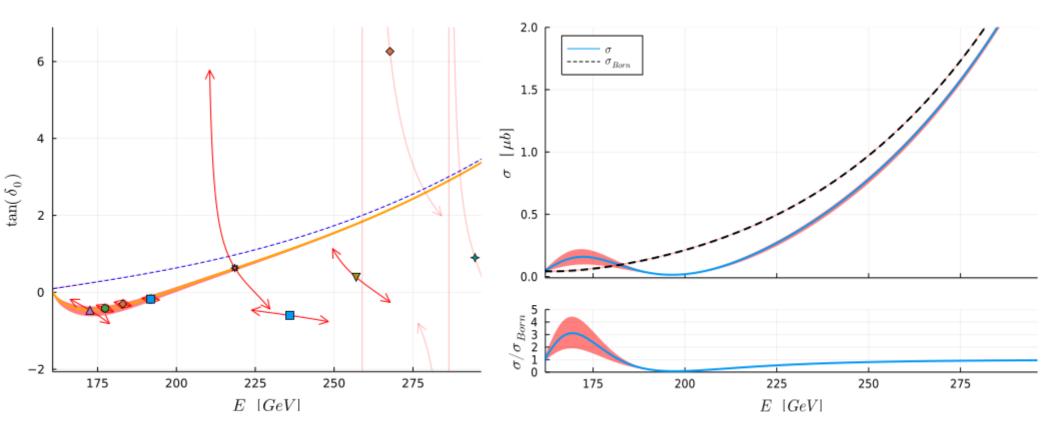
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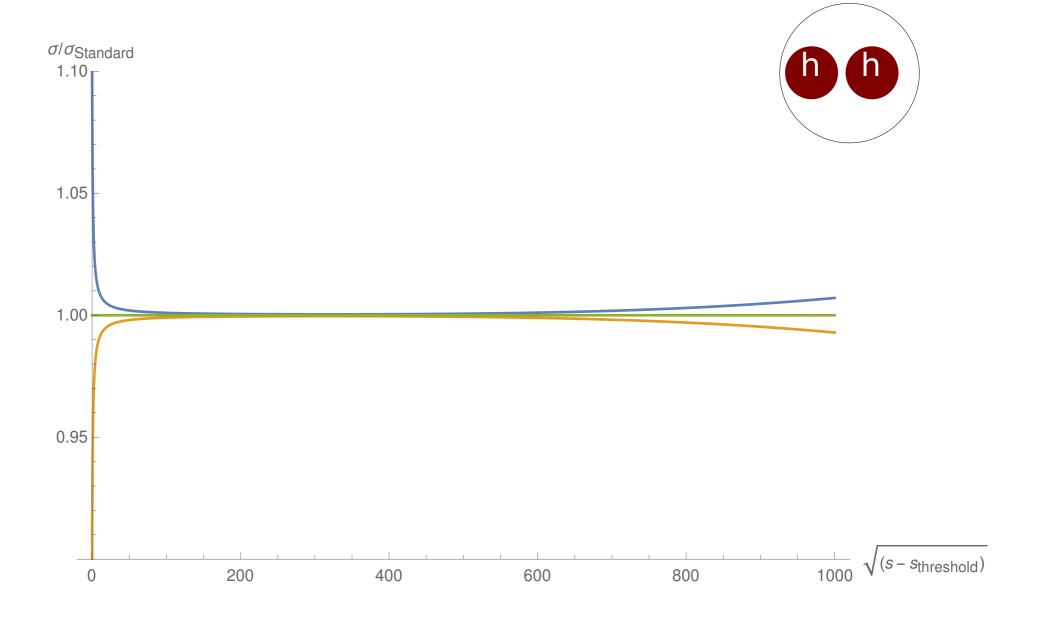
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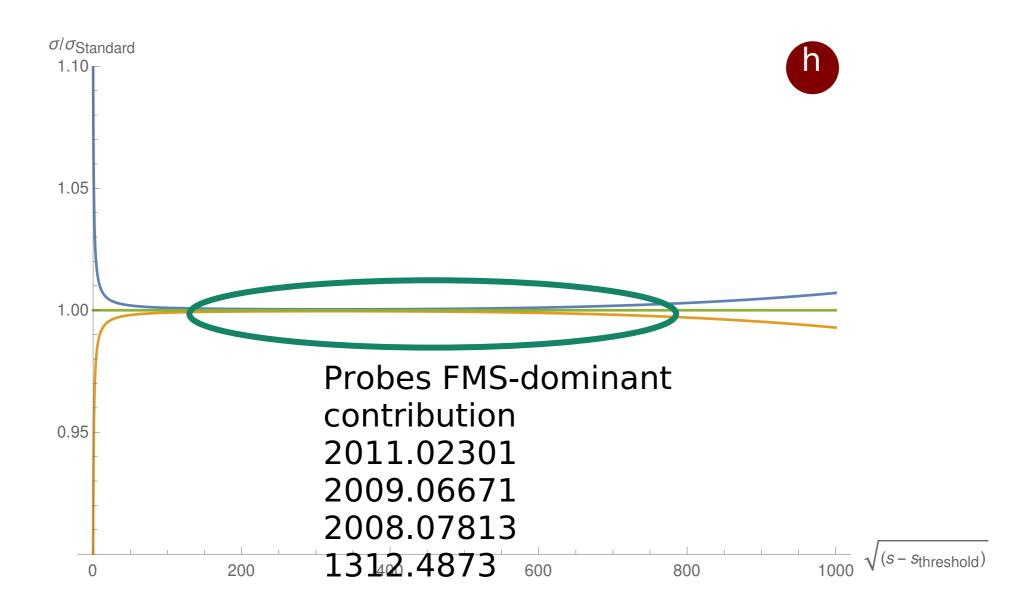


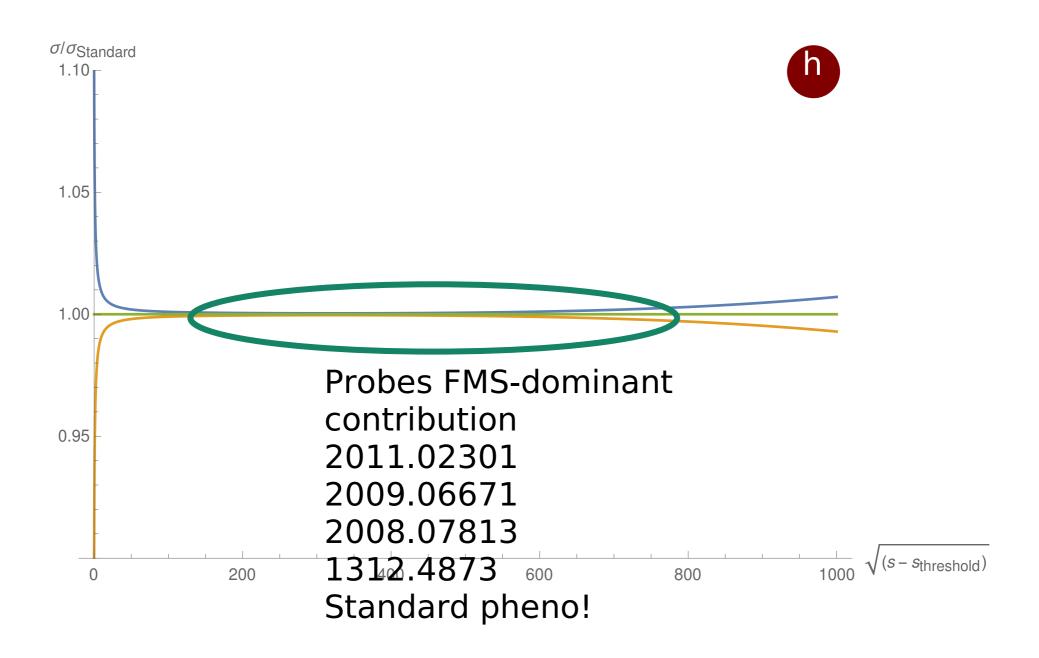
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- Trend seen in ATLAS/CMS off-shell $ZZ \rightarrow 4I$ [Talks @Higgs 2022]
 - 1.11(7) 180-220 GeV (ATLAS)/~0.8(2) 220-275 GeV (CMS)





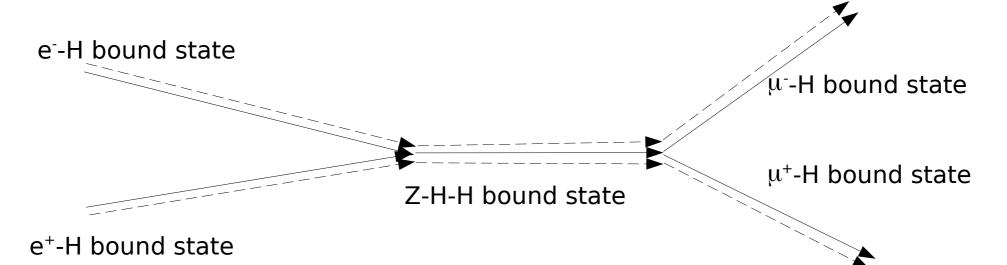


e⁻-H bound state μ^+ -H bound state e⁺-H bound state

[Maas'12]

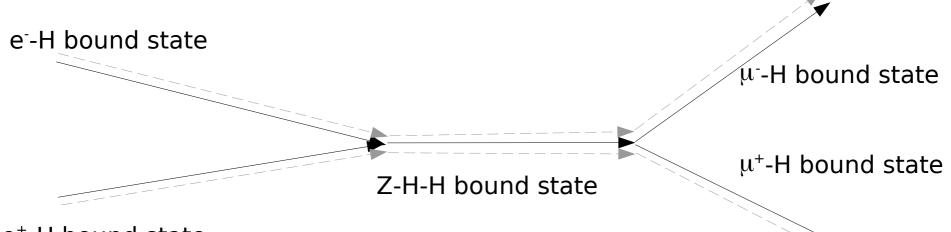
Collision of bound states

[Maas'12]



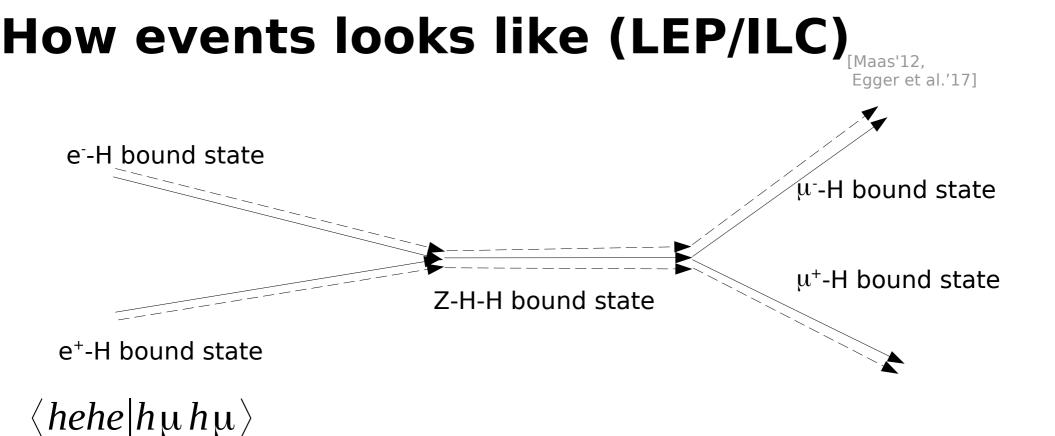
Collision of bound states - 'constituent' particles

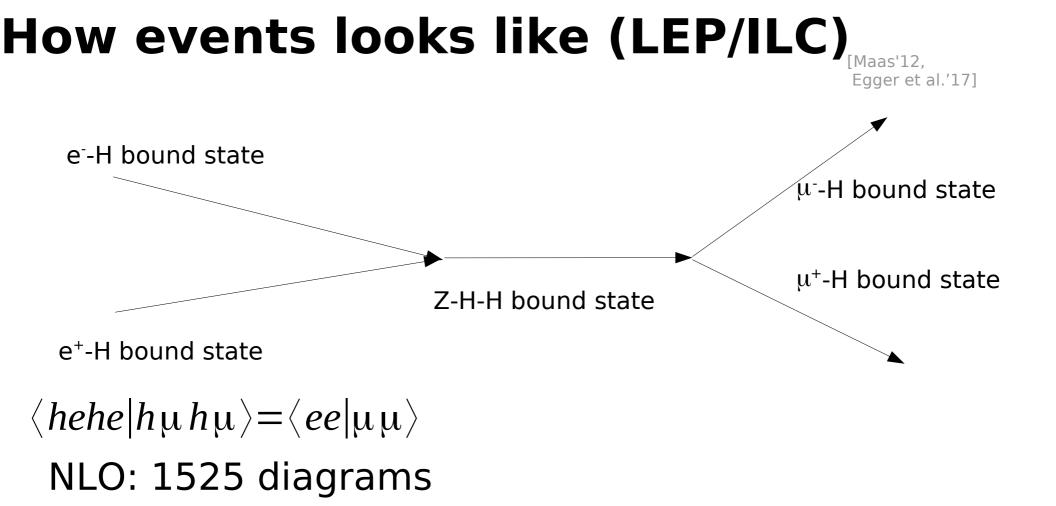
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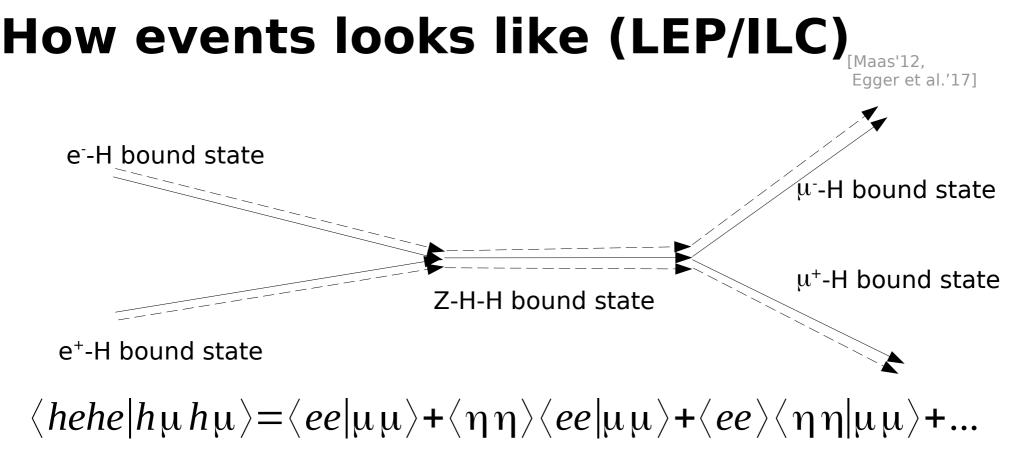


e⁺-H bound state

- Collision of bound states 'constituent' particles
- Standard perturbation theory
 - Higgs partners just spectators
 - Similar to pp collisions

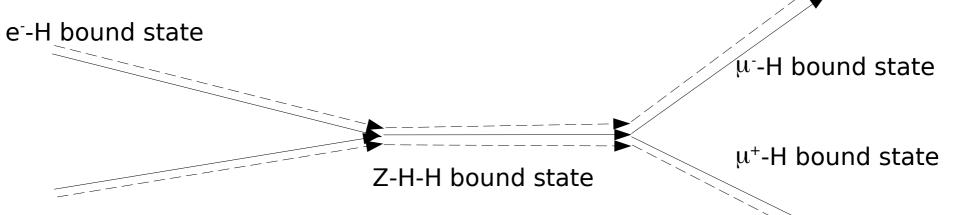






NLO: 1525 diagrams+3431 diagrams

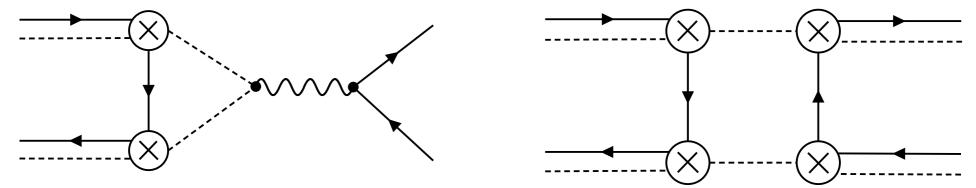
[Maas, Plätzer, Sondenheimer, Veider unpublished]



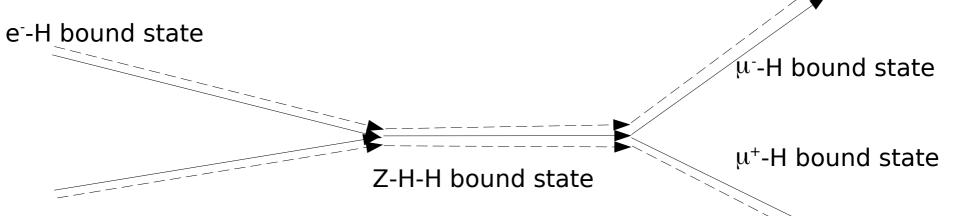
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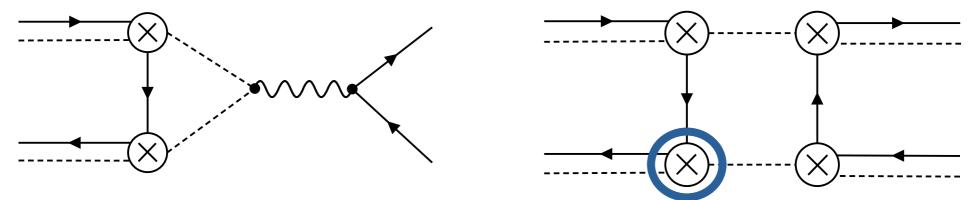
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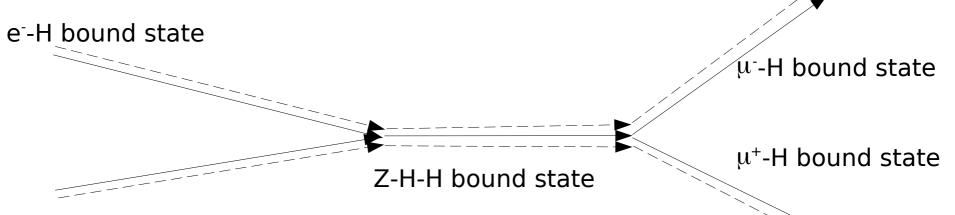
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Enhanced Feynman rules: New bound state splitting vertex

How events looks like (LEP/ILC)

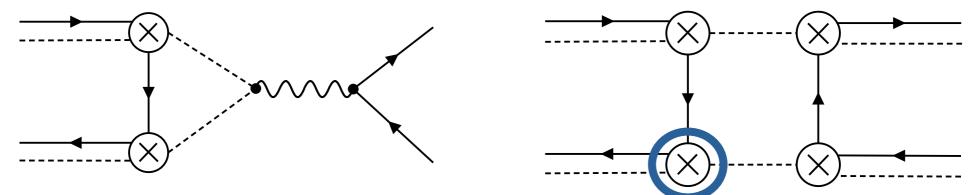
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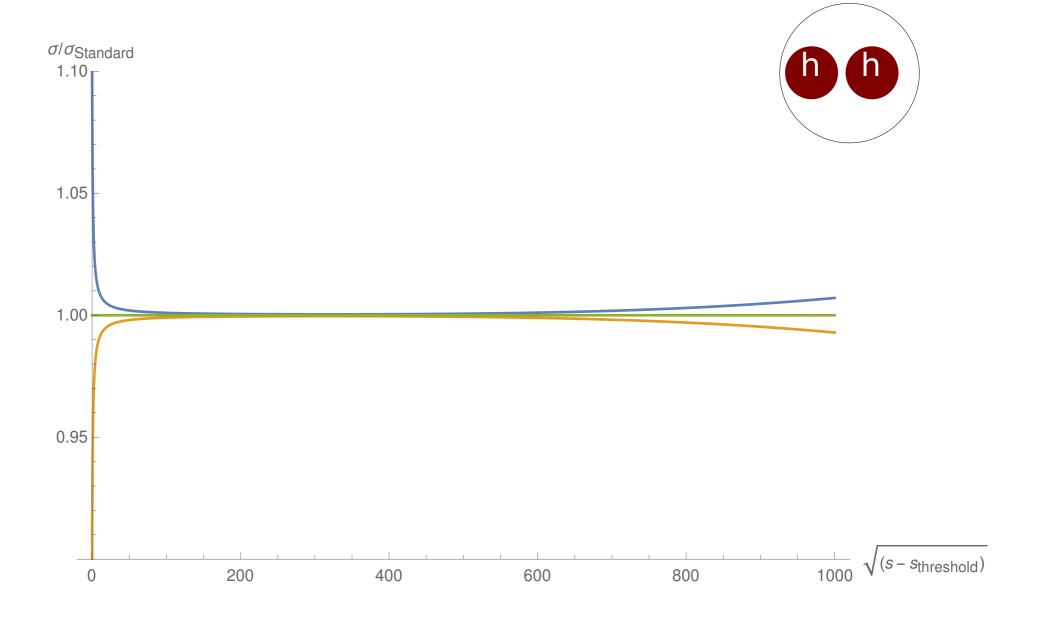
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NLO: 1525 diagrams+3431 diagrams

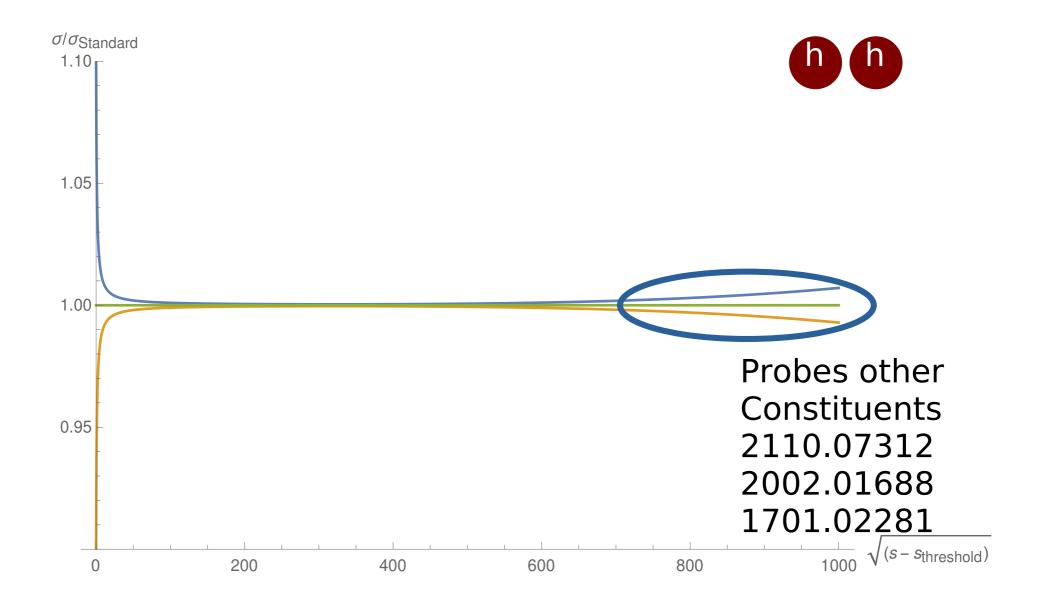


Enhanced Feynman rules: New bound state splitting vertex Can be calculated with standard tools: Managable

Generic behavior: DIS-like

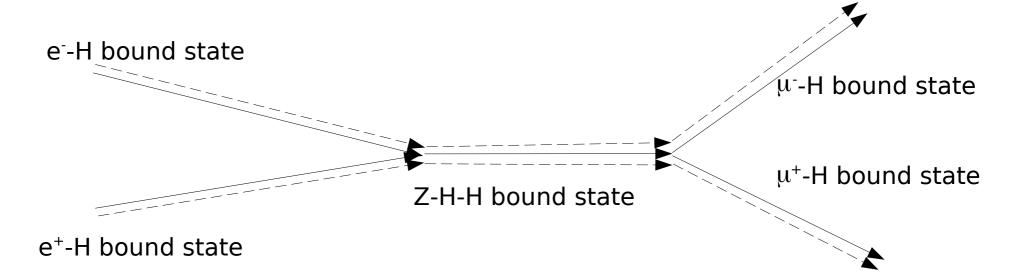


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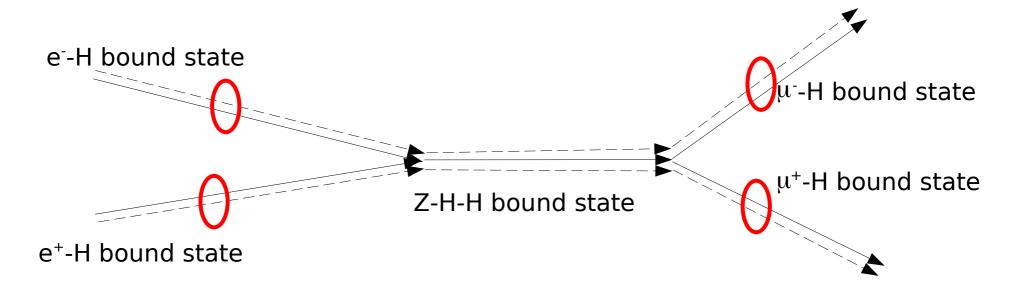
How events looks like (LEP/ILC)

[Maas'12]



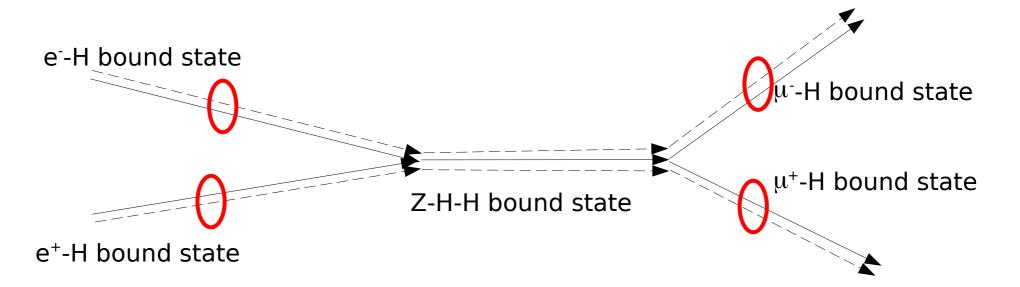
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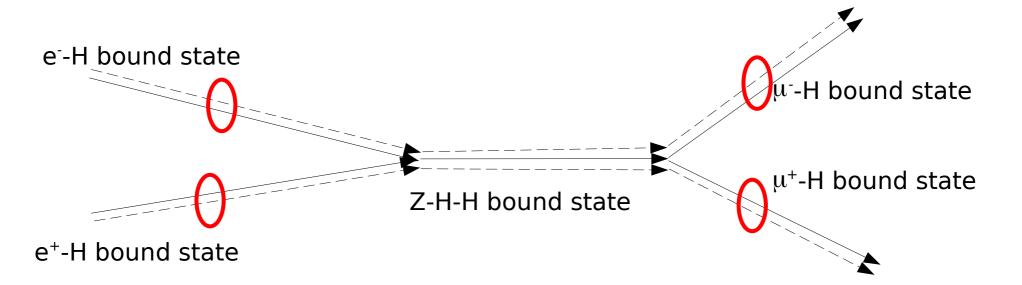
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[Maas'12, Maas, Reiner'22 Fernbach et al.'20]



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 - Generalizes to the LHC
 - PDFs at high energies affected

Field theory requires composite states



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 - Confirmed by lattice
 - Analytically treatable with FMS mechanism

Review: 1712.04721

• Can have measurable impact



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- FMS mechanism applicable to many theories
 - 2HDM, GUTs, MSSM, quantum gravity
 - Qualitative impact in many new physics scenarios

🔰 @axelmaas