

Intermediate Vector Bosons and Gauge Symmetry

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Krakow
Poland



NAWI Graz
Natural Sciences

FWF Österreichischer
Wissenschaftsfonds



What's up?

Review: 1712.04721
Update: 2305.01960

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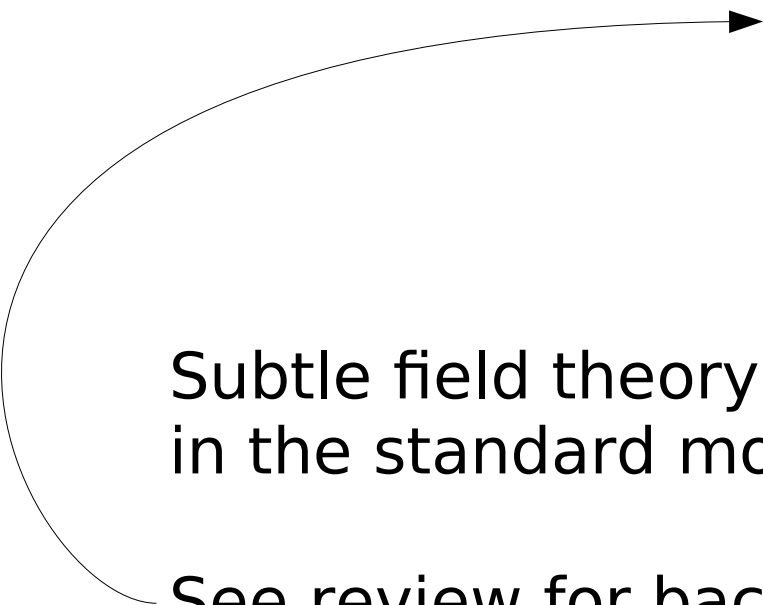
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Subtle field theory creates new effects
in the standard model

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in the standard model

See review for background!

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- Physical spectrum: Observable particles
 - Peaks in (experimental) cross-sections

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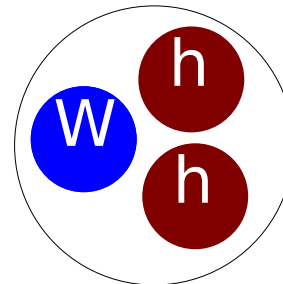
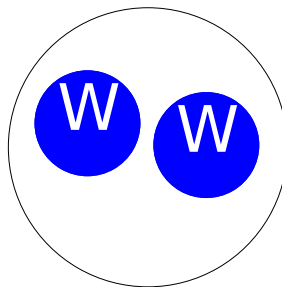
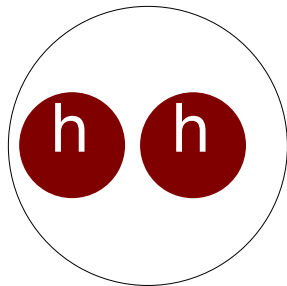
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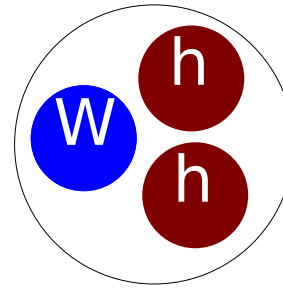
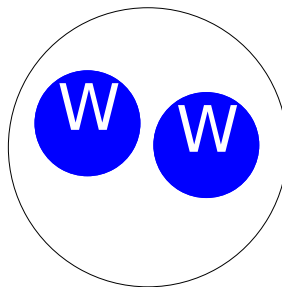
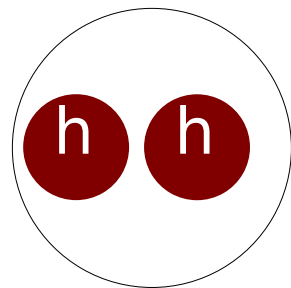


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- Why does perturbation theory work?
 - Fröhlich-Morchio-Strocchi mechanism

Fröhlich-Morchio-Strocchi Mechanism

[Fröhlich et al.'80,'81
Maas'12,'17]

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0^+ singlet: $\langle (h^\dagger h)(x)(h^\dagger h)(y) \rangle$

Higgs field

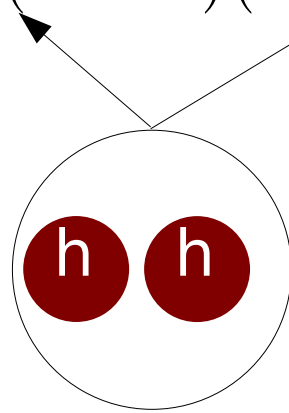


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Augmented perturbation theory

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3) Standard perturbation theory

Bound
state
mass

The diagram shows the expansion of the Higgs field $h=v+\eta$ and the resulting expression for the bound state mass. The first term, $v^2 \langle \eta^\dagger(x) \eta(y) \rangle$, is circled in red and labeled "Bound state mass". The second term, $\langle \eta^\dagger(x) \eta(y) \rangle \langle \eta^\dagger(x) \eta(y) \rangle$, is circled in purple and labeled "Trivial two-particle state". The full expression is:

$$\langle (h^\dagger h)(x)(h^\dagger h)(y) \rangle = v^2 \langle \eta^\dagger(x) \eta(y) \rangle + \langle \eta^\dagger(x) \eta(y) \rangle \langle \eta^\dagger(x) \eta(y) \rangle + O(g, \lambda)$$

Trivial two-particle state

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Standard
Perturbation
Theory

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What about
this? →

$$+v \langle \eta^\dagger \eta^2 + \eta^{\dagger 2} \eta \rangle + \langle \eta^{\dagger 2} \eta^2 \rangle$$

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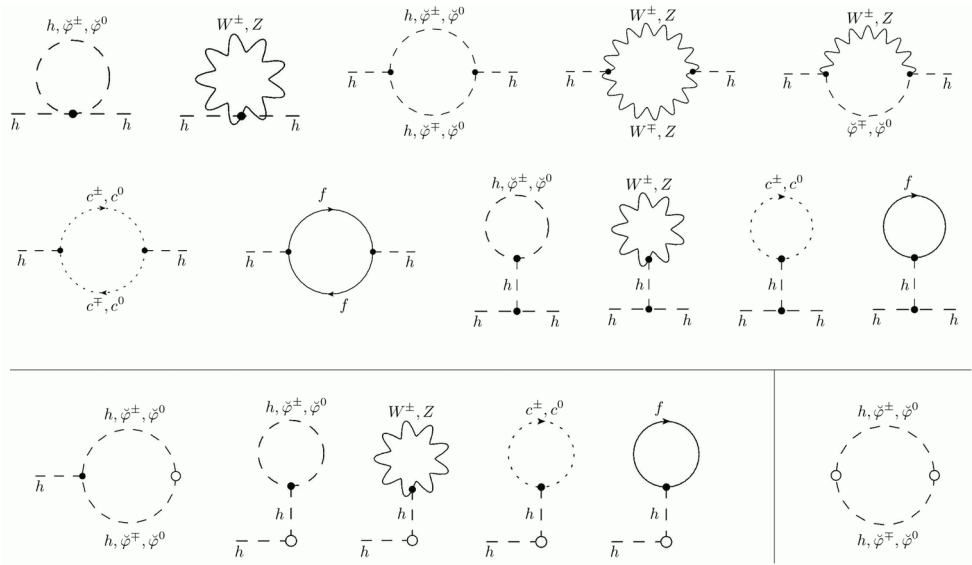
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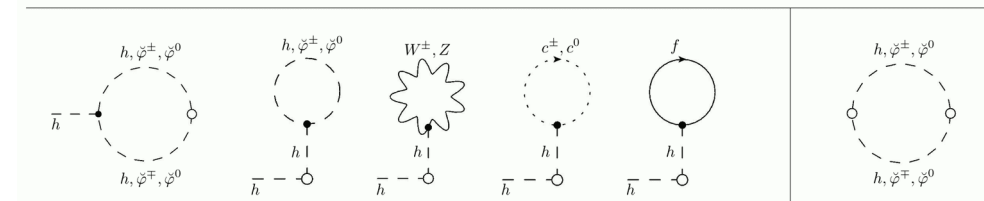
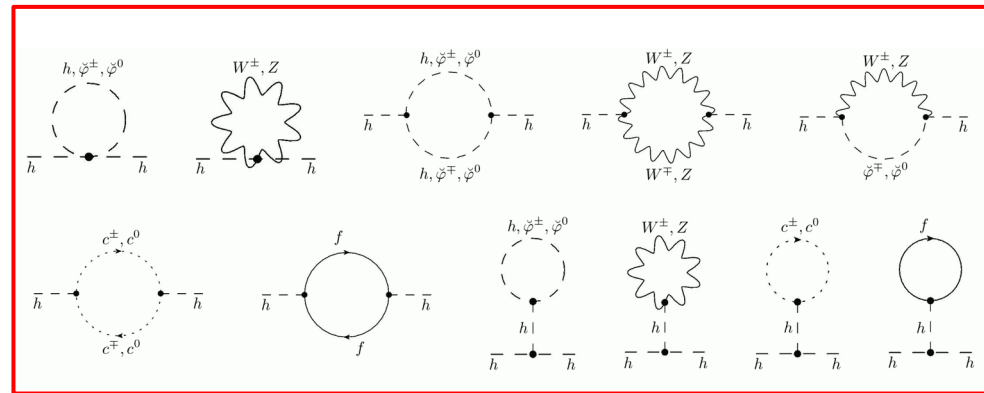
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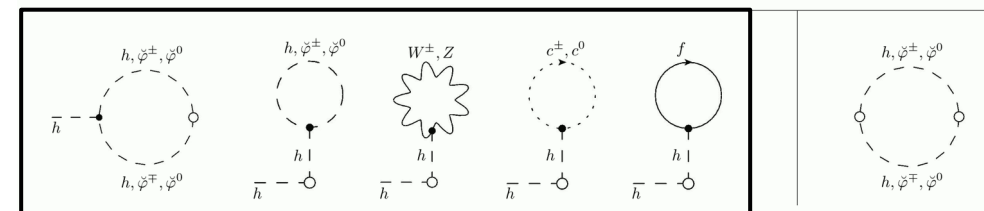
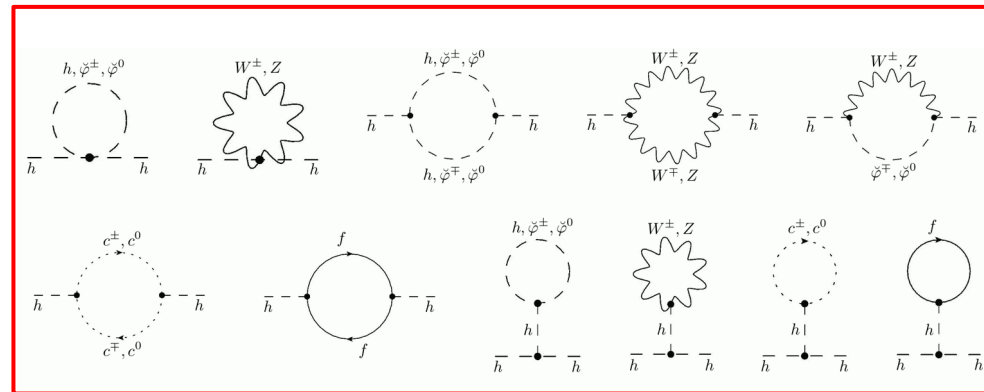
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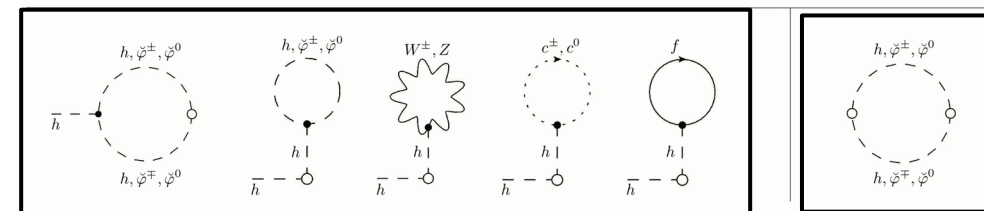
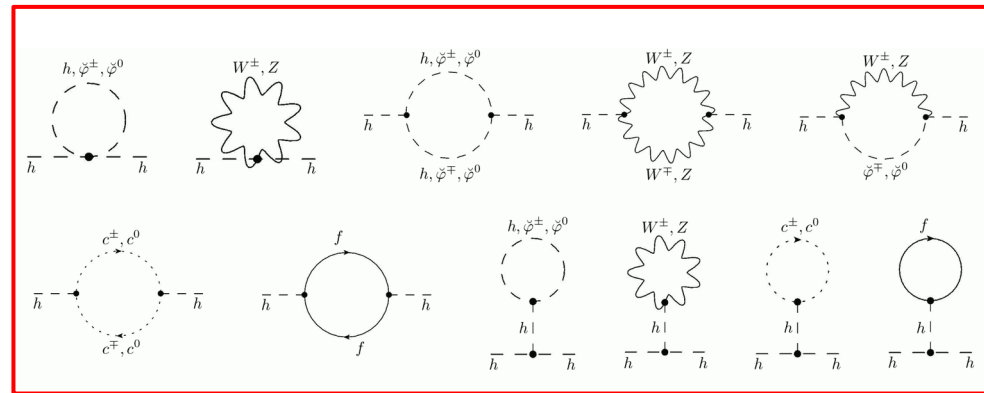
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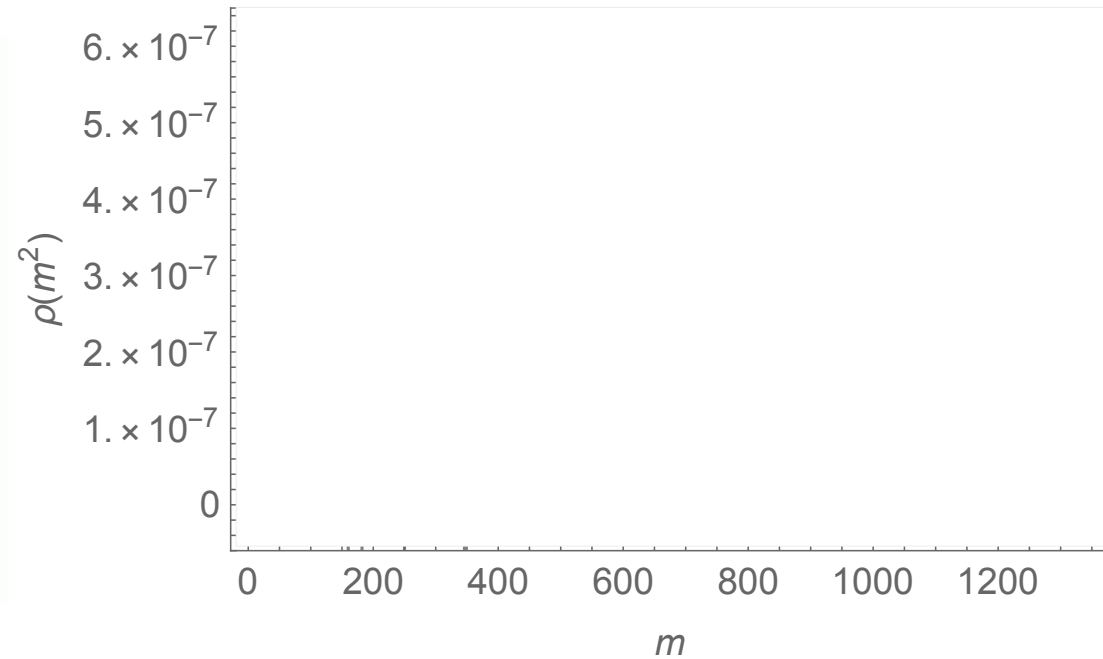
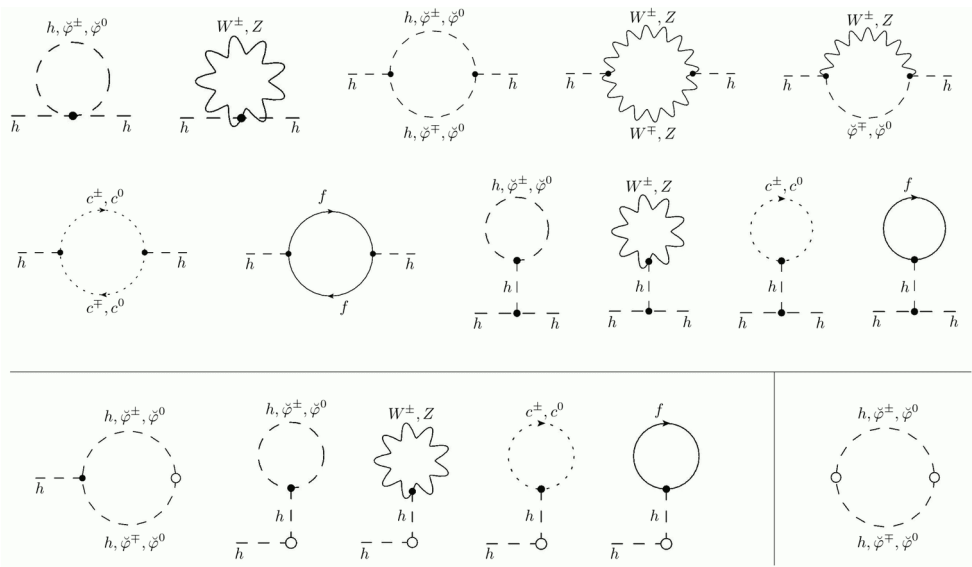
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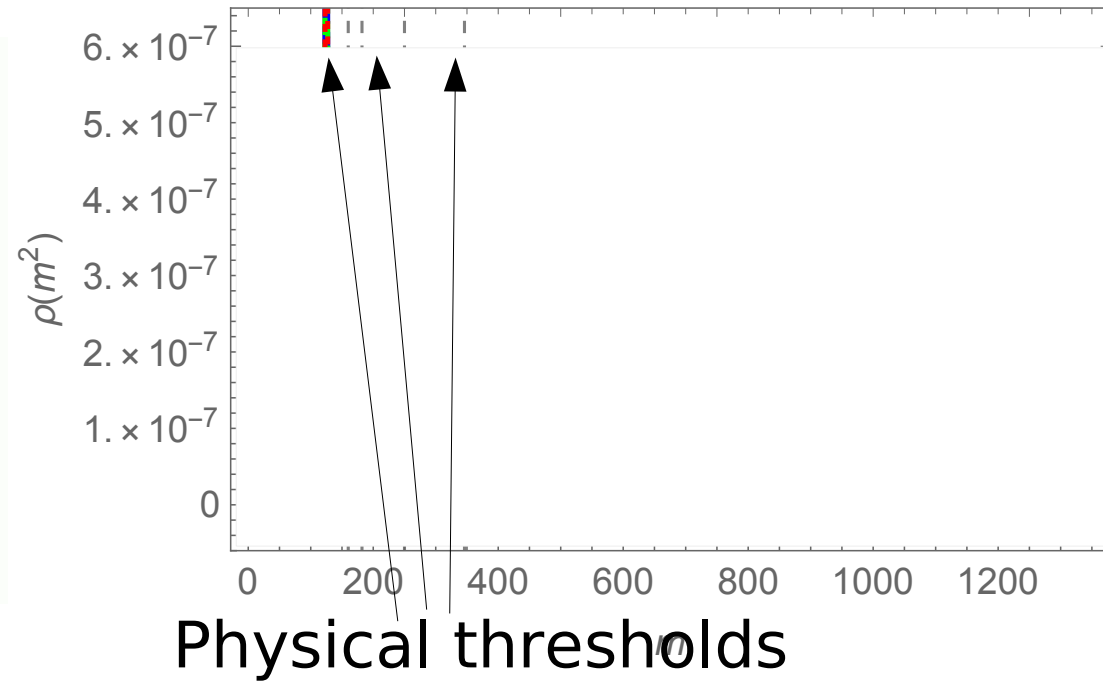
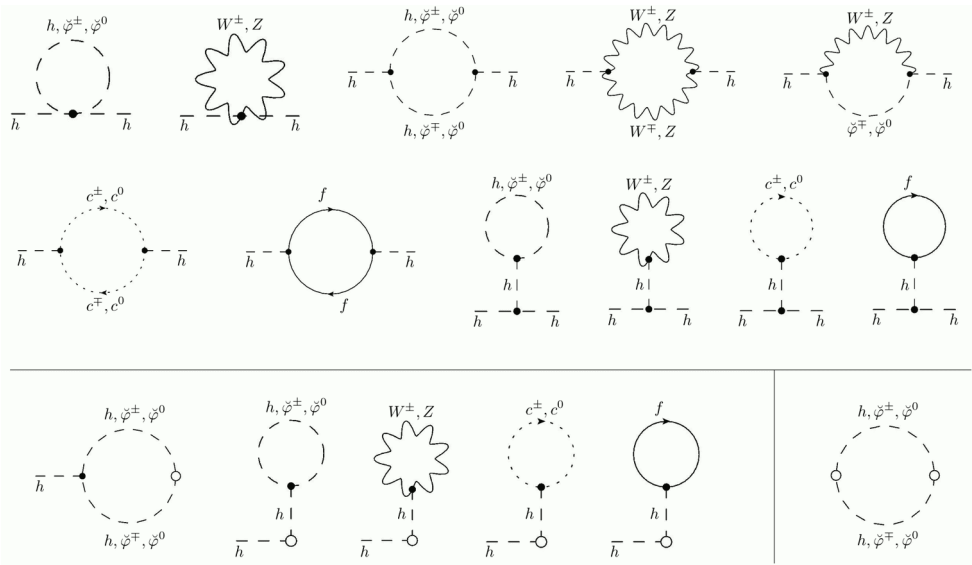


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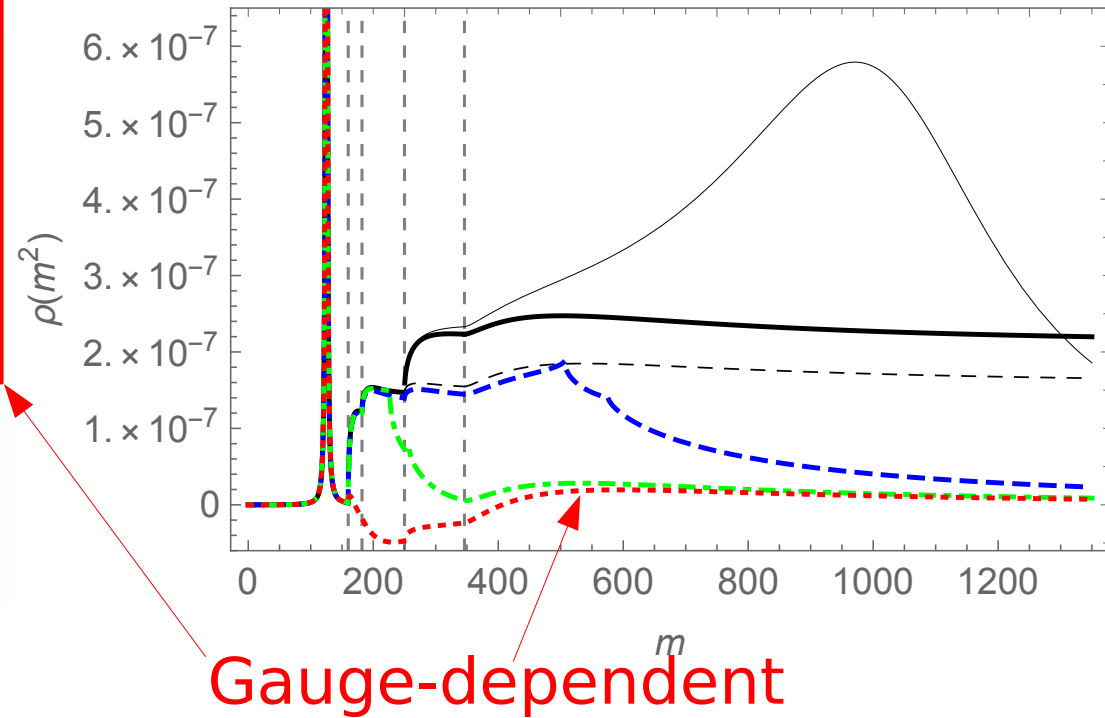
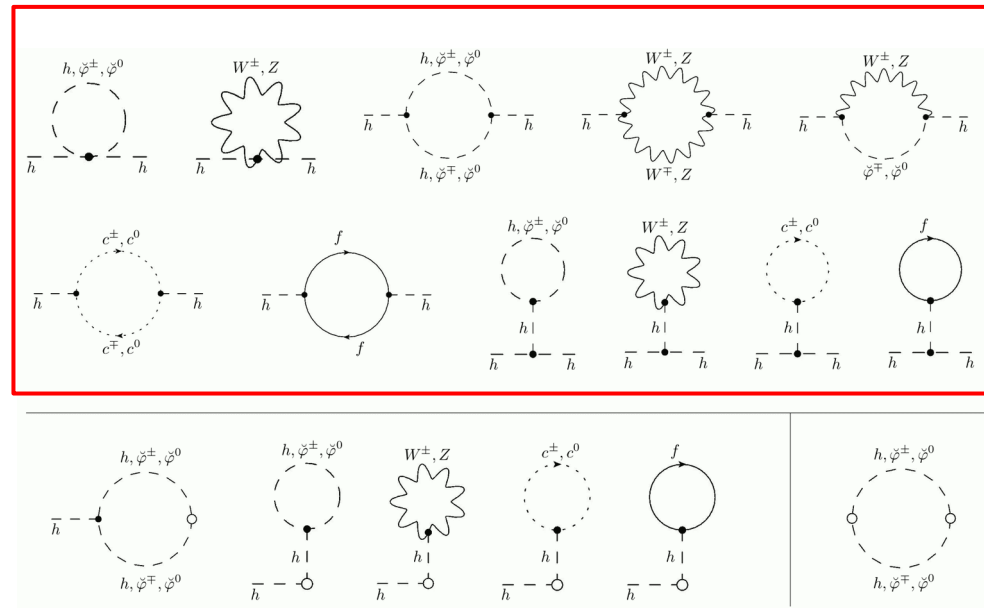
Augmented perturbation theory



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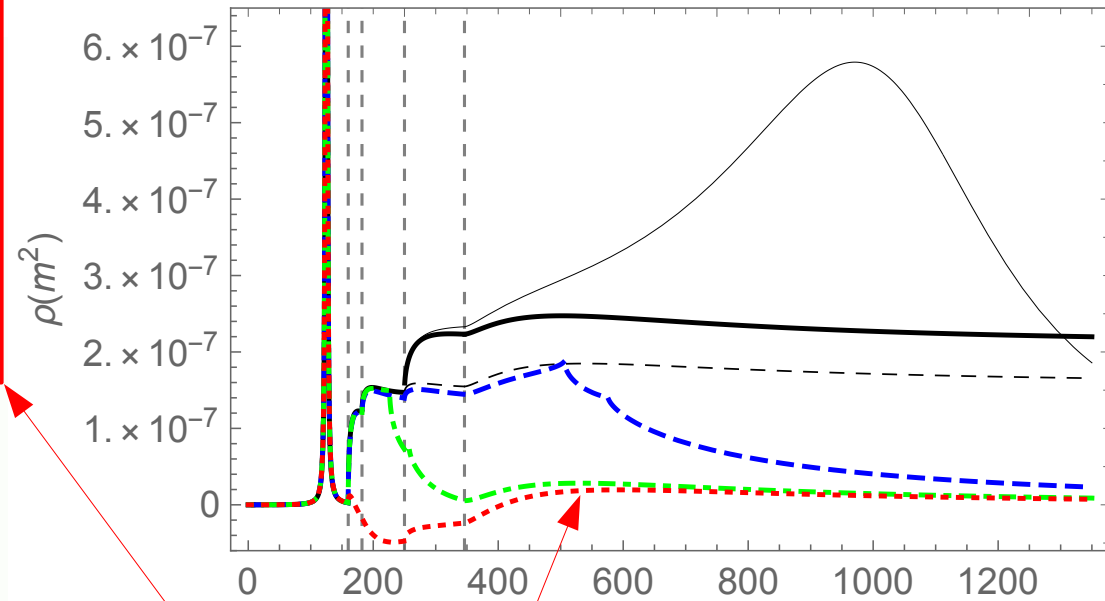
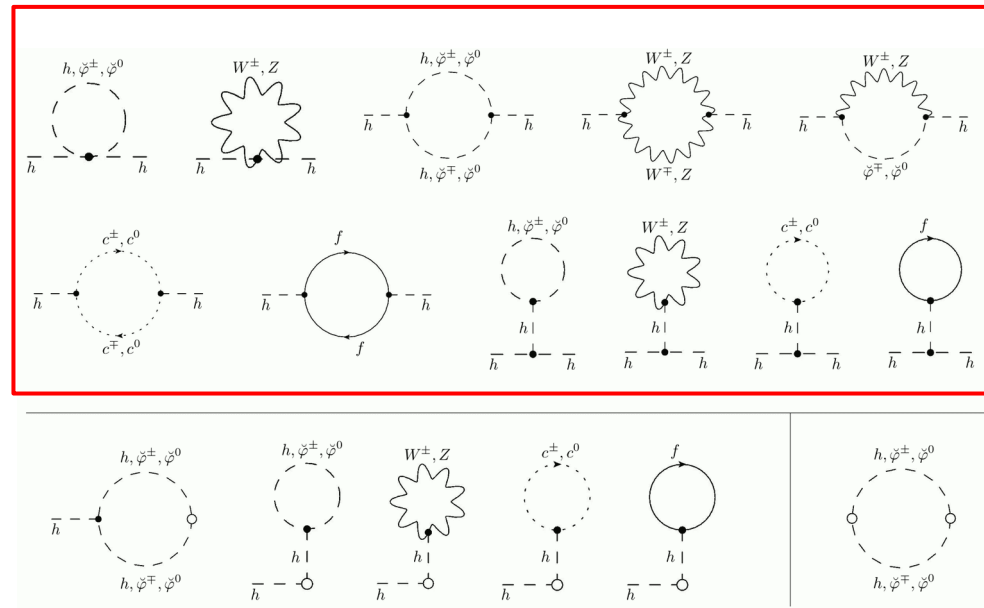


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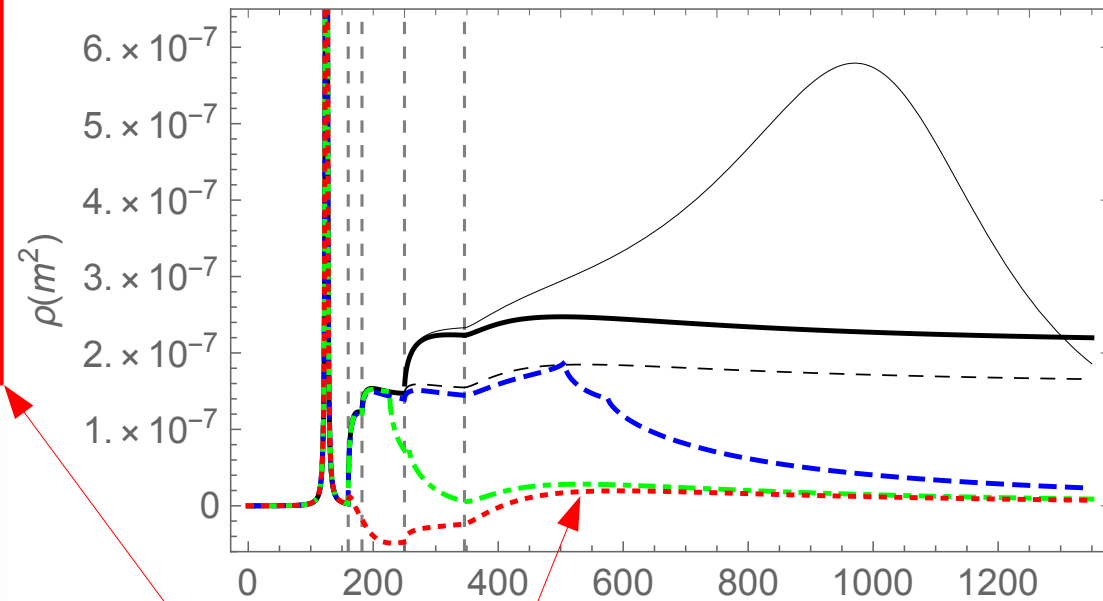
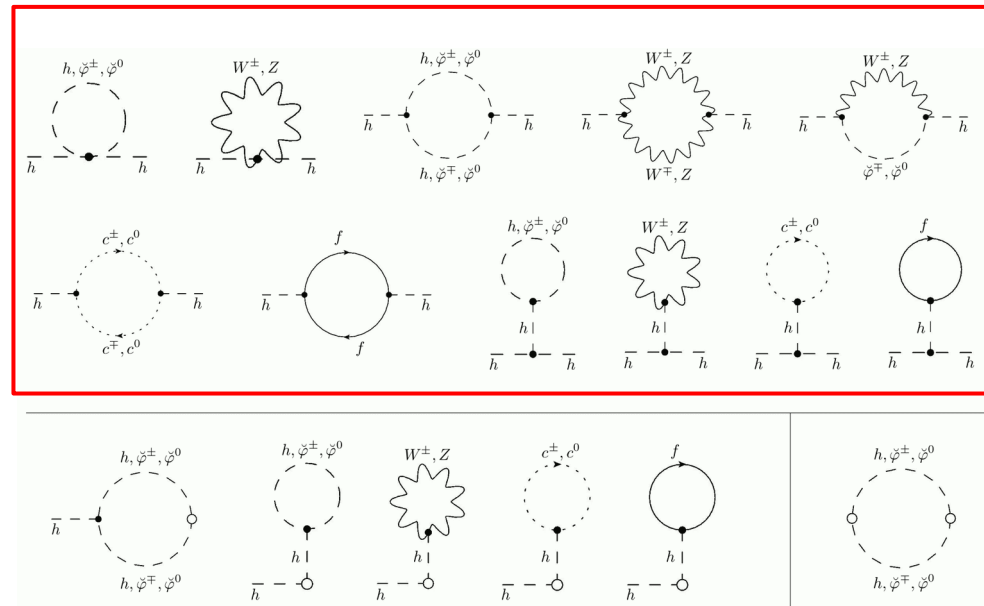
[Maas'12,'17
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Augmented perturbation theory



Gauge-dependent
 Unphysical features:
 Positivity violation
 Additional thresholds

Augmented perturbation theory



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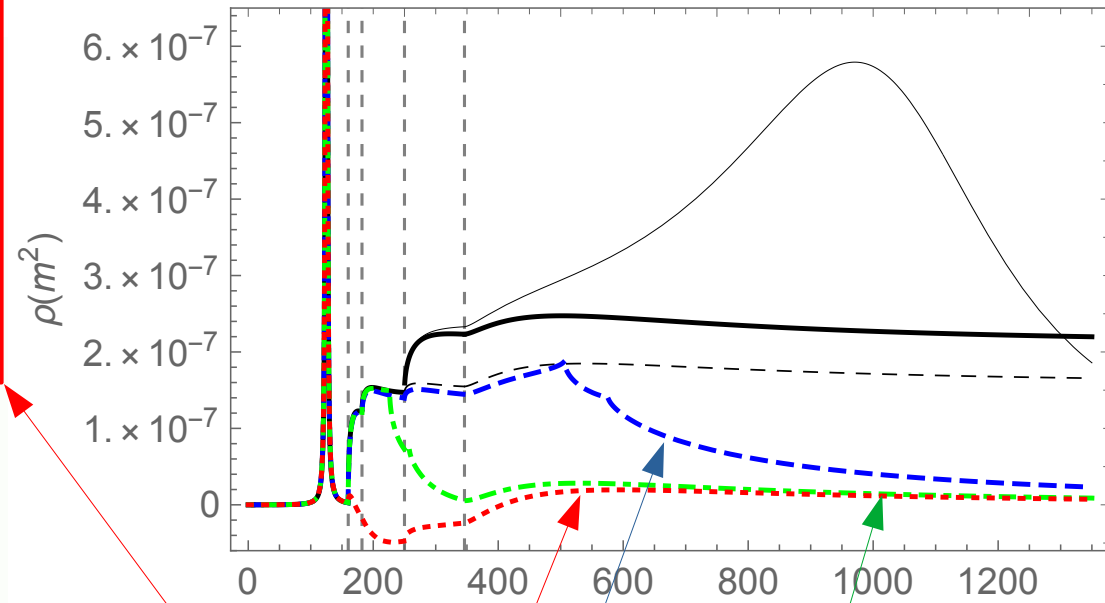
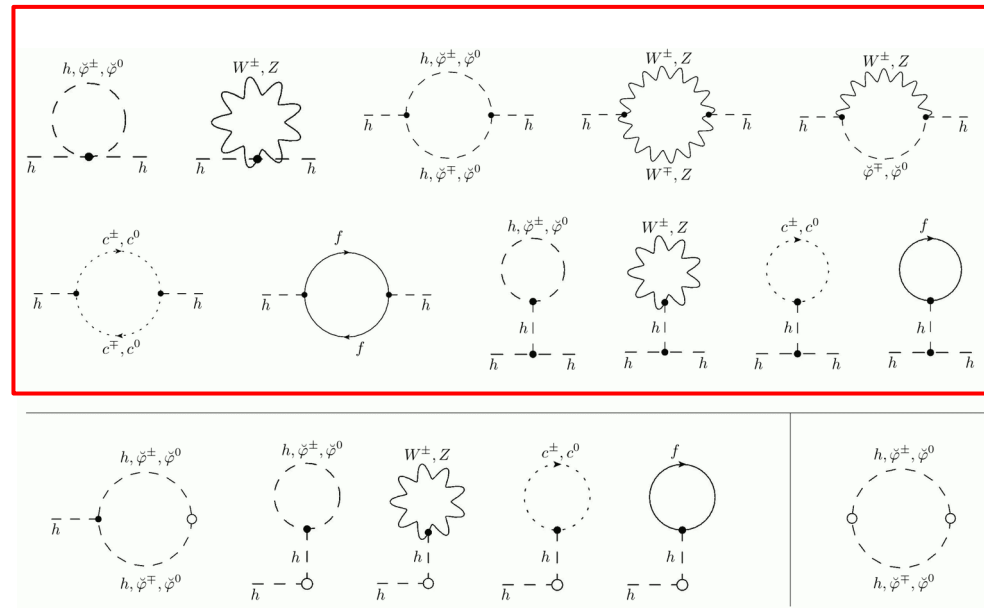
Positivity violation

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Not a consequence
of instability: Occurs even
for an asymptotically stable
Higgs in a toy theory

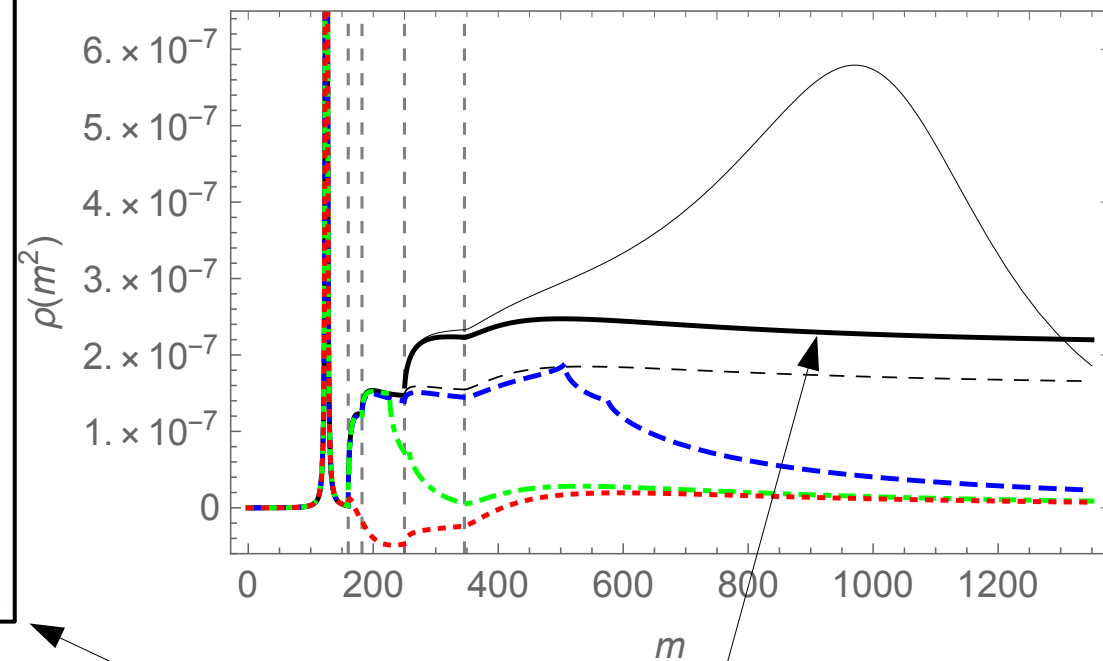
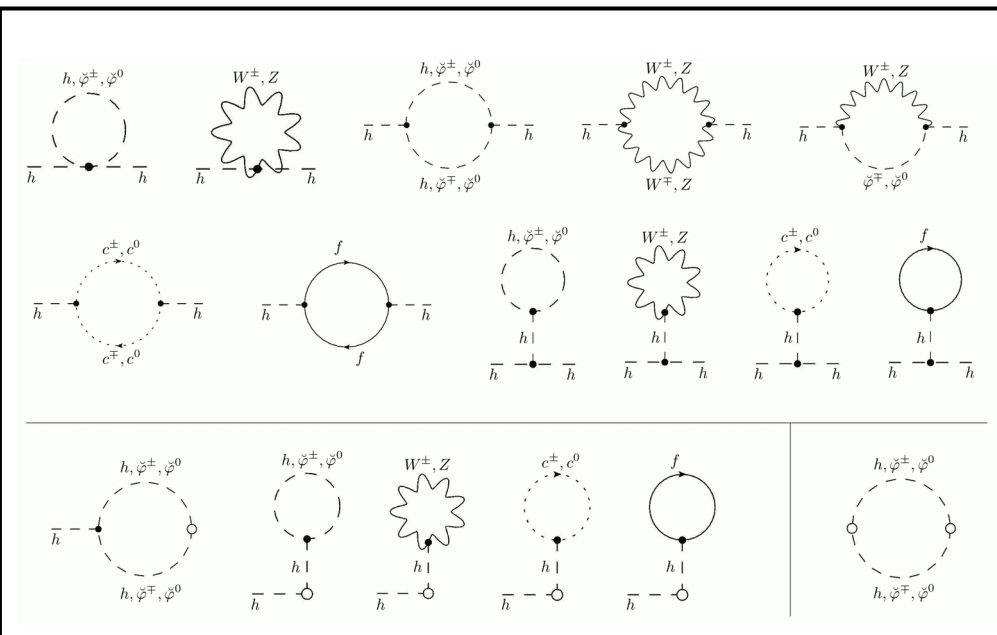
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Augmented perturbation theory



Gauge-dependent
Other gauge choices

Augmented perturbation theory



Physical – same for all gauge choices

What about the vector?

[Fröhlich et al.'80,'81
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1⁻ triplet: $\langle (\tau^i h^\dagger D_\mu h)(x) (\tau^j h^\dagger D_\mu h)(y) \rangle$

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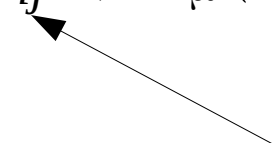
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c projects custodial
states to gauge
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Exactly one gauge boson
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Exactly one gauge boson
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Gauge-invariant operator has on-shell physical,
observable polarization states

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 - Local $SU(2)$ weak gauge (up/down distinction)

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- Same argument: Weak gauge not observable
- Replaced by bound state – FMS applicable

$$\left| \left\langle \begin{pmatrix} h_2 & -h_1 \\ h_1^* & h_2^* \end{pmatrix} \begin{pmatrix} \mathbf{v}_L \\ l_L \end{pmatrix} \right\rangle_i (x) + \left\langle \begin{pmatrix} h_2 & -h_1 \\ h_1^* & h_2^* \end{pmatrix} \begin{pmatrix} \mathbf{v}_L \\ l_L \end{pmatrix} \right\rangle_j (y) \right| \stackrel{h=v+\eta}{\approx} v^2 \left| \begin{pmatrix} \mathbf{v}_L \\ l_L \end{pmatrix} (x) + \begin{pmatrix} \mathbf{v}_L \\ l_L \end{pmatrix} (y) \right| + O(\eta)$$

- Gauge-invariant state, but custodial doublet

- Flavor has two components
 - Global SU(3) generation
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- **Gauge-invariant state**, **but custodial doublet**
- Yukawa terms break custodial symmetry
 - Different masses for doublet members
- Can this be true? Lattice test

Flavor on the lattice

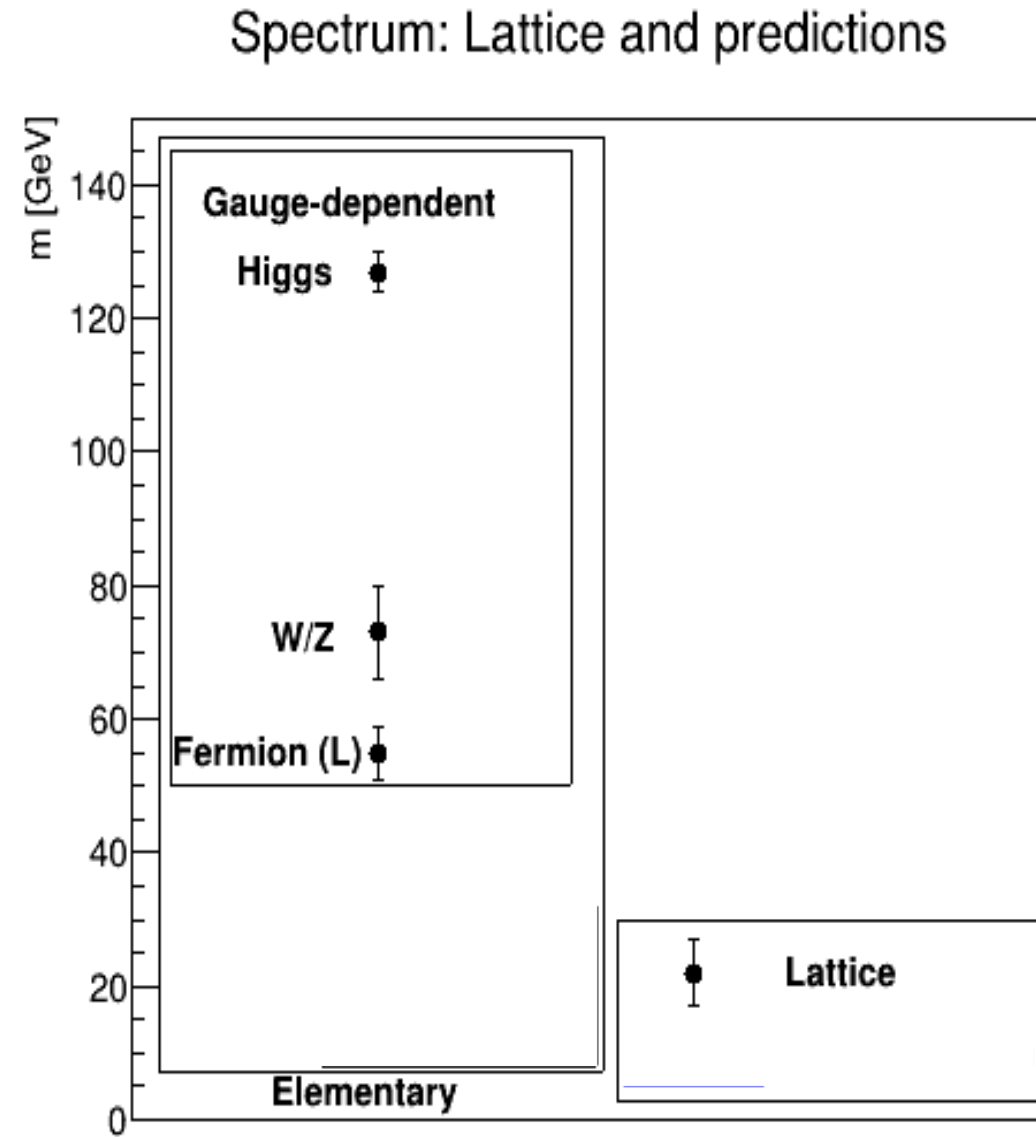
- Only mock-up standard model
 - Compressed mass scales
 - One generation
 - Degenerate leptons and neutrinos
 - Dirac fermions: left/right-handed non-degenerate
 - Quenched

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- Same qualitative outcome
 - FMS construction
 - Mass defect
 - Flavor and custodial symmetry patterns

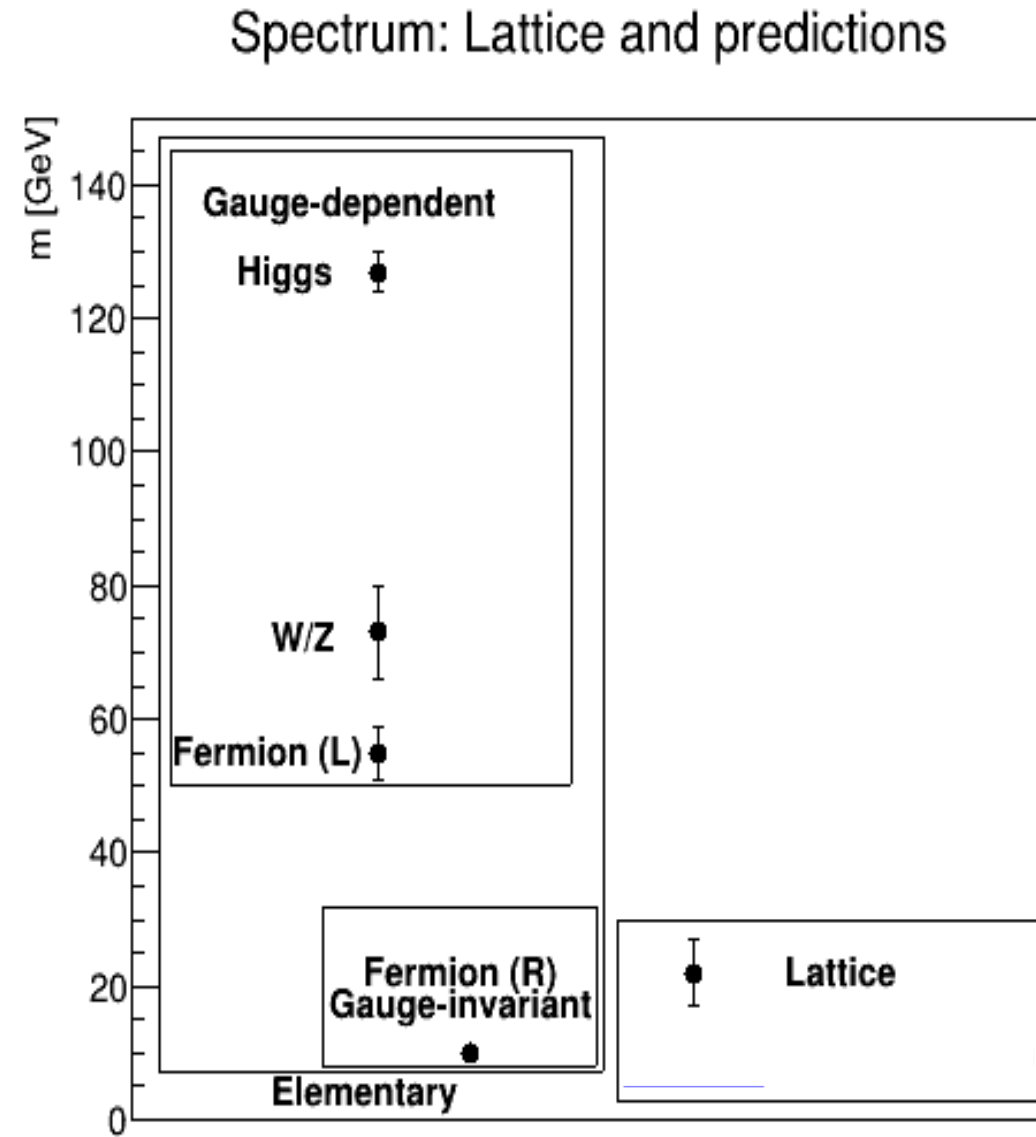
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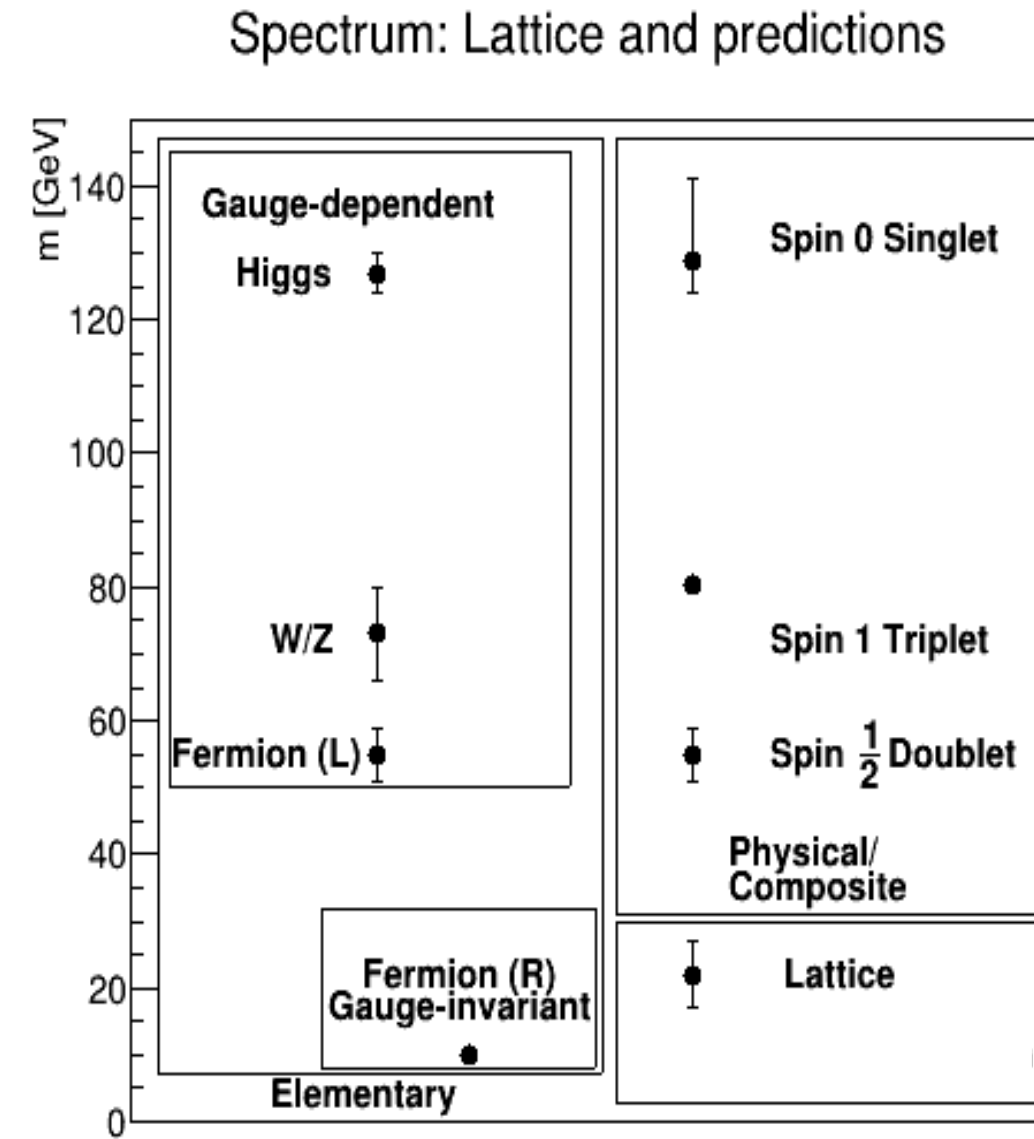
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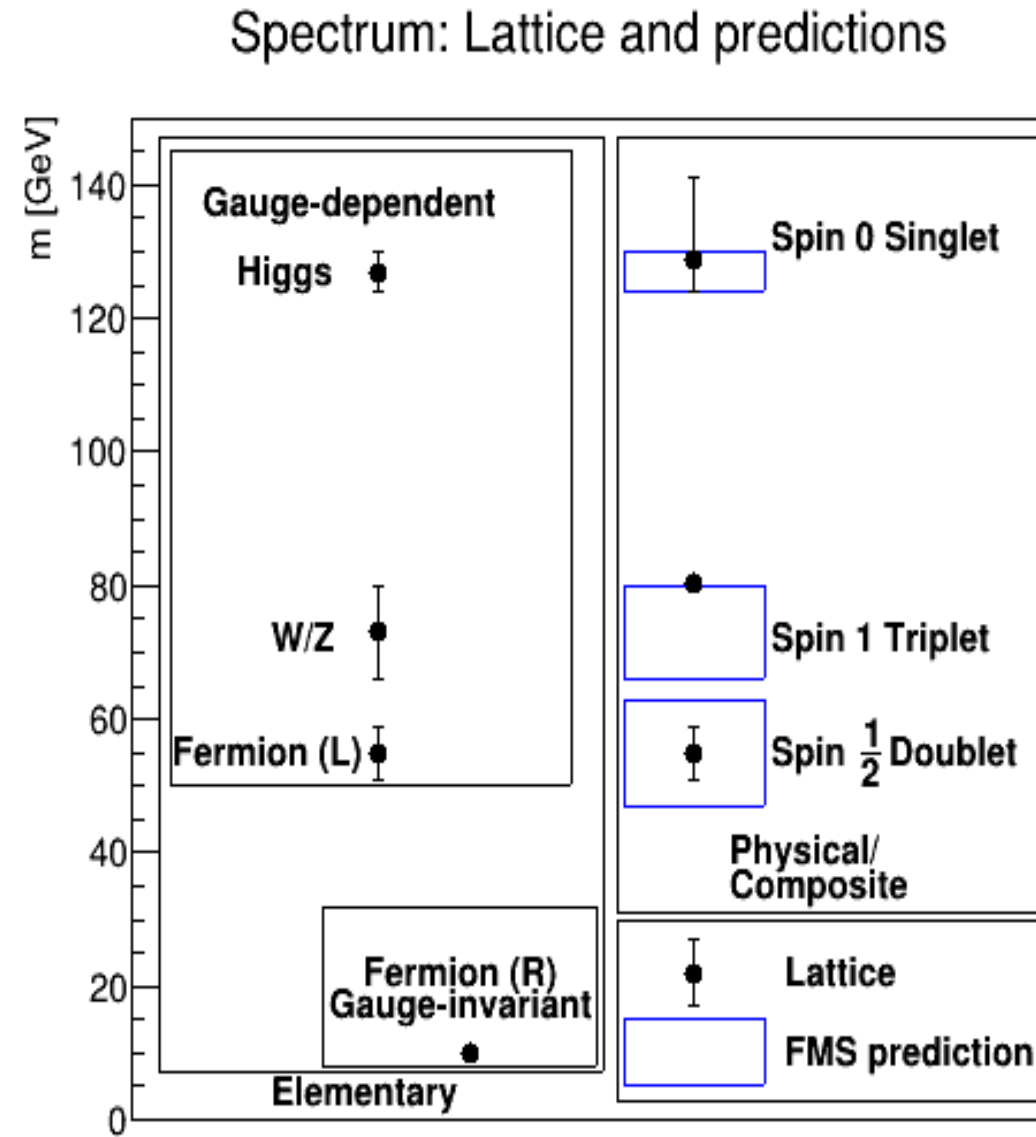
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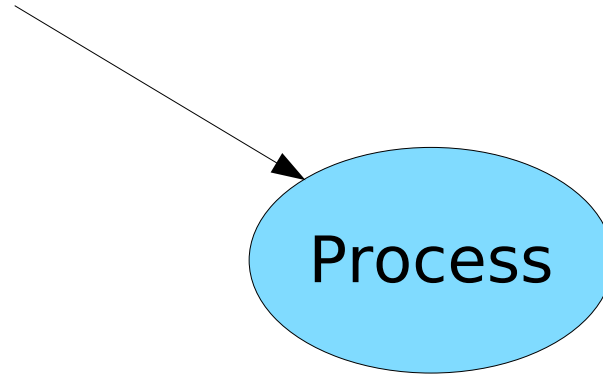
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- Supports FMS prediction



Scattering

[Maas et al.'17
Maas & Reiner '22
Maas, Plätzer et al.' unpublished]

Incoming (asymptotic) particle
Standard LSZ: Elementary particle

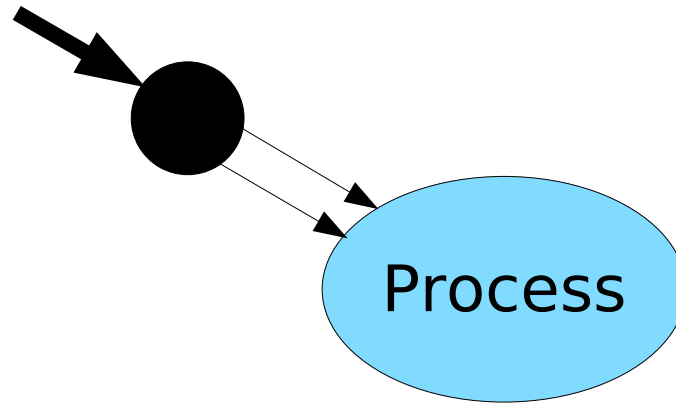


$$\langle f(p) \dots \rangle$$

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Gauge-invariant LSZ: Bound state

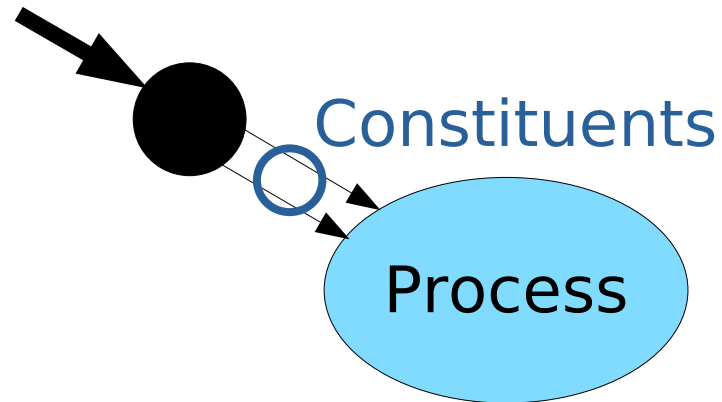


$$\langle (Hf)(p) \dots \rangle$$

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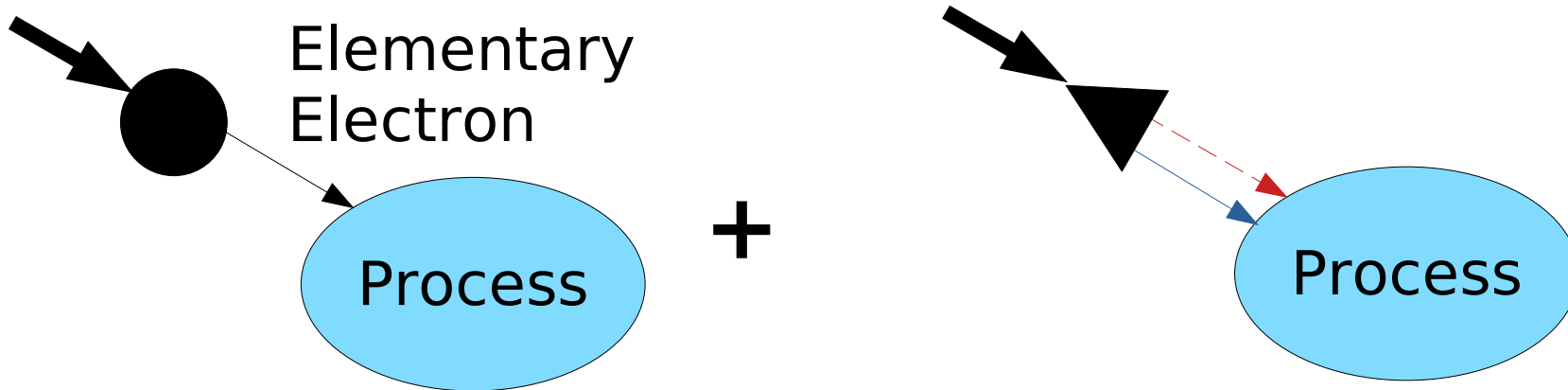


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Incoming (asymptotic) particle
FMS LSZ: Elementary and fluctuations

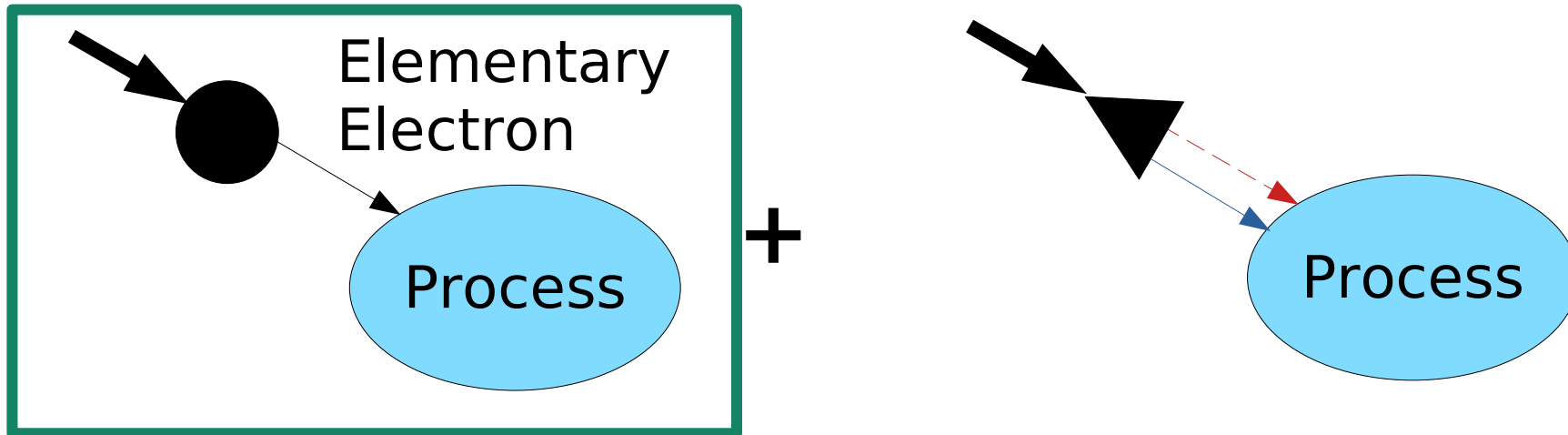


$$v \langle f(p) \dots \rangle + \int dq \Gamma(P, q) D_f(p - q) D_h(q) \langle h(q) f(P - q) \dots \rangle$$

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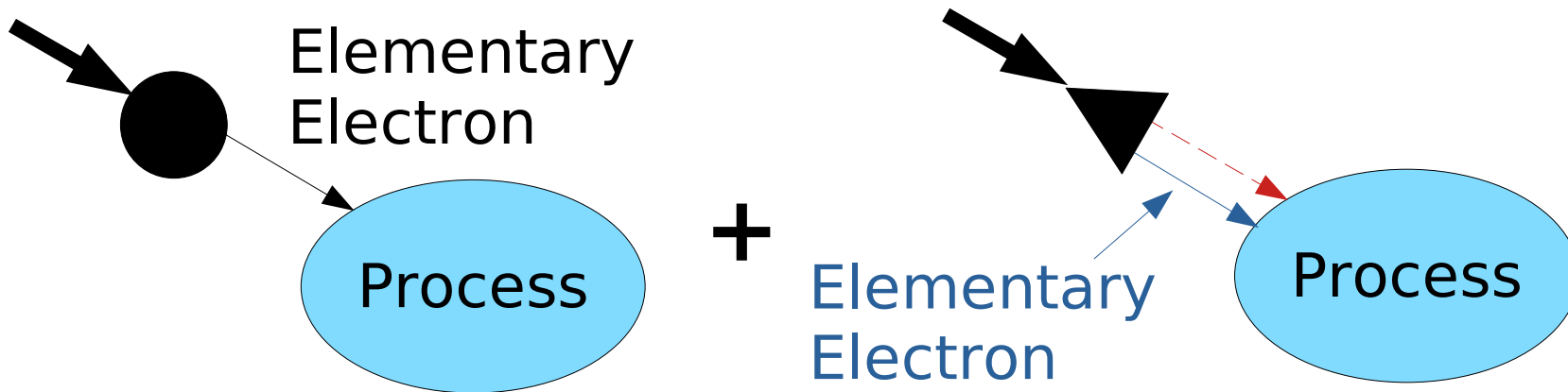
Standard perturbation theory

$$\boxed{v \langle f(p) \dots \rangle} + \int dq \Gamma(P, q) D_f(p - q) D_h(q) \langle h(q) f(P - q) \dots \rangle$$

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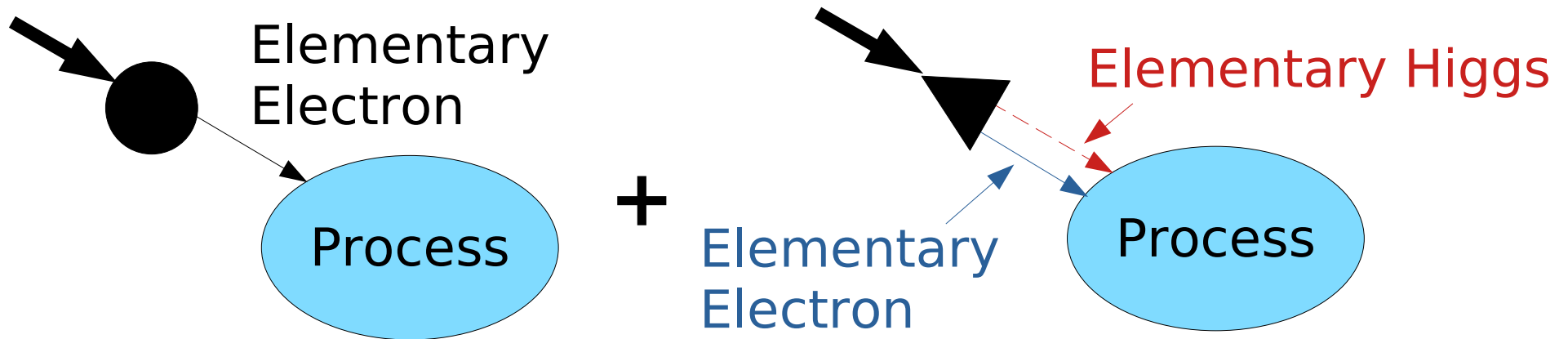


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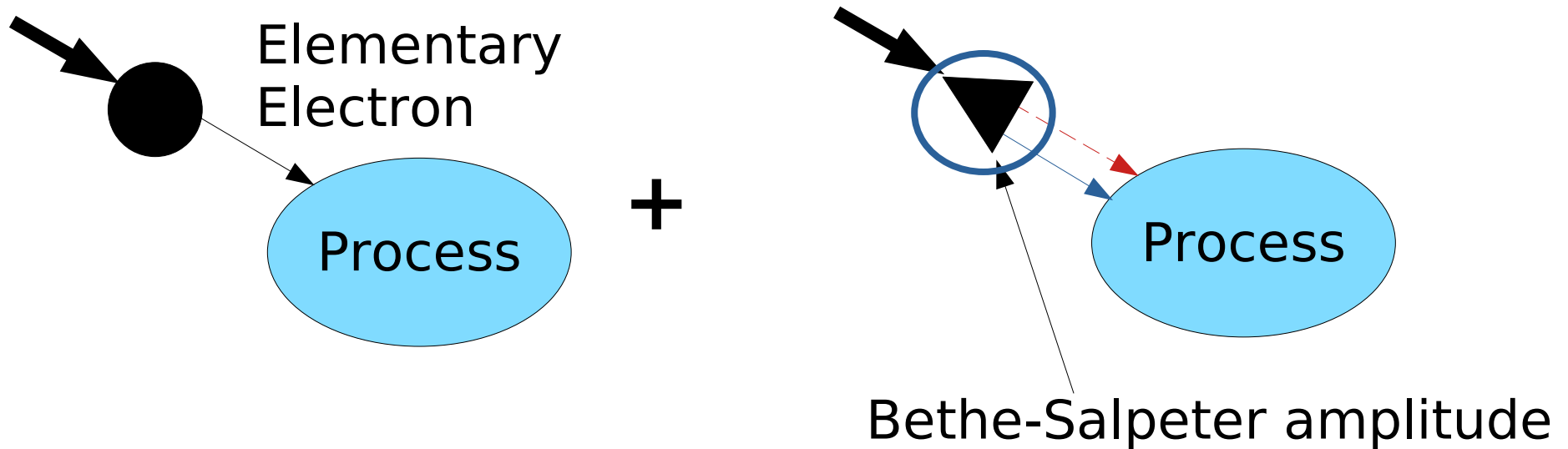


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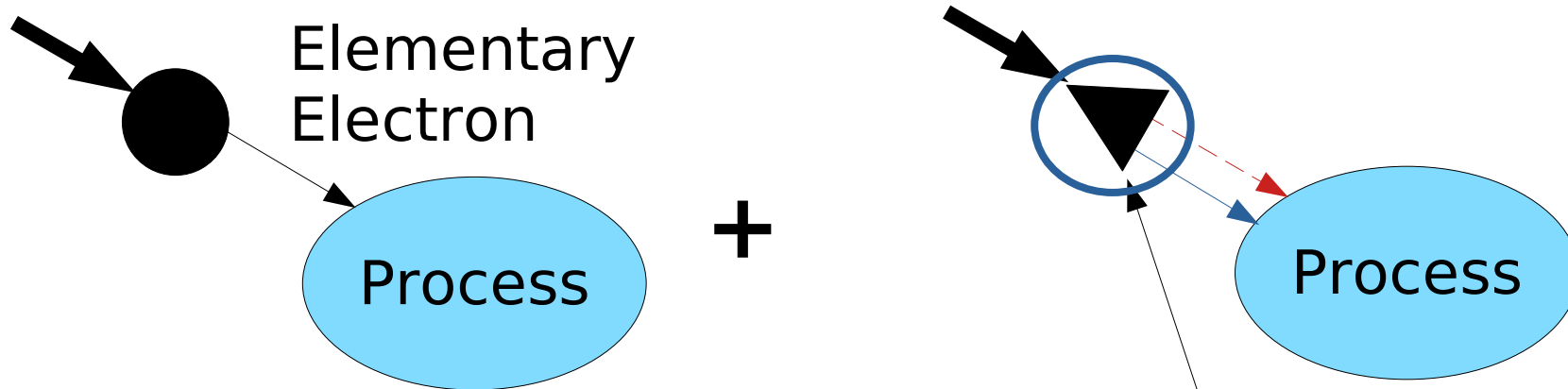


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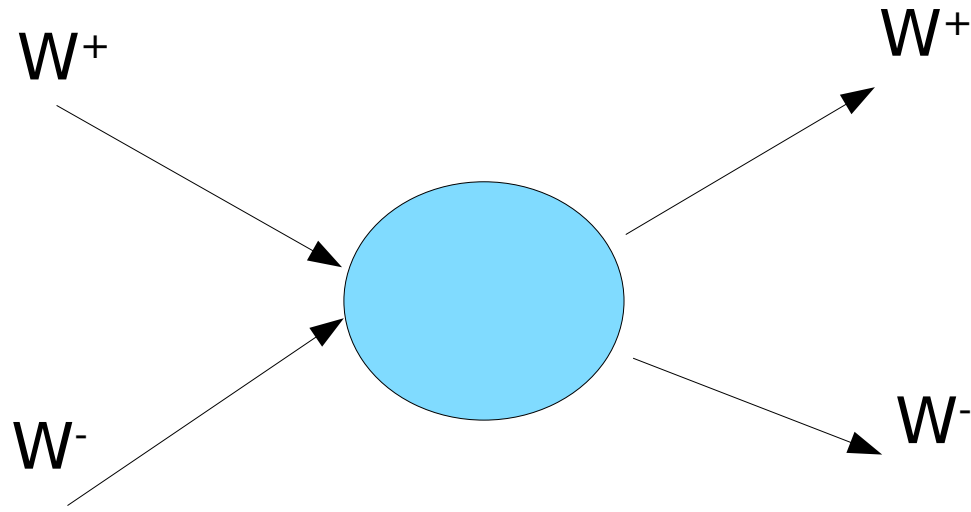


Bethe-Salpeter amplitude:
Calculate in augmented PT

$$v \langle f(p) \dots \rangle + \int dq \Gamma(P, q) D_f(p-q) D_h(q) \langle h(q) f(P-q) \dots \rangle$$

Phase shifts in on-shell VBS/VBF

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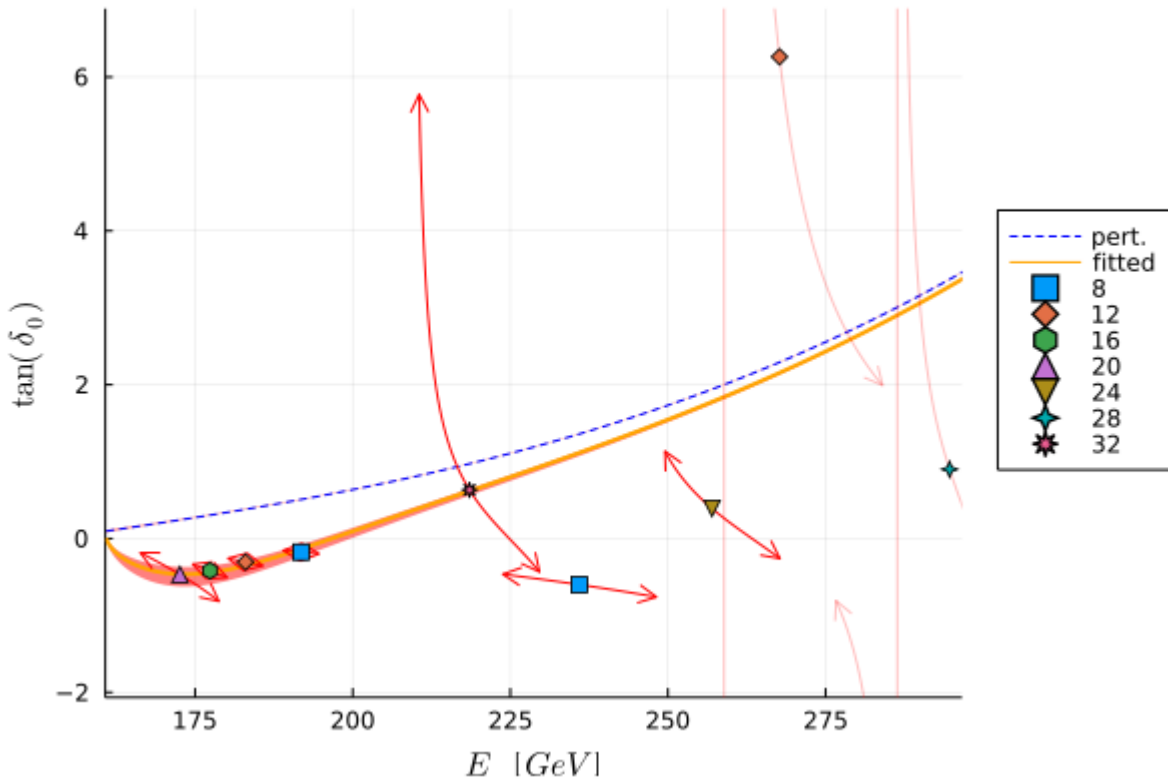


Elastic scattering, s-wave, $160^2 < s < 250^2$

Phase shifts in on-shell VBS/VBF

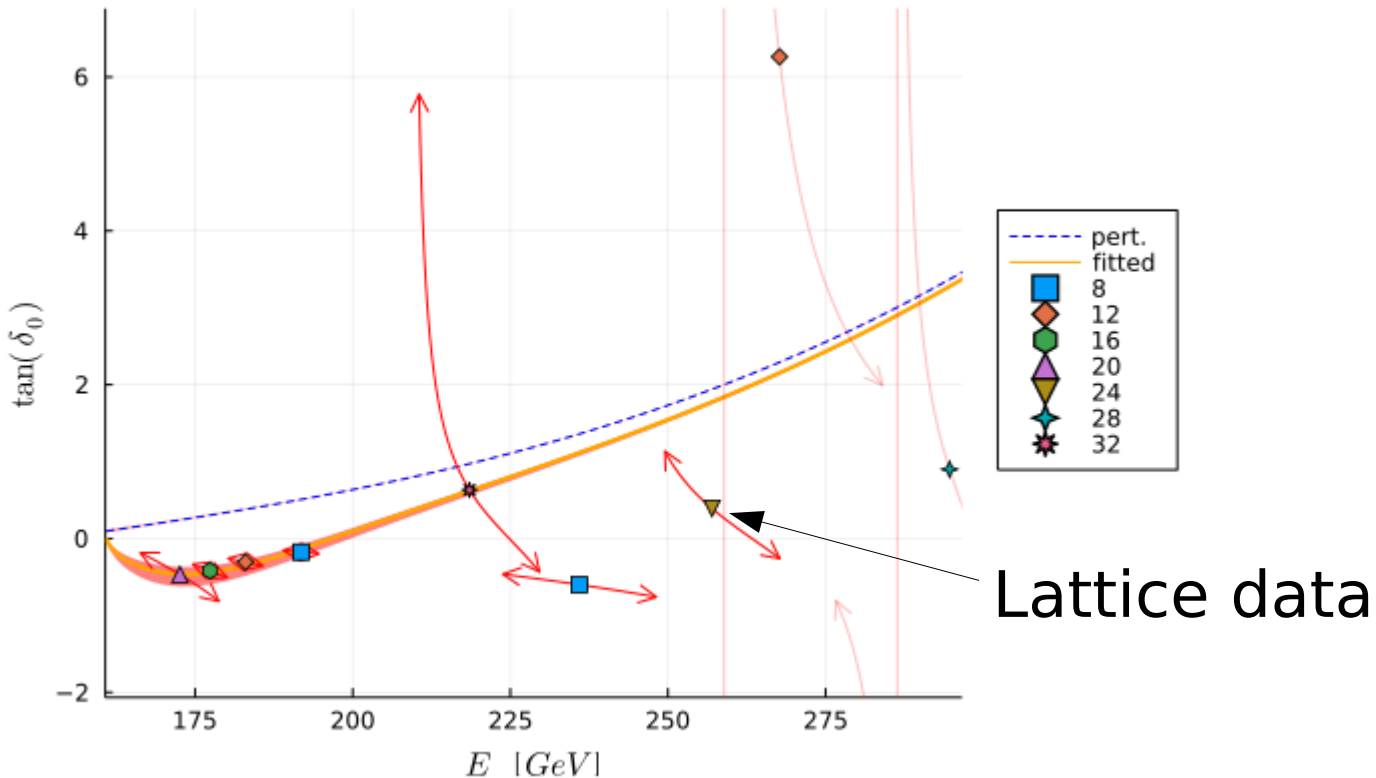
- Reduced SM: Only W/Z and the Higgs
 - Parameters slightly different
 - Higgs 145 GeV and weak coupling larger
 - Standard lattice Lüscher analysis
 - Qualitatively but not quantitatively

Phase shifts in on-shell VBS/VBF



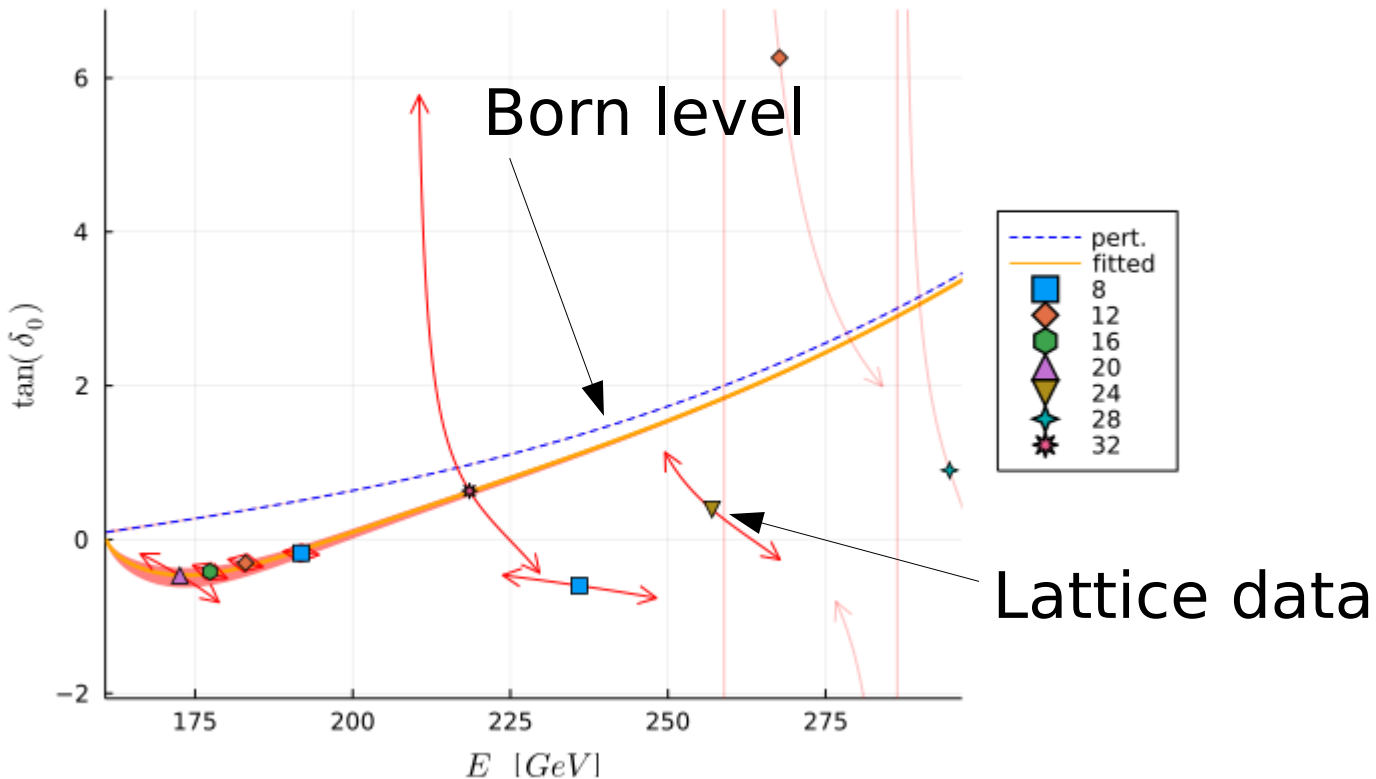
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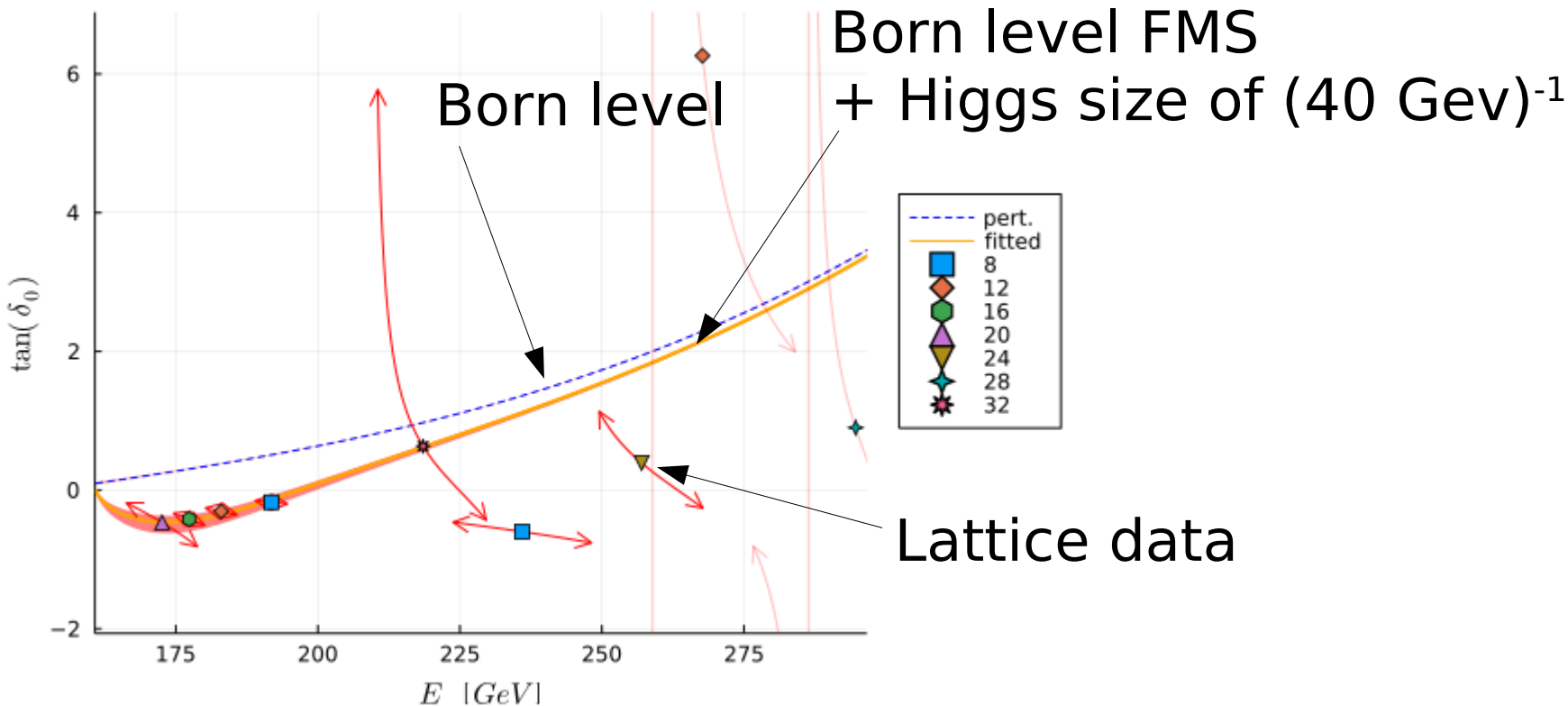
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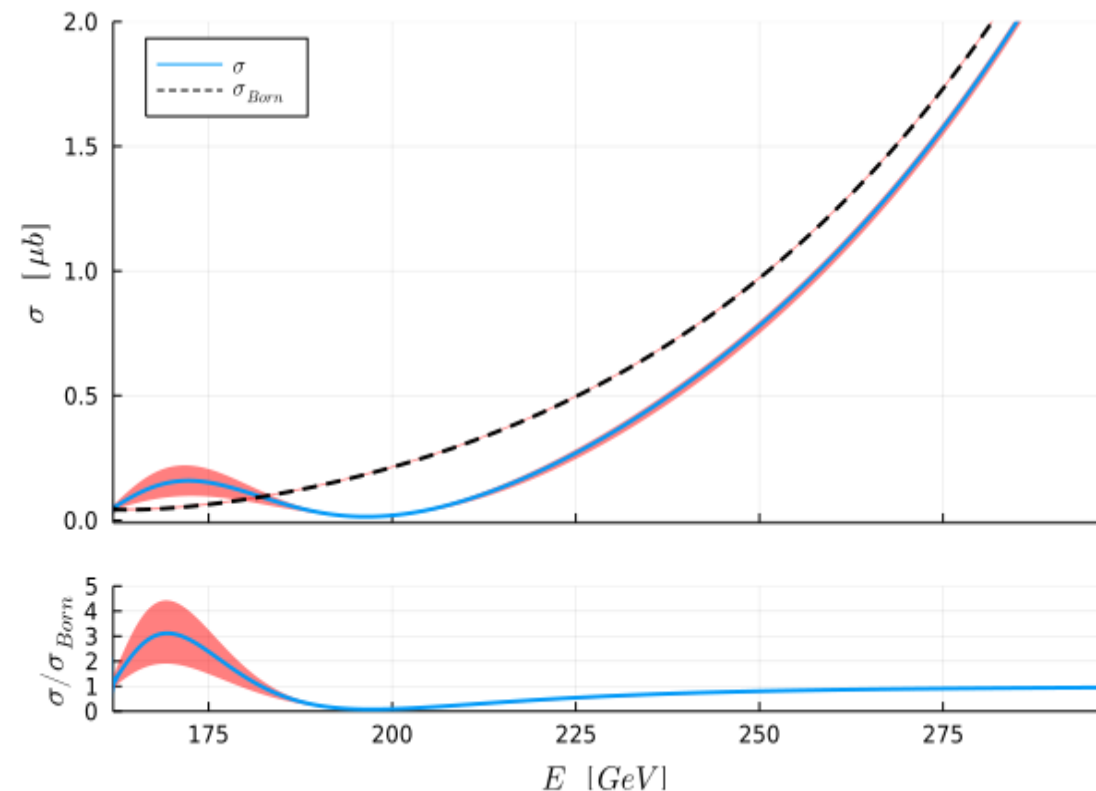
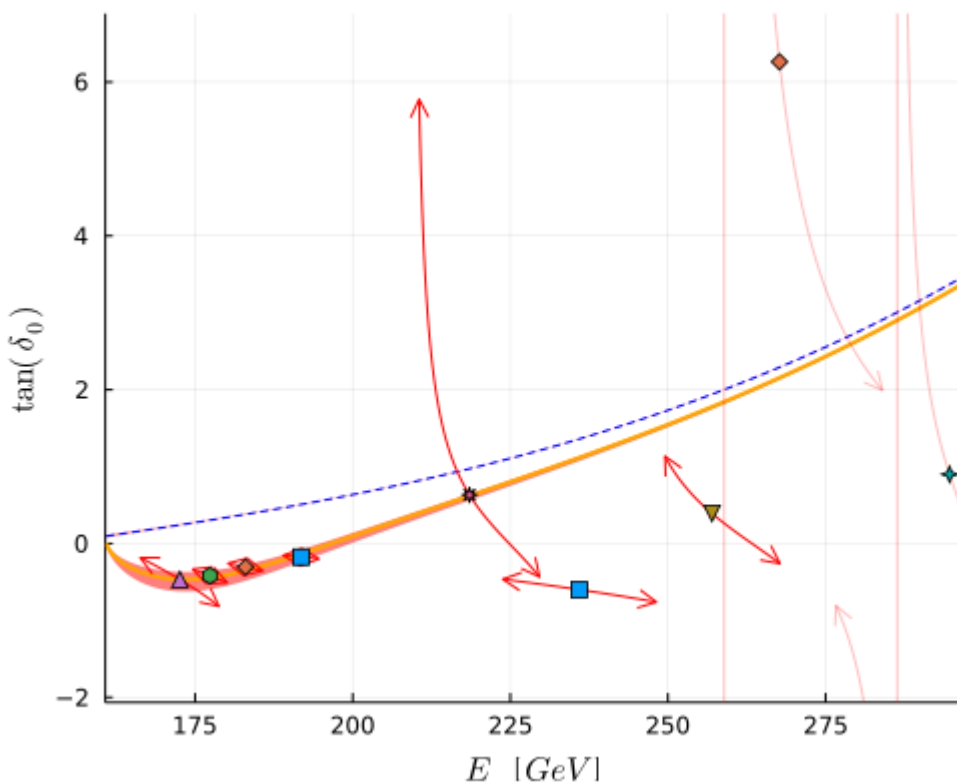
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Resummation effects

[Ciafaloni et al. '00]

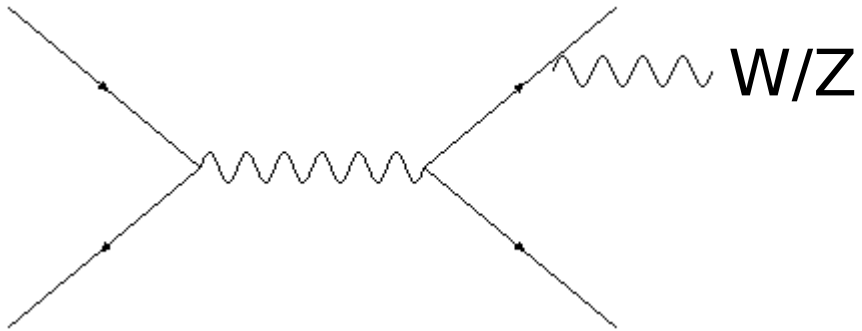
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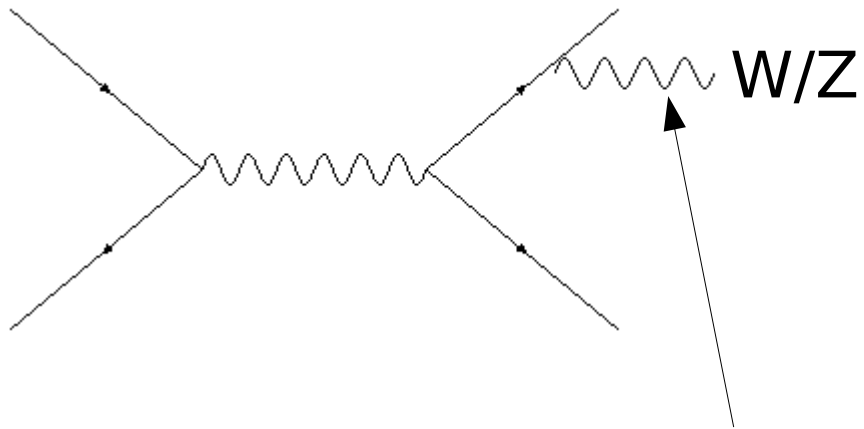
Standard perturbation theory



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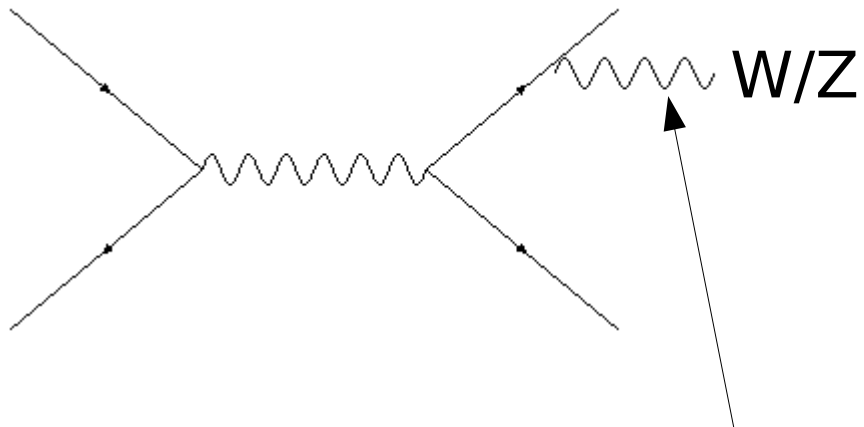


Resumming real emission

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[Ciafaloni et al. '00]

Standard perturbation theory

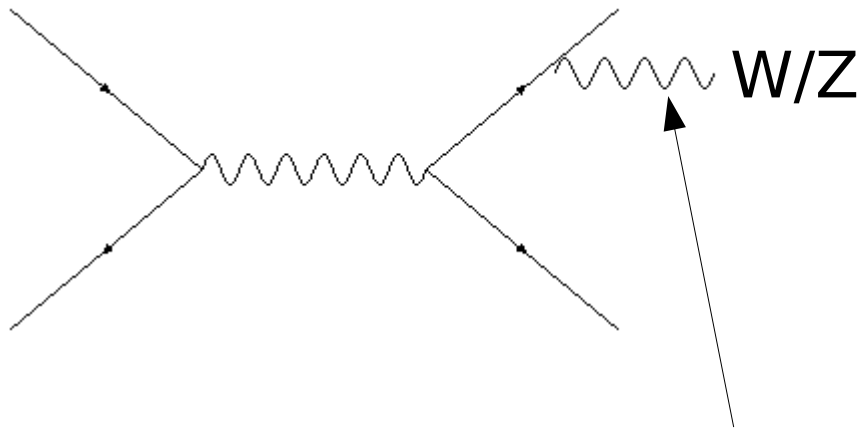


Resumming real (almost collinear) emission: Weak jet

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[Ciafaloni et al. '00]

Standard perturbation theory



Resumming real (almost collinear) emission: Weak jet

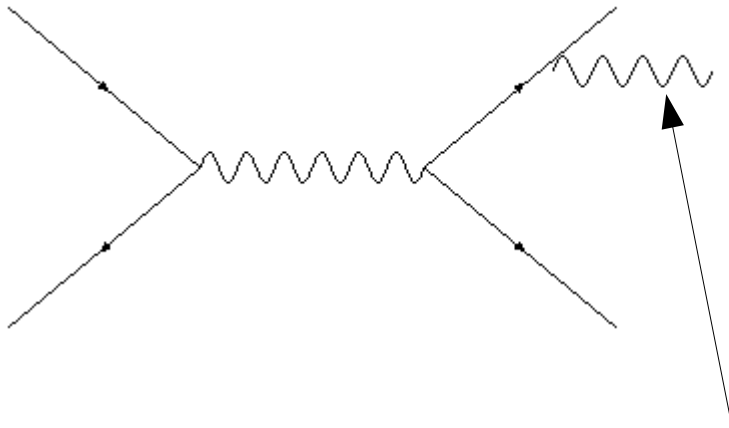
$$\frac{\Delta \sigma}{\sigma_{noresummation}} \sim \ln^2 \frac{s}{m_W^2}$$

at 1 TeV of the same
order as strong
corrections

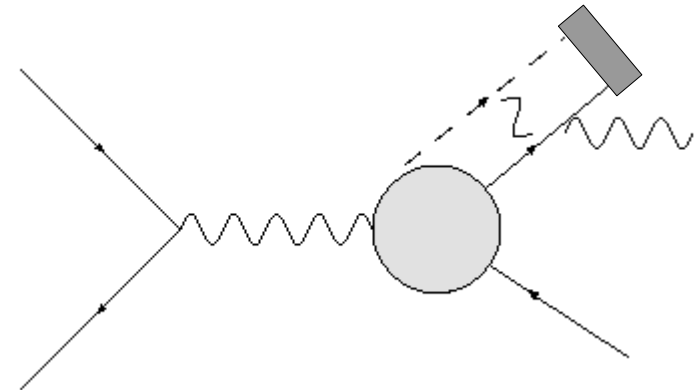
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[Ciafaloni et al. '00
Maas et al.'22]

Standard perturbation theory



Augmented by correct asymptotic state



Resumming real emission

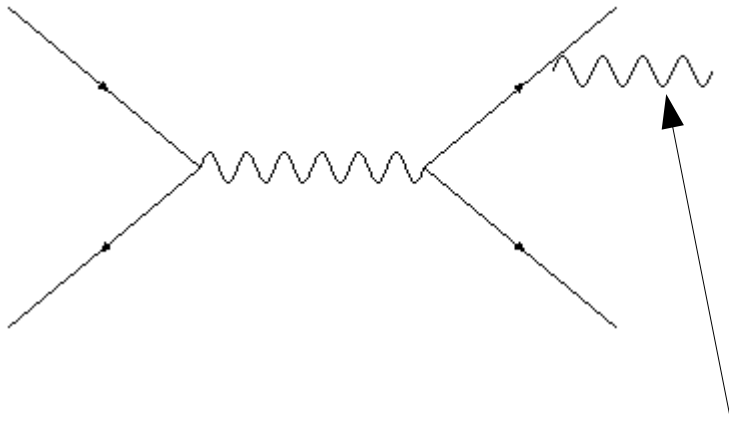
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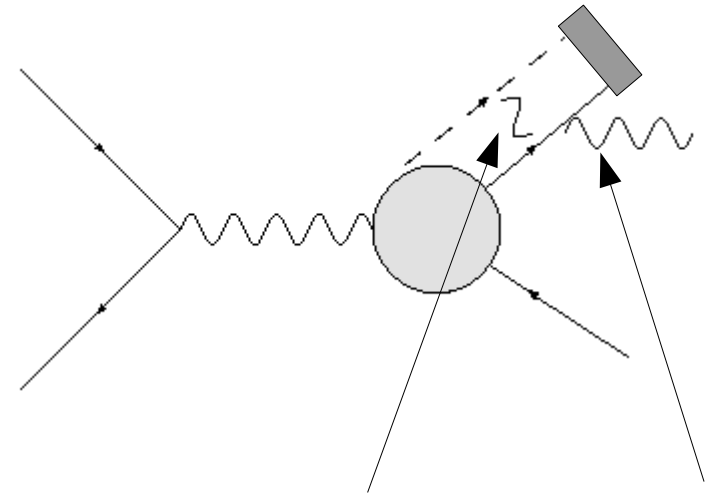


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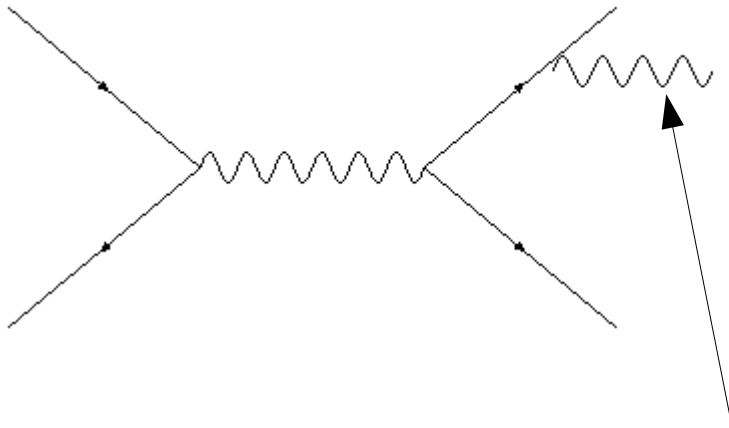
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Virtual and real
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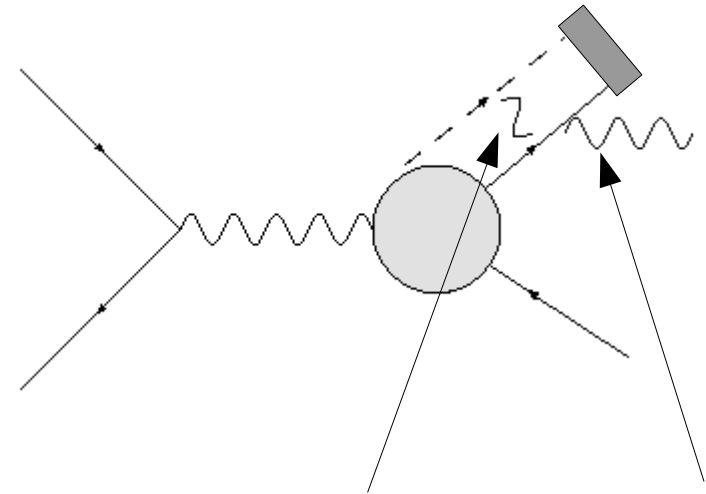


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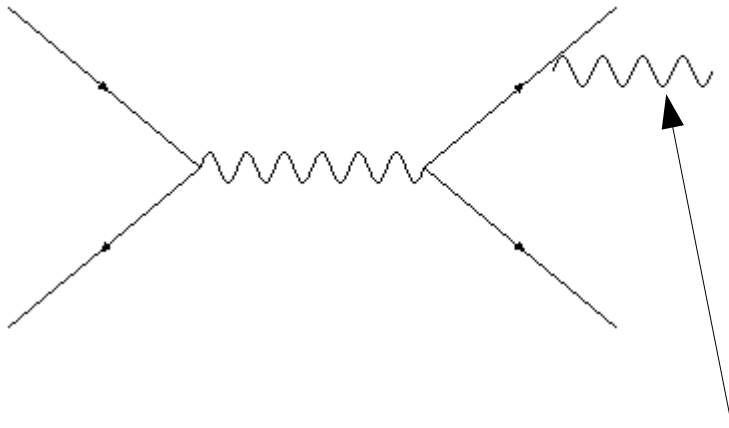
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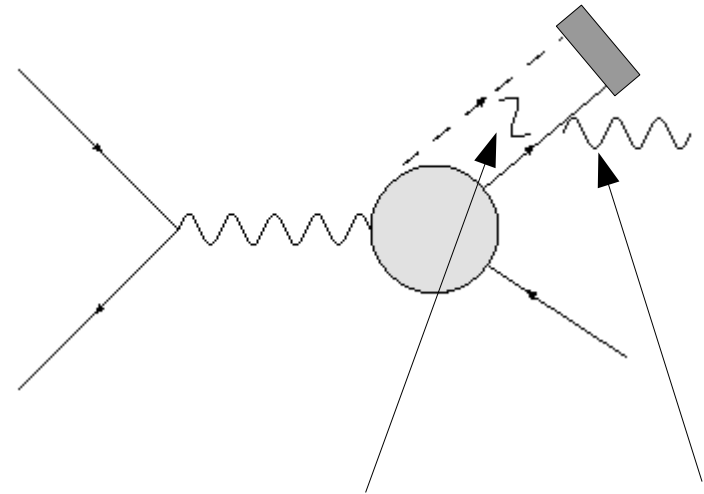


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Less weak jets

Summary

Review: 1712.04721

Update: 2305.01960

- Field theory requires change of asymptotic states
 - Can be treated using FMS-augmented perturbation theory
 - Changes in the SM at one or two loop orders

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