

Electroweak Phenomenology from Fundamental Field Theory

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Germany



NAWI Graz
Natural Sciences

FWF

Der Wissenschaftsfonds

What is this talk about?

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- Why the field theory of the standard model is more tricky than expected

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- Phenomenology
 - Particle spectrum and properties
 - Form factors
 - Tests at LHC

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 - But why you did not yet needed to care
- Phenomenology
 - Particle spectrum and properties
 - Form factors
 - Tests at LHC
- Beyond qualitative: BSM
 - Experimental consequences

Setting the scene

-

The standard model Higgs

A toy model

- Consider an $SU(2)$ with a single fundamental scalar

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- Essentially the standard model Higgs

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- W_s W_μ^a 
- Coupling g and some numbers f^{abc}



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- **Higgs** h_i 
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- Couplings g, v, λ and some numbers f^{abc} and t_a^{ij}
- Parameters selected for a BEH effect

A toy model: Symmetries

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- Global SU(2) custodial (flavor) symmetry

- Acts as (right-)transformation on the scalar field only

$$W_\mu^a \rightarrow W_\mu^a \qquad h \rightarrow h \Omega$$

Textbook approach

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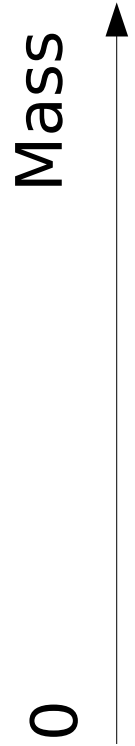
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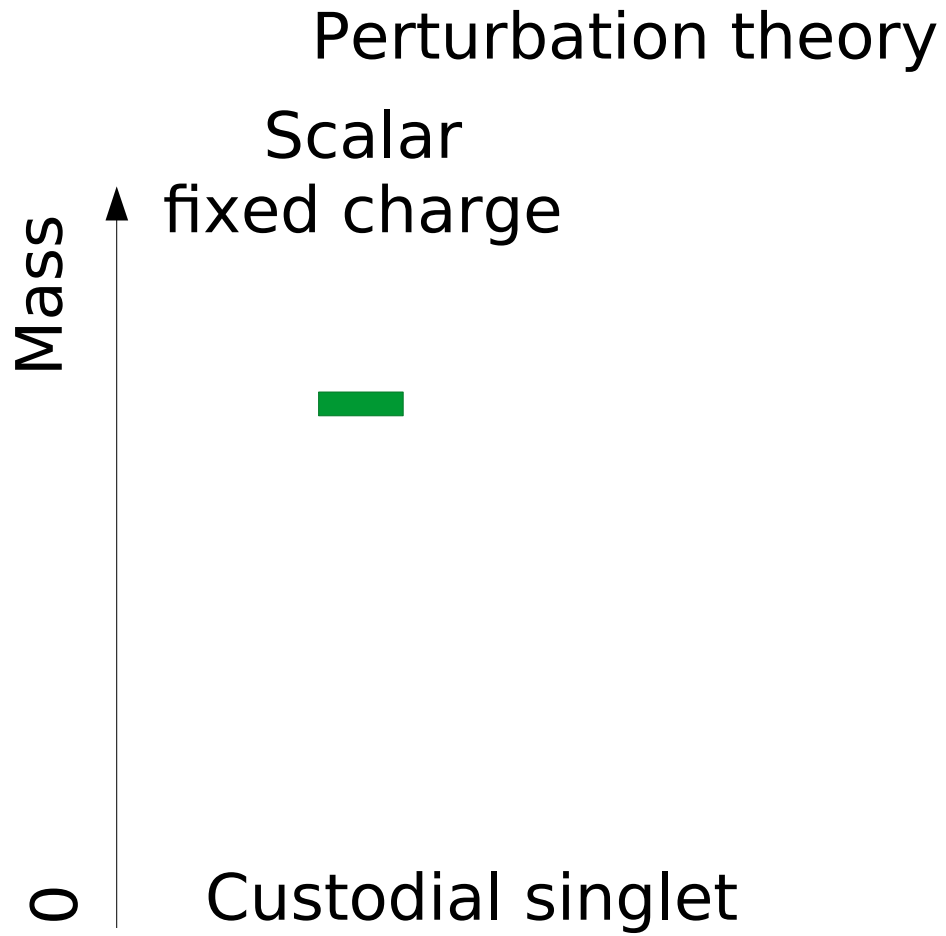
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- Choose a suitable gauge and obtain 'spontaneous gauge symmetry breaking': $SU(2) \rightarrow 1$
- Get masses and degeneracies at tree-level
- Perform perturbation theory

Physical spectrum

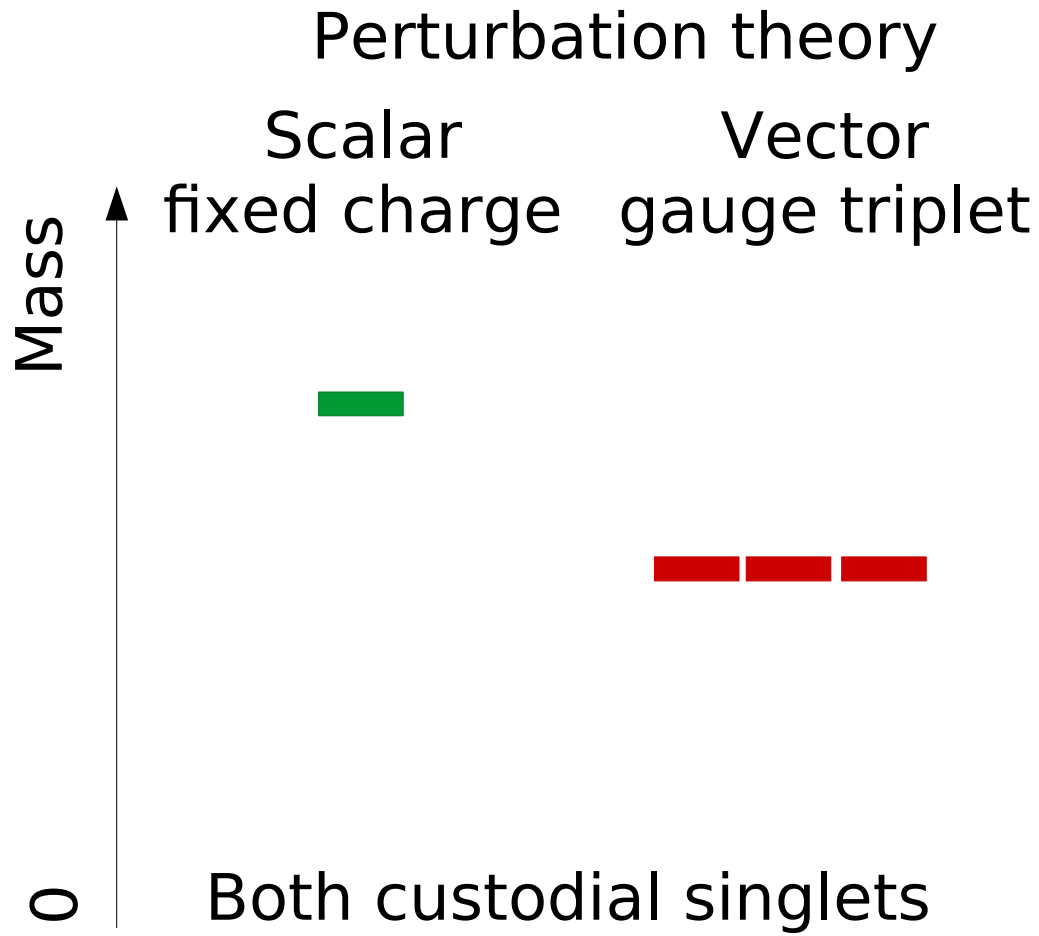
Perturbation theory



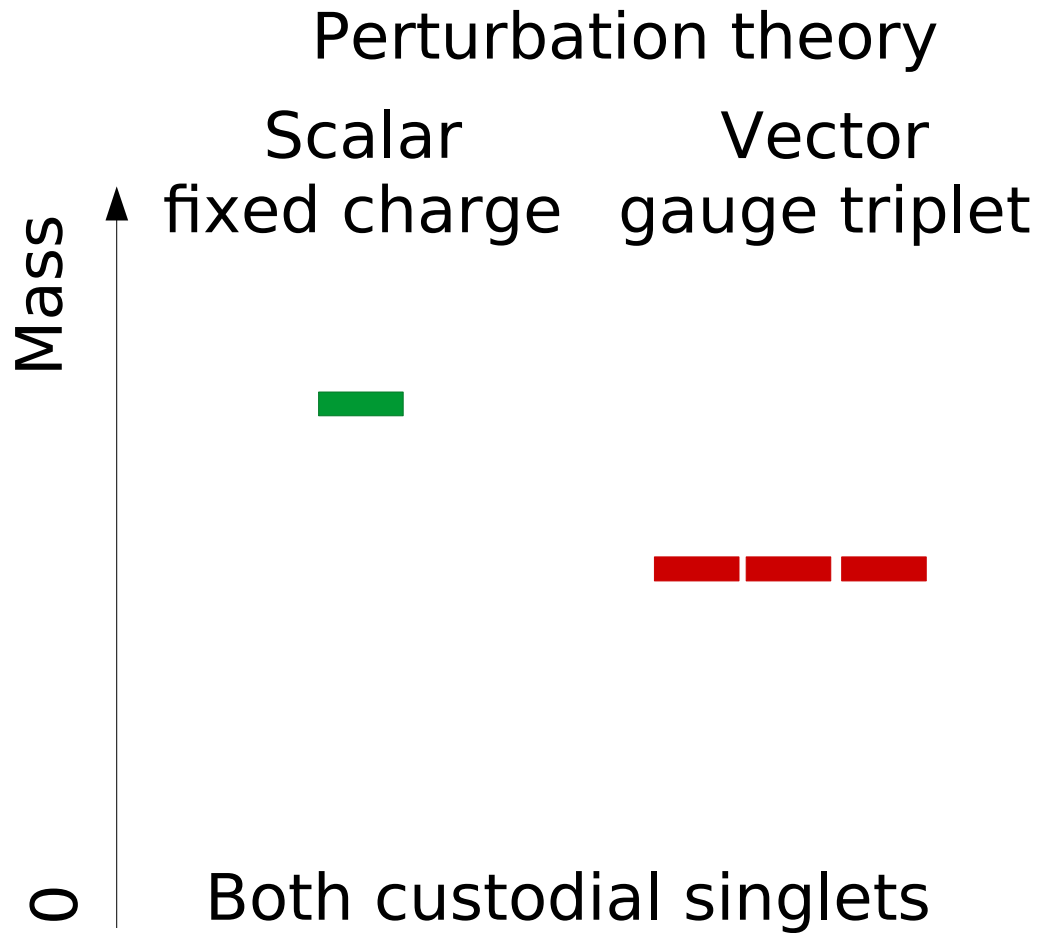
Physical spectrum



Physical spectrum



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Experiment tells that somehow the left is correct

The origin of the problem

[Fröhlich et al.'80,
Banks et al.'79]

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- Physics has to be expressed in terms of manifestly gauge-invariant quantities
 - And this includes non-perturbative aspects...
 - ...even at weak coupling [Gribov'78, Singer'78, Fujikawa'82]

Physical states

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- Need physical, gauge-invariant particles

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 - **Cannot** be the elementary particles
 - Non-Abelian nature is relevant

Physical states

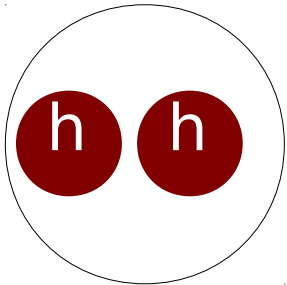
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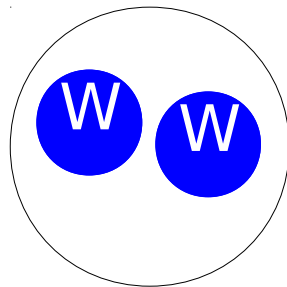
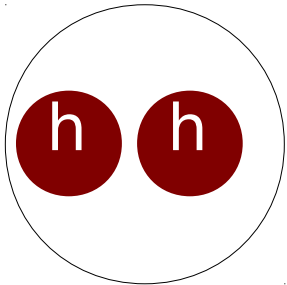
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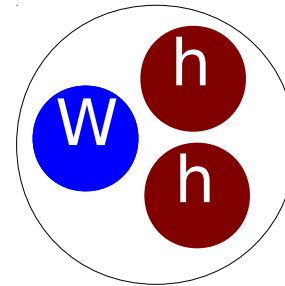
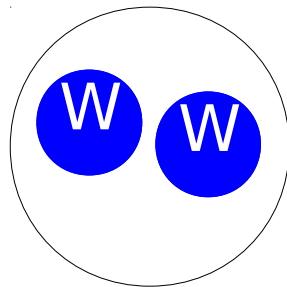
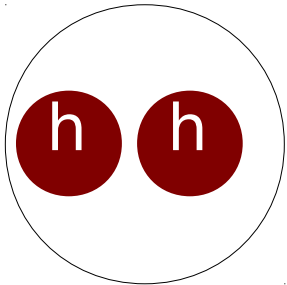
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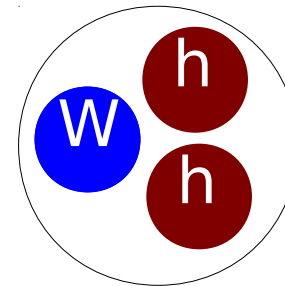
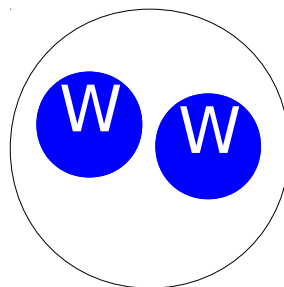
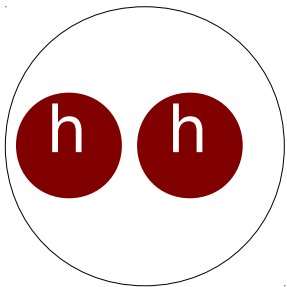
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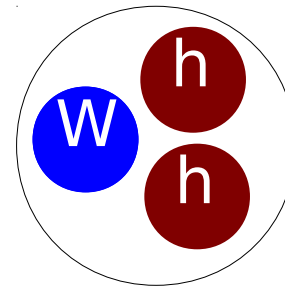
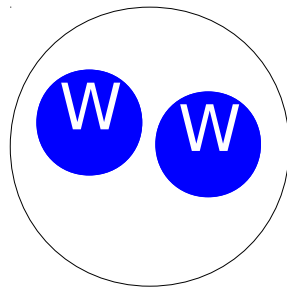
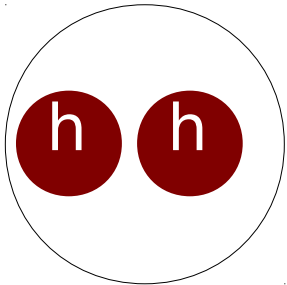


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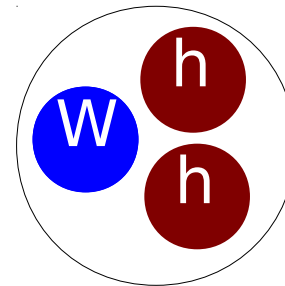
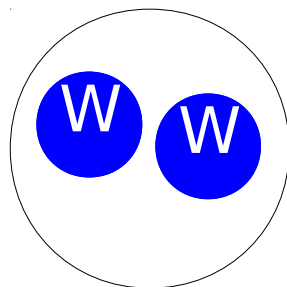
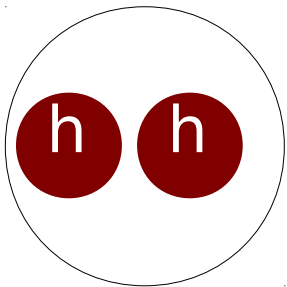


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 - Think QED (hydrogen atom!)
- Can this matter?

How to make predictions

[Fröhlich et al.'80,'81,
Maas & Törek'16,'18,
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- J^{PC} and custodial charge only quantum numbers

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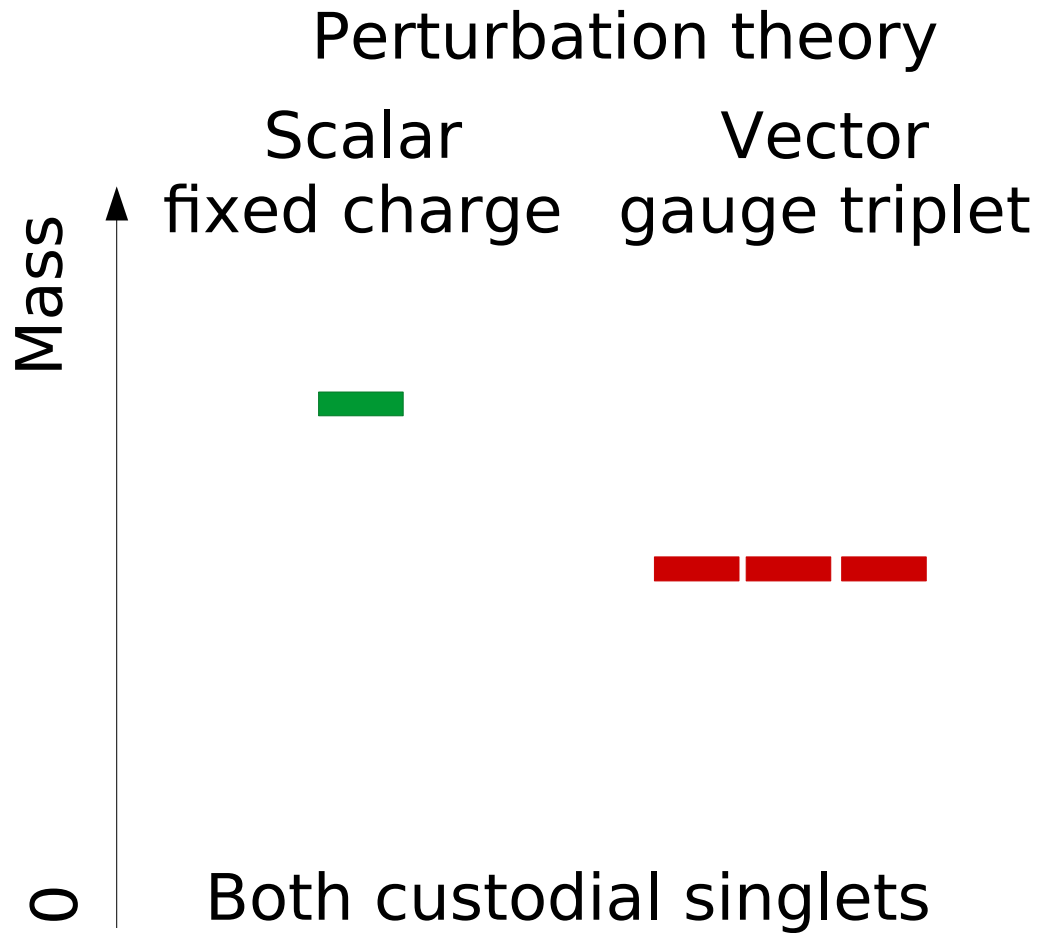
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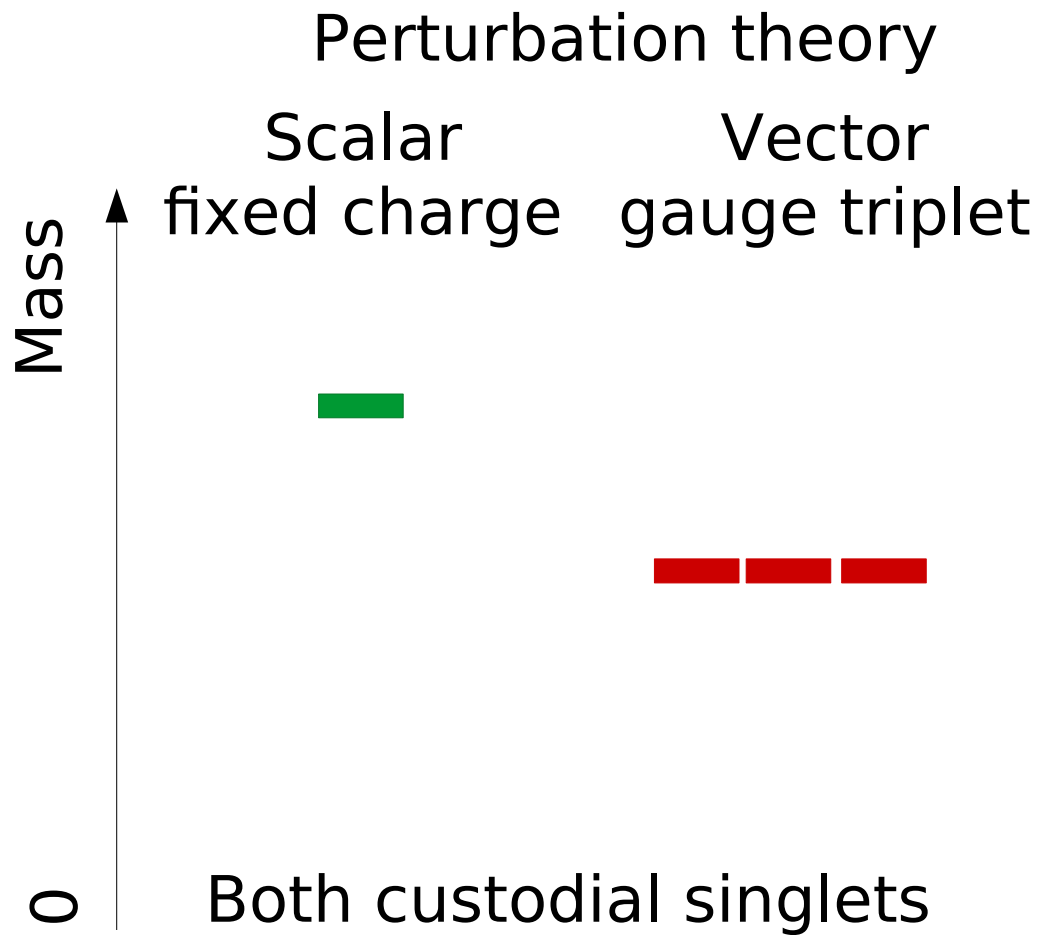
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 - Bound state structure – non-perturbative methods! - Lattice

Physical spectrum

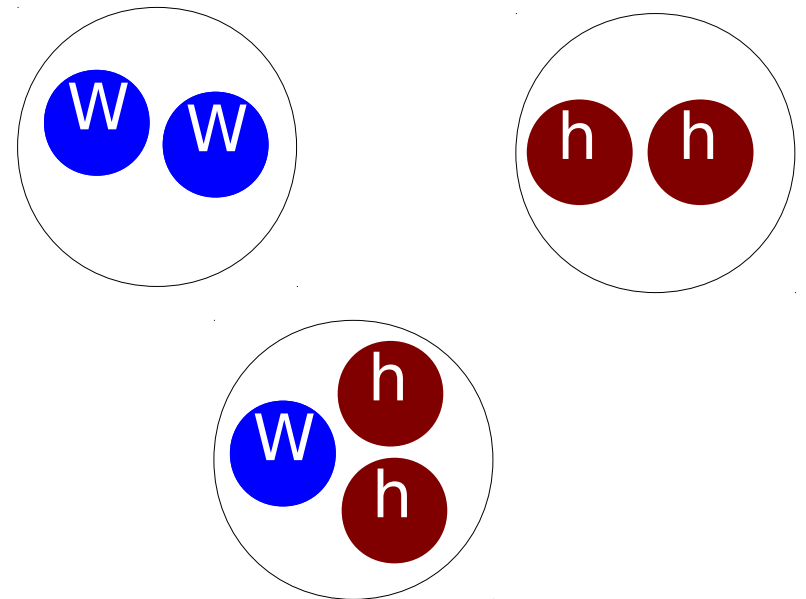


Experiment tells that somehow the left is correct

Physical spectrum

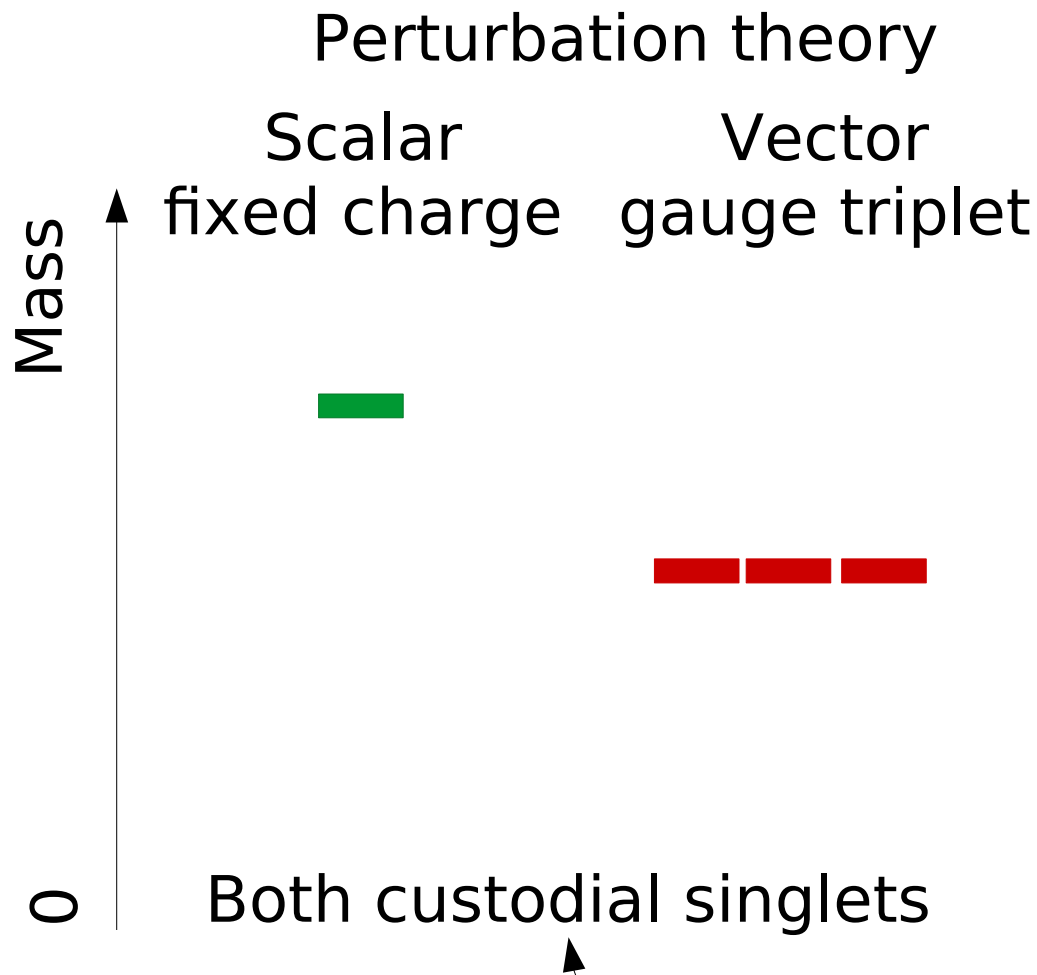


Composite (bound) states

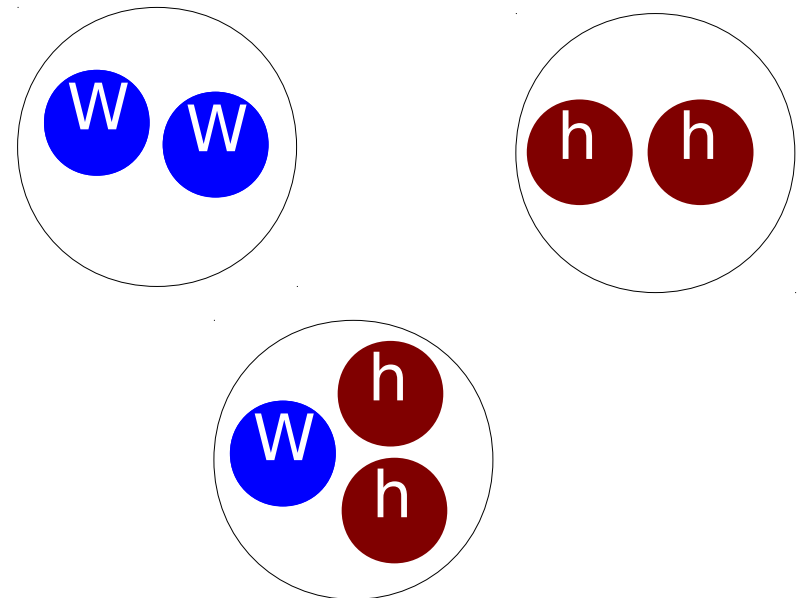


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Physical spectrum



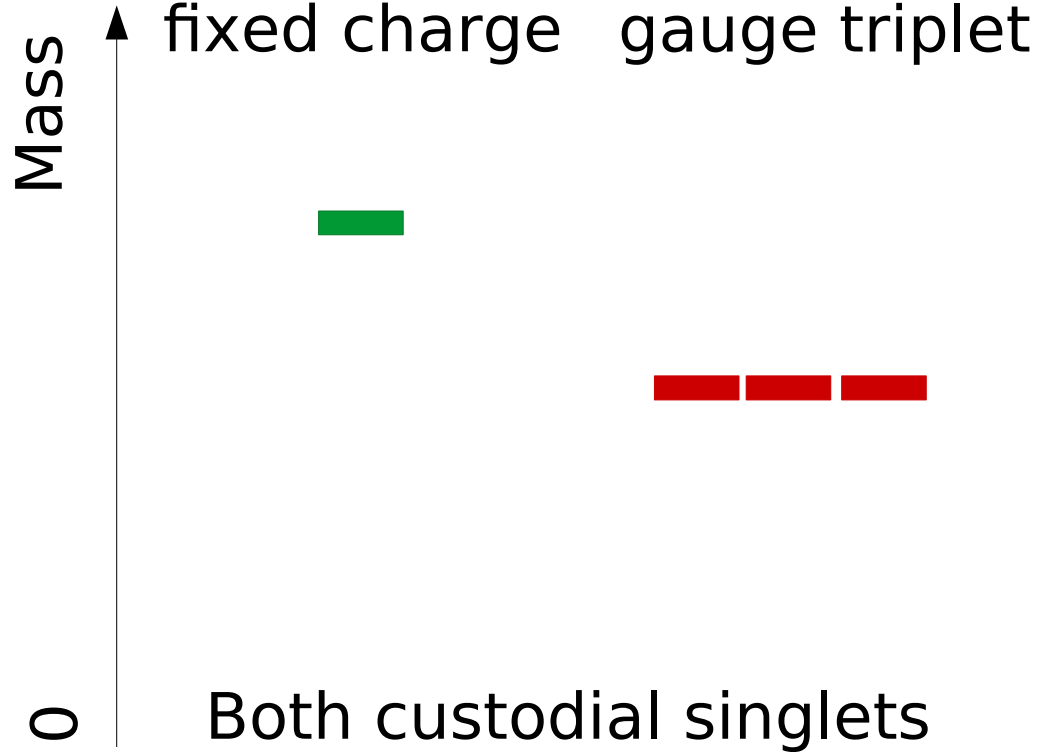
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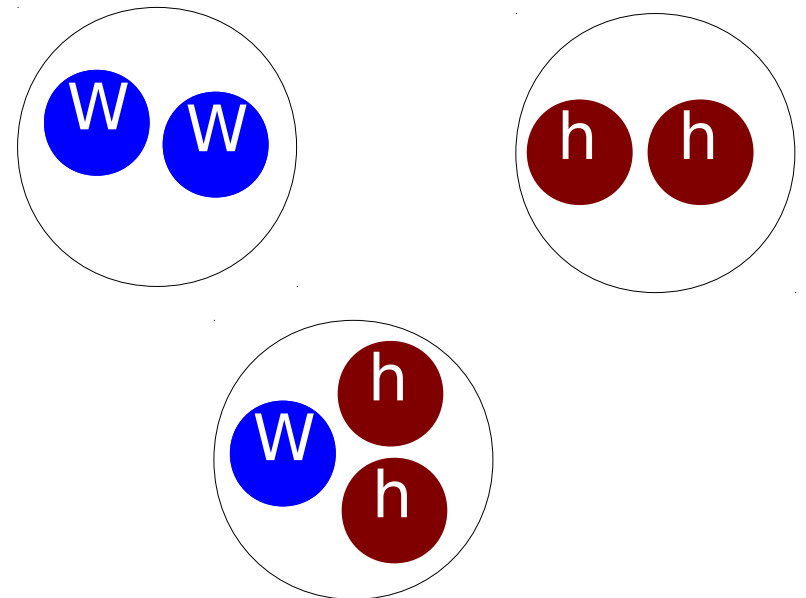
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Theory say the right is correct
There must exist a relation that both are correct

Physical spectrum

Perturbation theory
Scalar fixed charge Vector gauge triplet



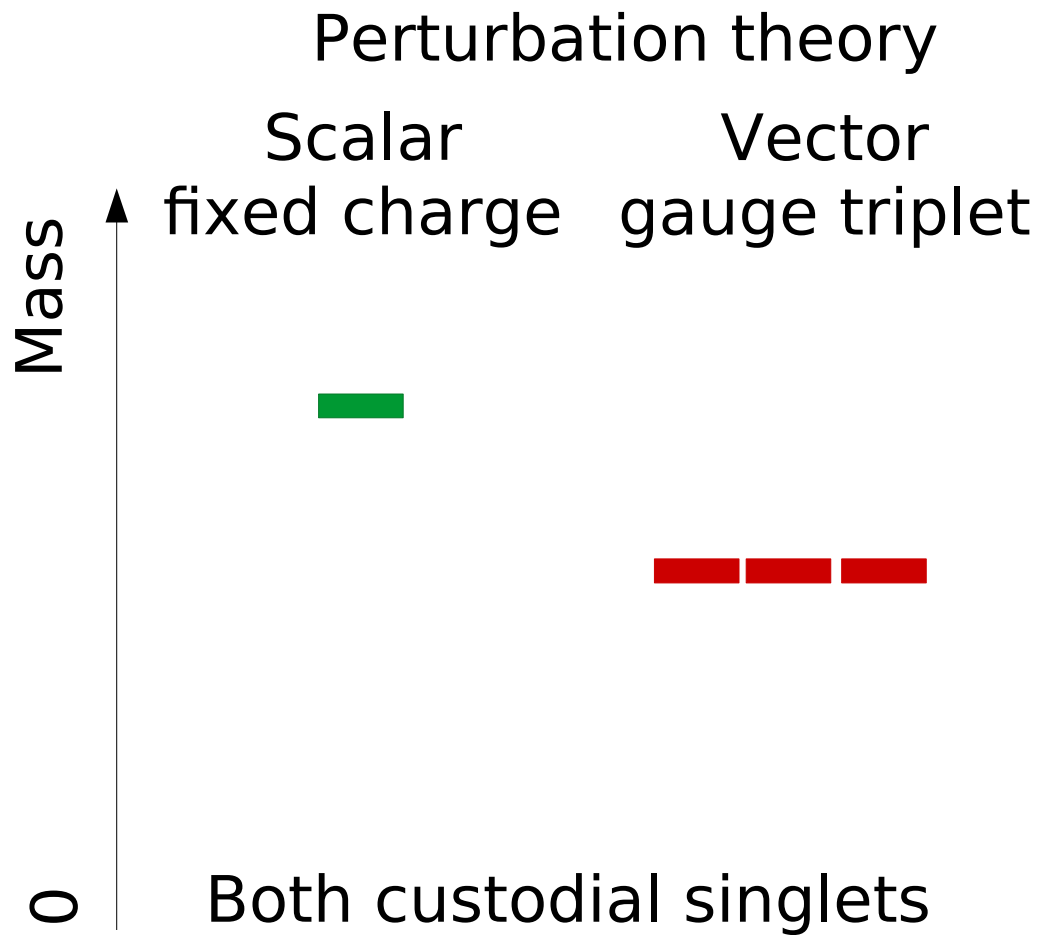
Composite (bound) states
Require non-perturbative methods



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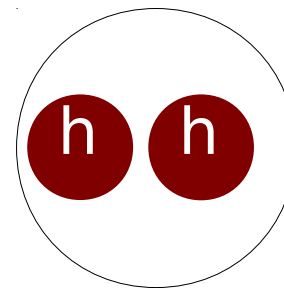
[Maas'12, Maas & Mufti'14]



Gauge-invariant

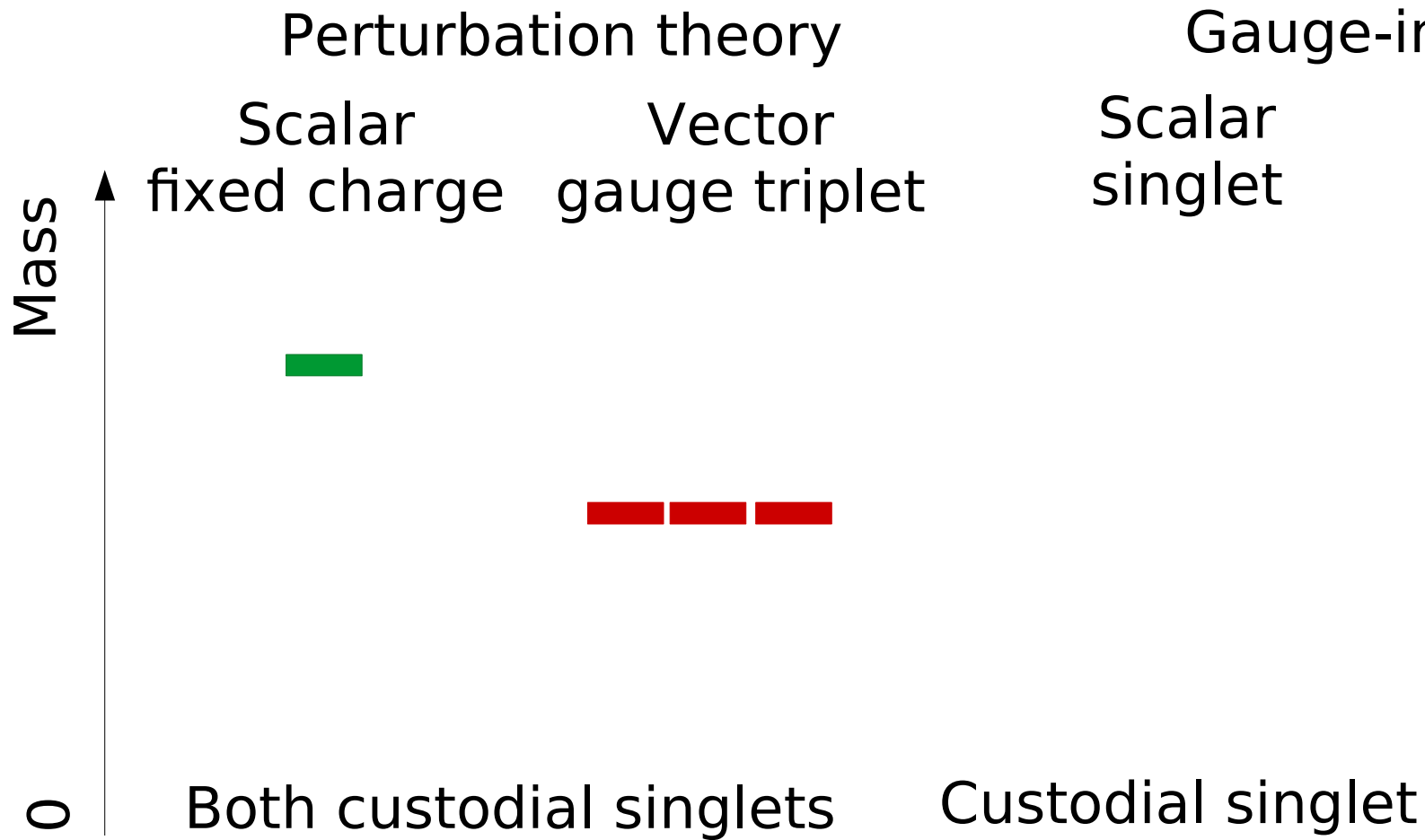
Scalar singlet

$$h(x)^+ h(x)$$

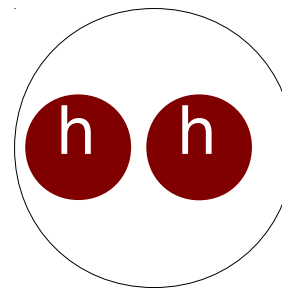


Physical spectrum

[Maas'12, Maas & Mufti'14]

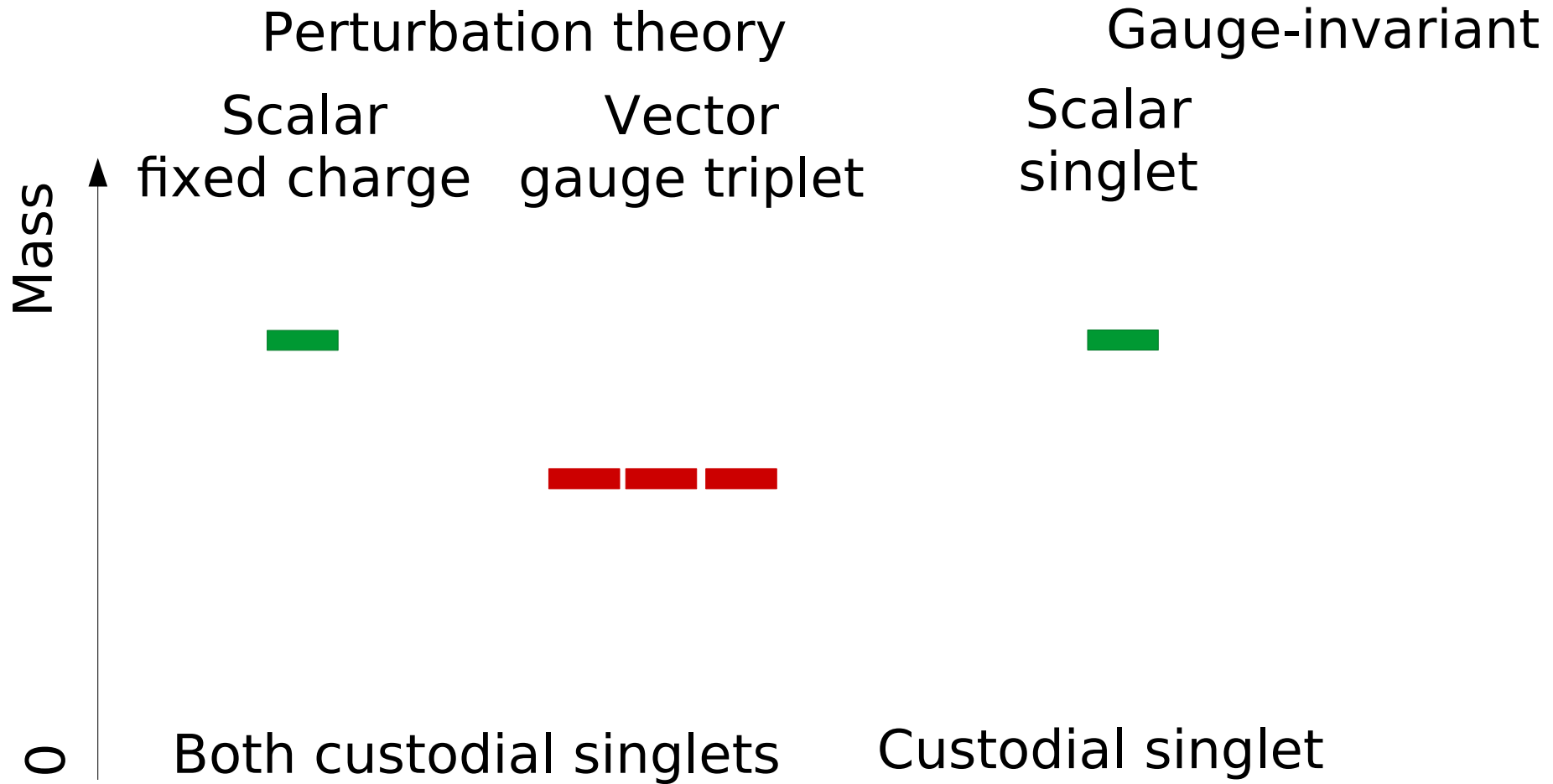


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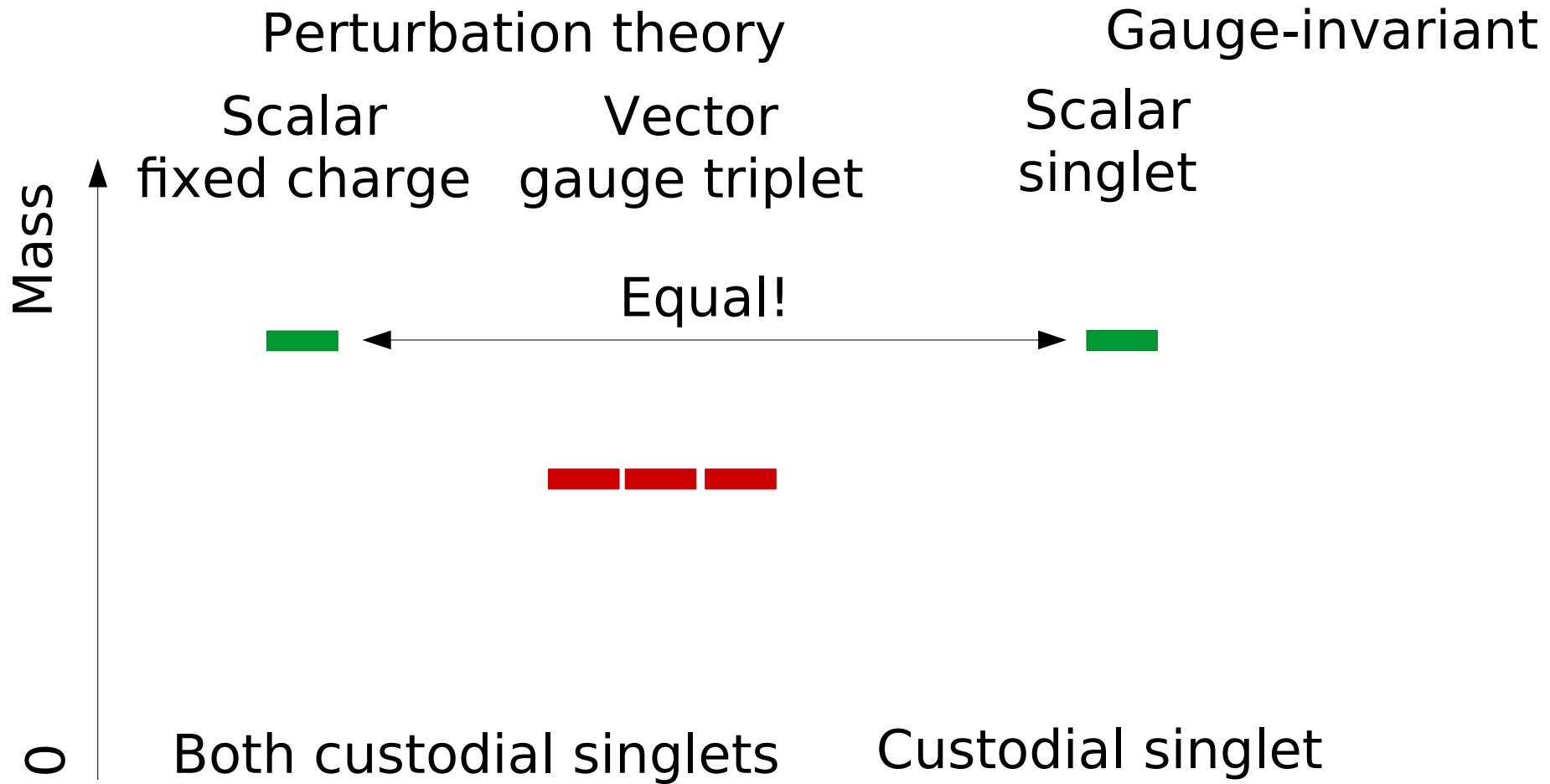
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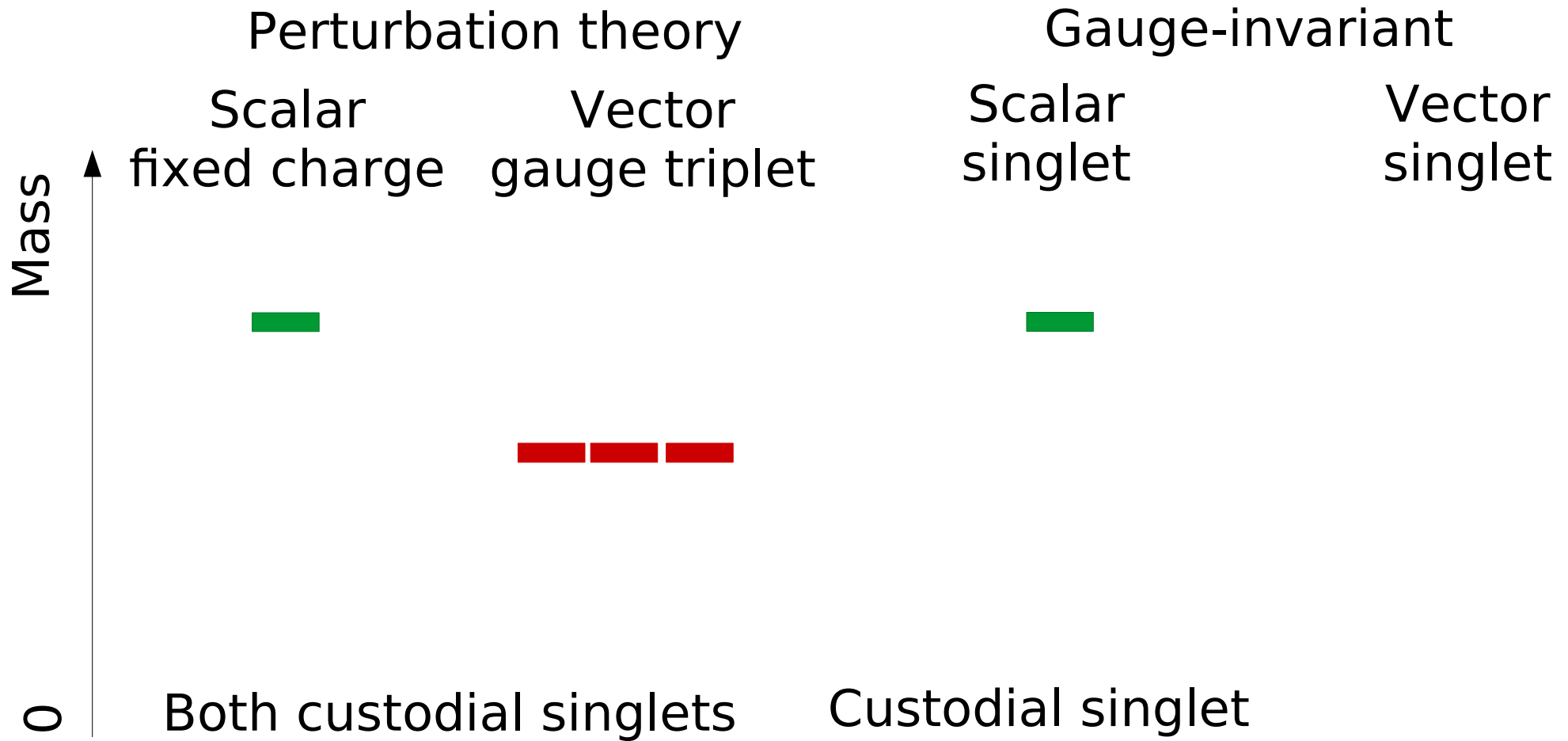
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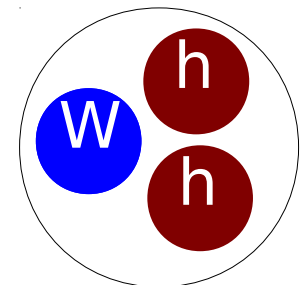
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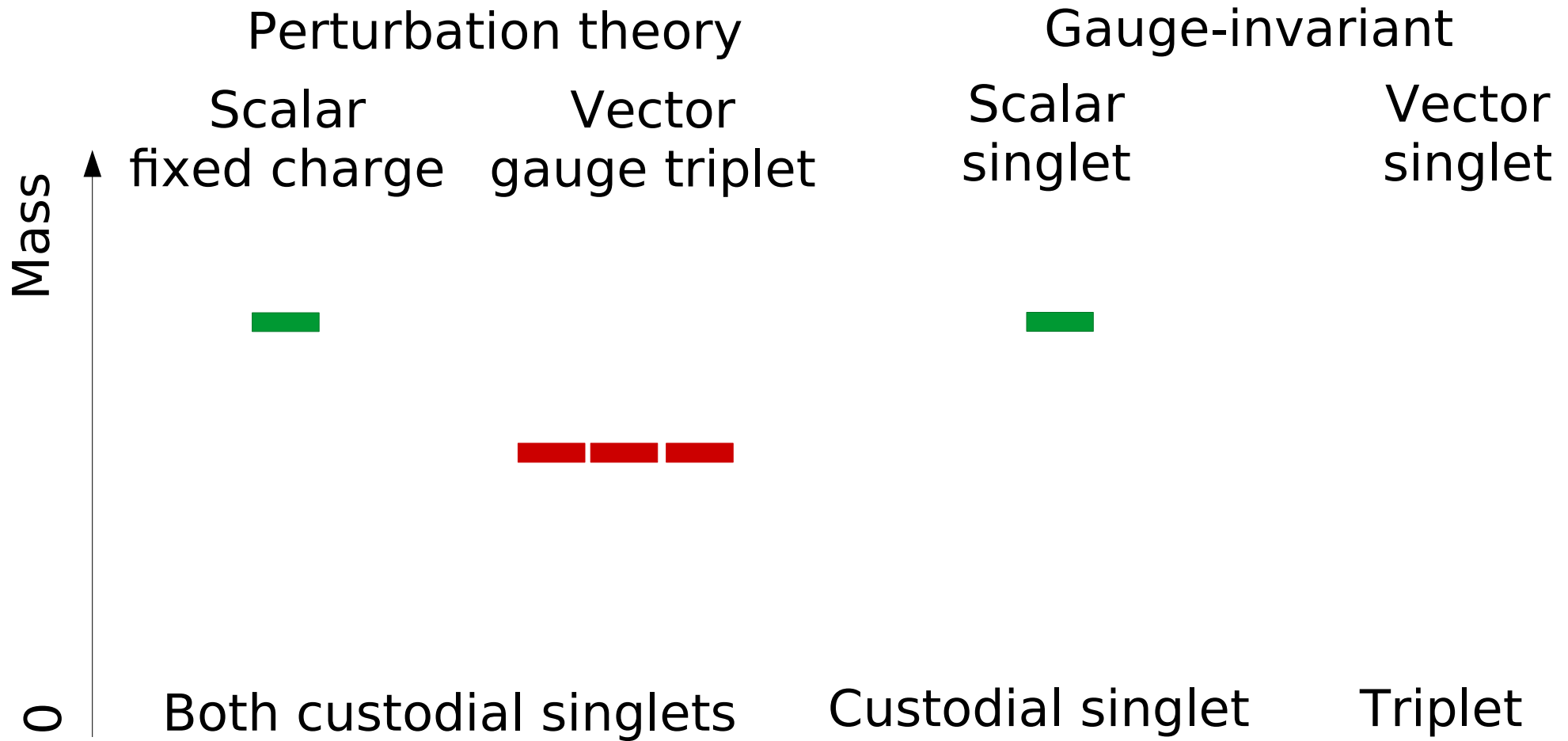


$$\text{tr } t^a \frac{h^+}{\sqrt{h^+ h}} D_\mu \frac{h}{\sqrt{h^+ h}}$$

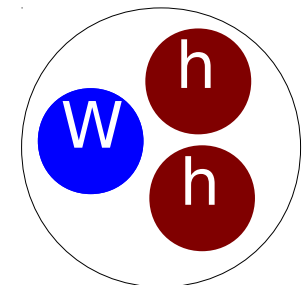


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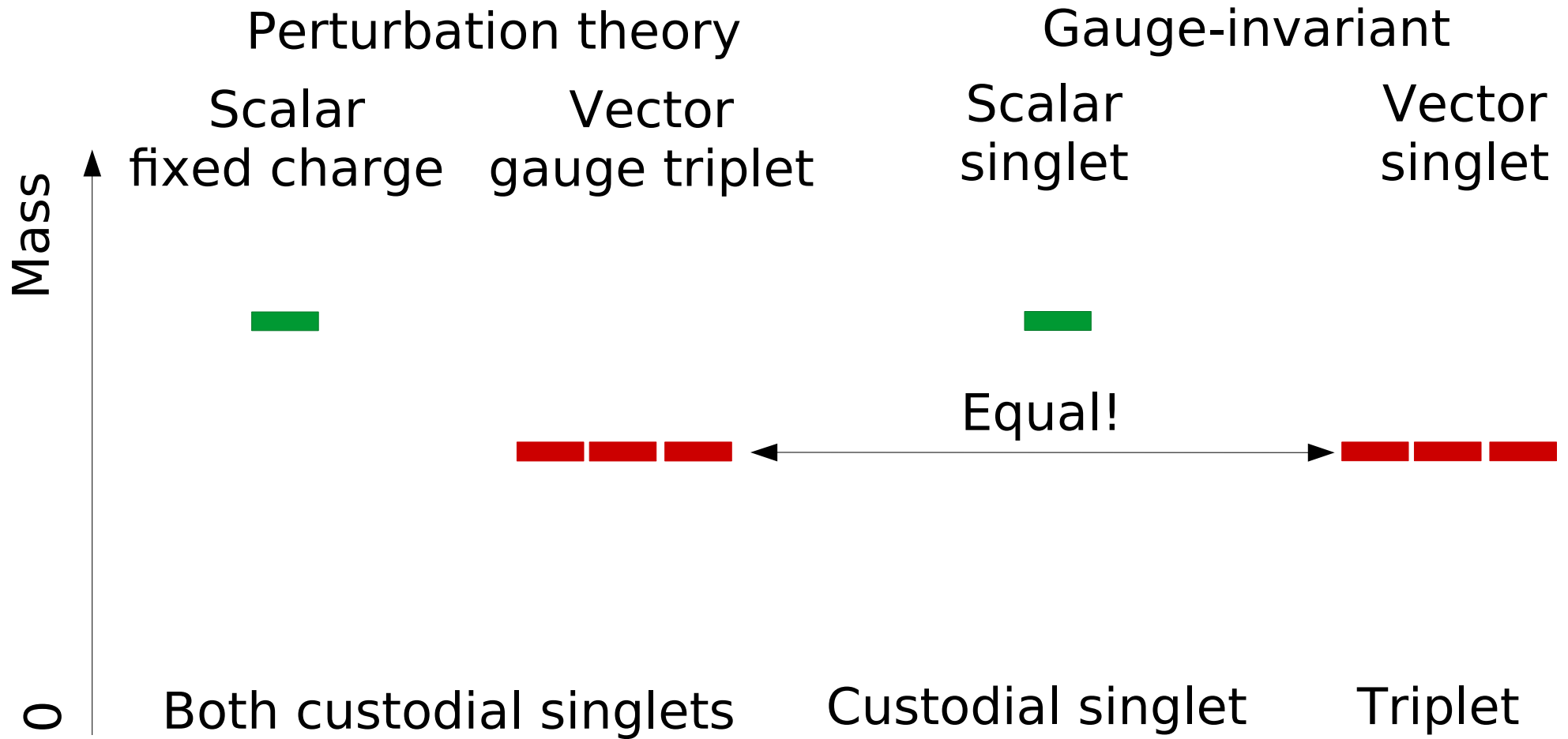


$$tr t^a \frac{h^+}{\sqrt{h^+ h}} D_u \frac{h}{\sqrt{h^+ h}}$$



Physical spectrum

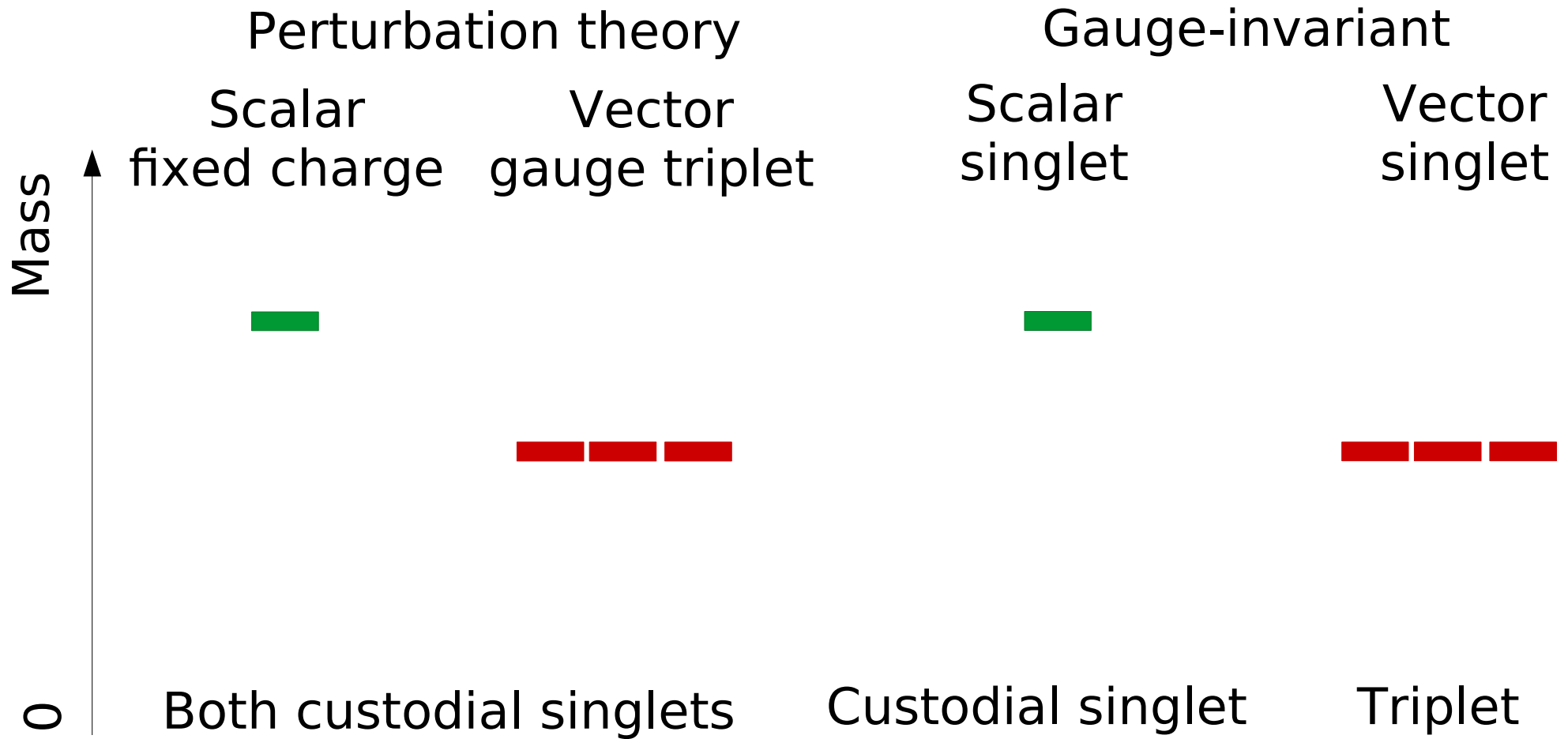
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- Confirmed on the lattice

Physical spectrum

[Maas'12, Maas & Mufti'14]



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- Some lattice support for $SU(2) \times U(1)$ [Shrock et al. 85-88]

A microscopic mechanism

-

Why on-shell is important

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 - But coupling is still weak and there is a BEH

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[Fröhlich et al.'80,'81,
Maas & Törek'16,'18,
Maas, Sondenheimer & Törek'17]

- J^{PC} and custodial charge only quantum numbers
 - Different from perturbation theory
 - Operators limited to asymptotic, elementary, gauge-dependent states
- Formulate gauge-invariant, composite operators
 - Bound state structure – non-perturbative methods?
 - But coupling is still weak and there is a BEH
 - Perform double expansion [Fröhlich et al.'80, Maas'12]
 - Vacuum expectation value (FMS mechanism)
 - Standard expansion in couplings
 - Together: Gauge-invariant perturbation theory

Gauge-invariant perturbation theory

[Fröhlich et al.'80,'81
Maas'12,'17]

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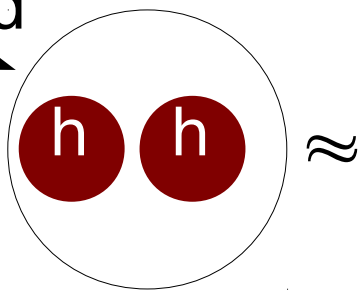
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\approx



+



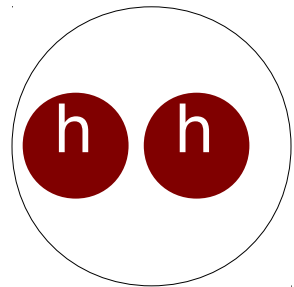
+ something small

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Gauge-invariant perturbation theory

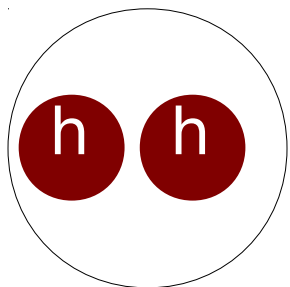
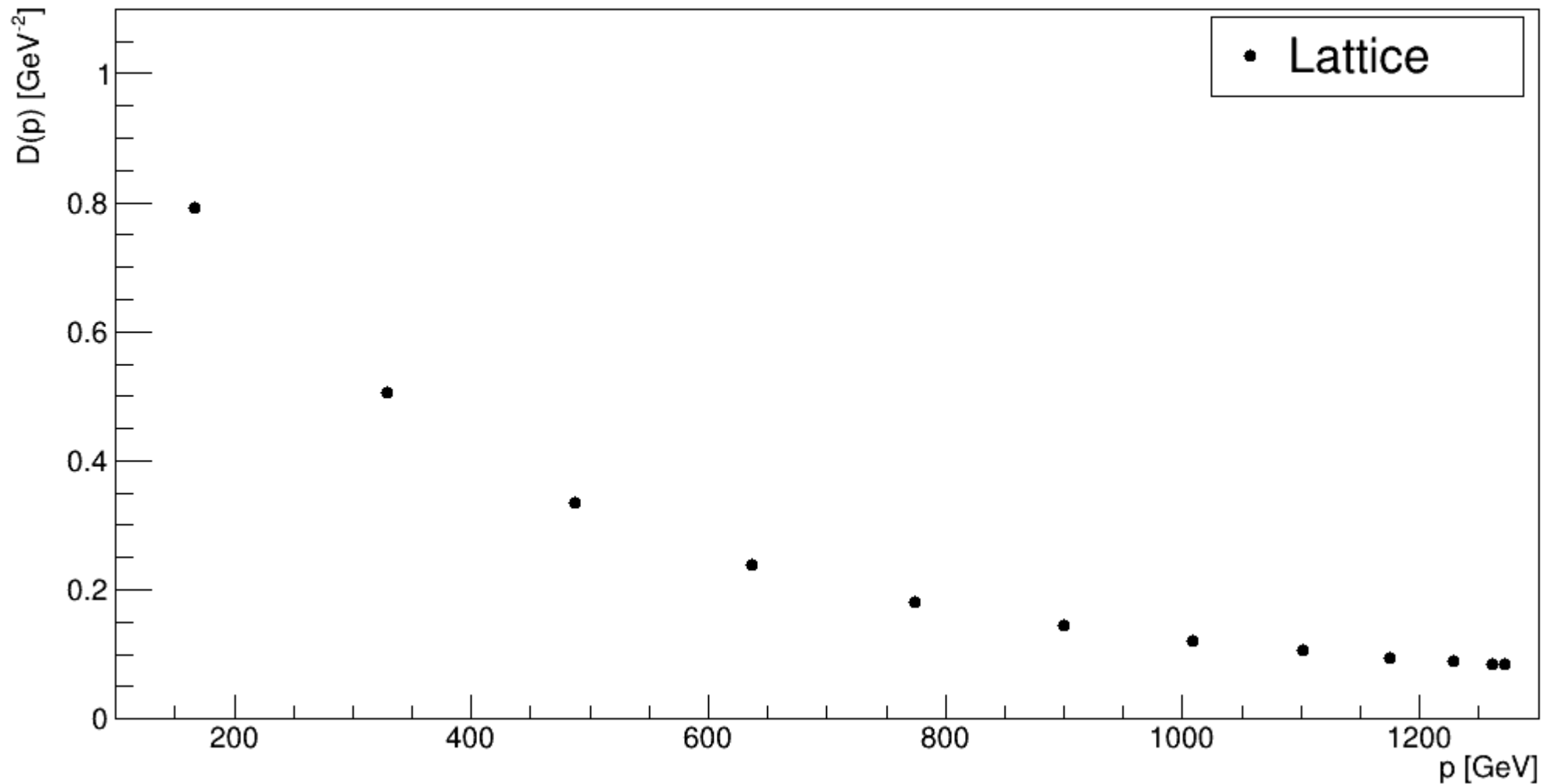


A Feynman diagram consisting of a large circle containing two smaller dark red circles, each with a white letter 'h' inside. This diagram is equated to the mathematical expression $D(P^2)$.

$$\text{Bubble}(h, h) = D(P^2)$$

Gauge-invariant perturbation theory

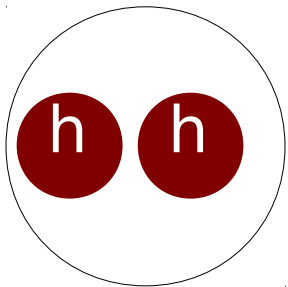
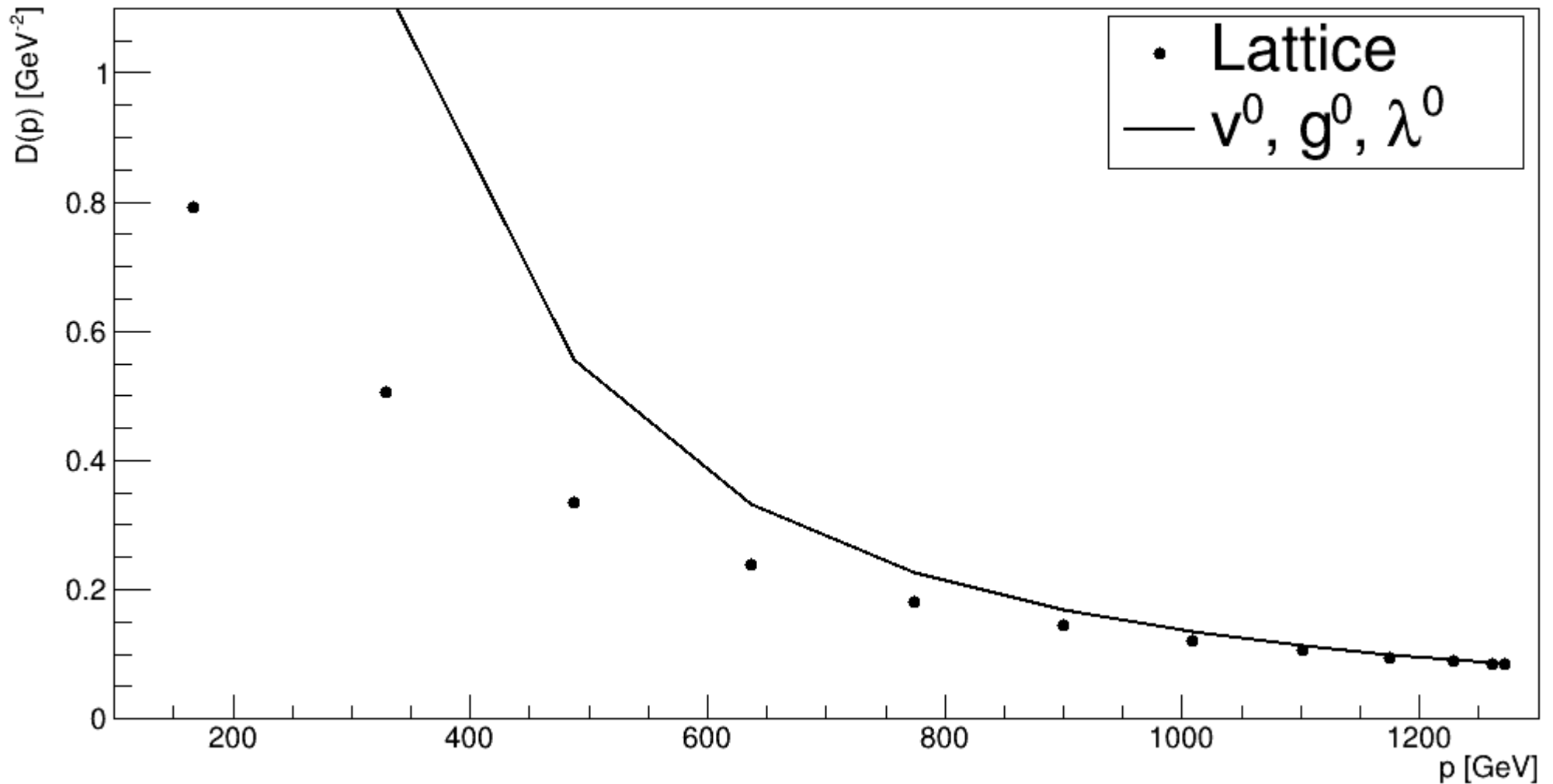
Scalar propagator



$$D(P) = \langle (h^+ h)(x) (h^+ h)(y) \rangle$$

Gauge-invariant perturbation theory

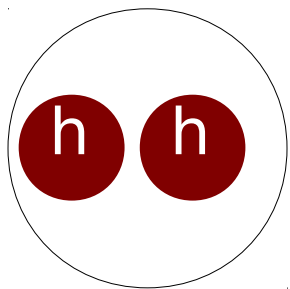
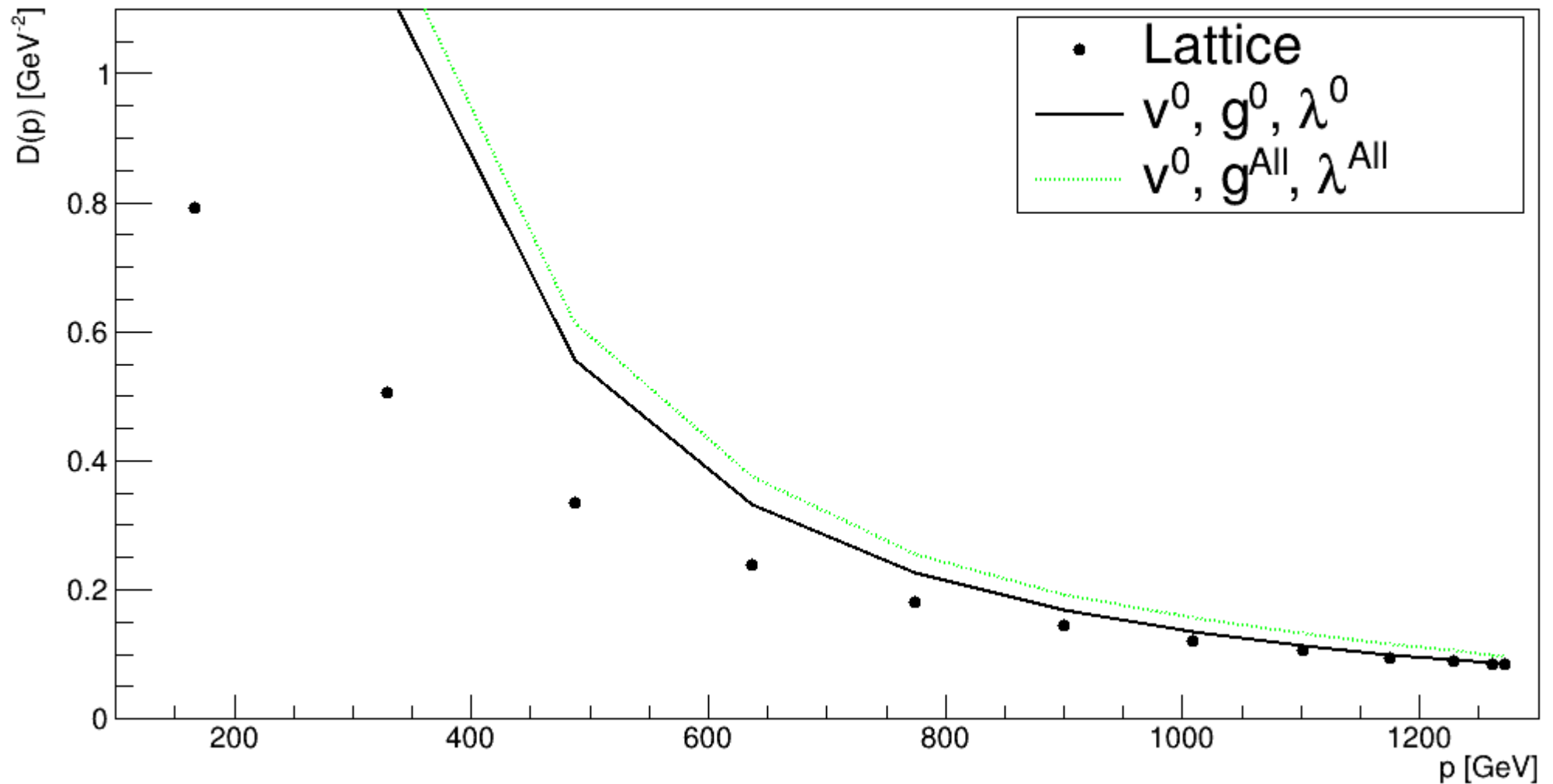
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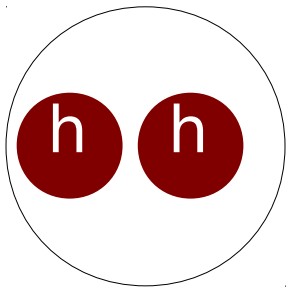
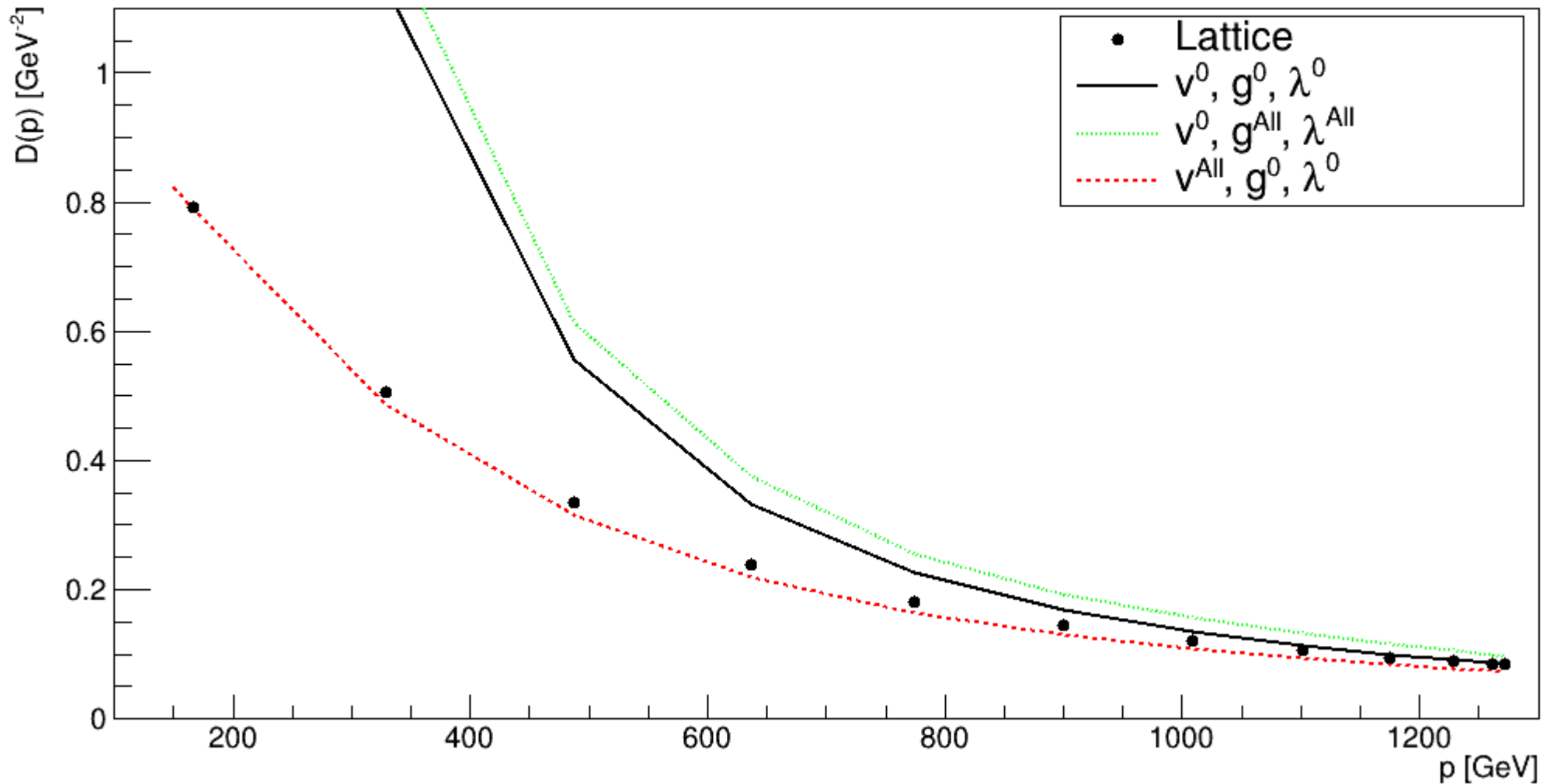
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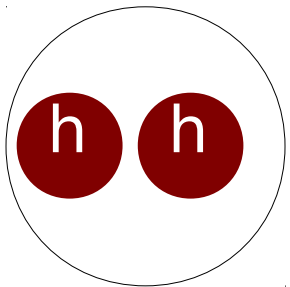
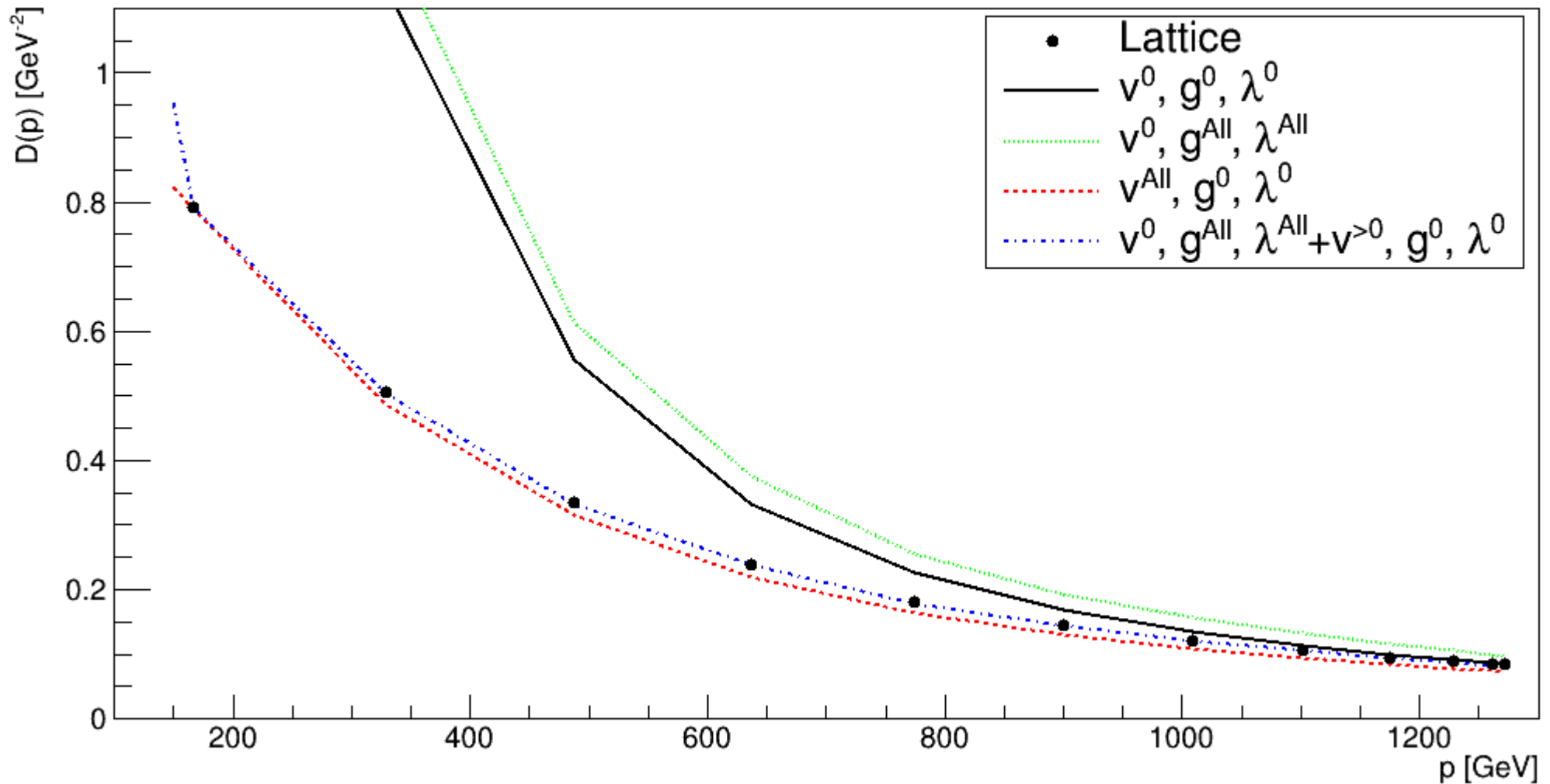
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Gauge-invariant perturbation theory

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What about the vector?

[Fröhlich et al.'80,'81
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Matrix from
group structure



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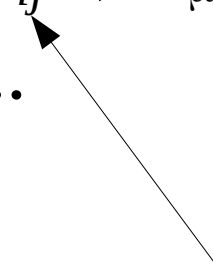
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c projects custodial
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c projects custodial states to gauge states

Exactly one gauge boson for every physical state

Matrix from group structure

Exploring implications

-

Experimental tests

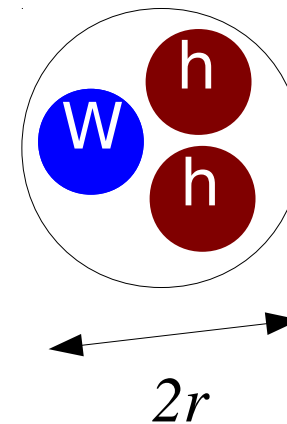
Bound states as extended objects

- Bound states have an extension
 - Can it be measured?

Bound states as extended objects

[Maas,Raubitzke,Törek'18]

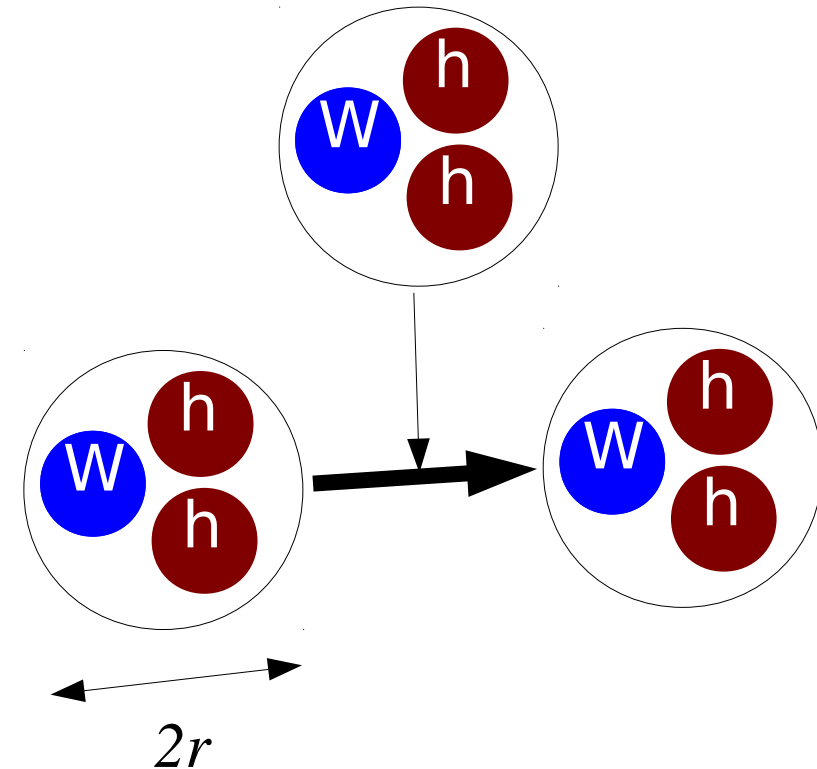
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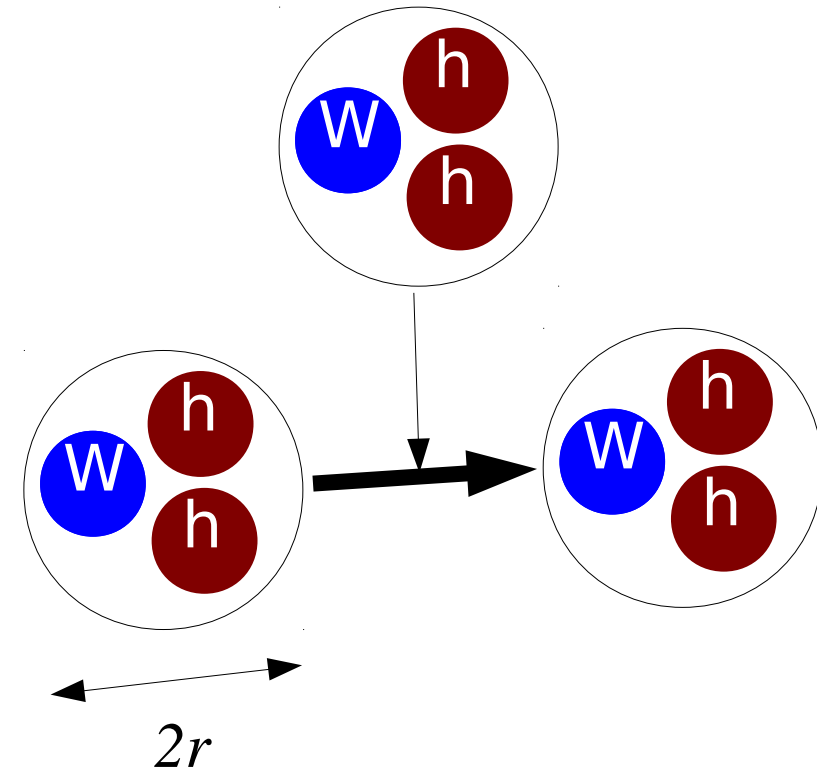
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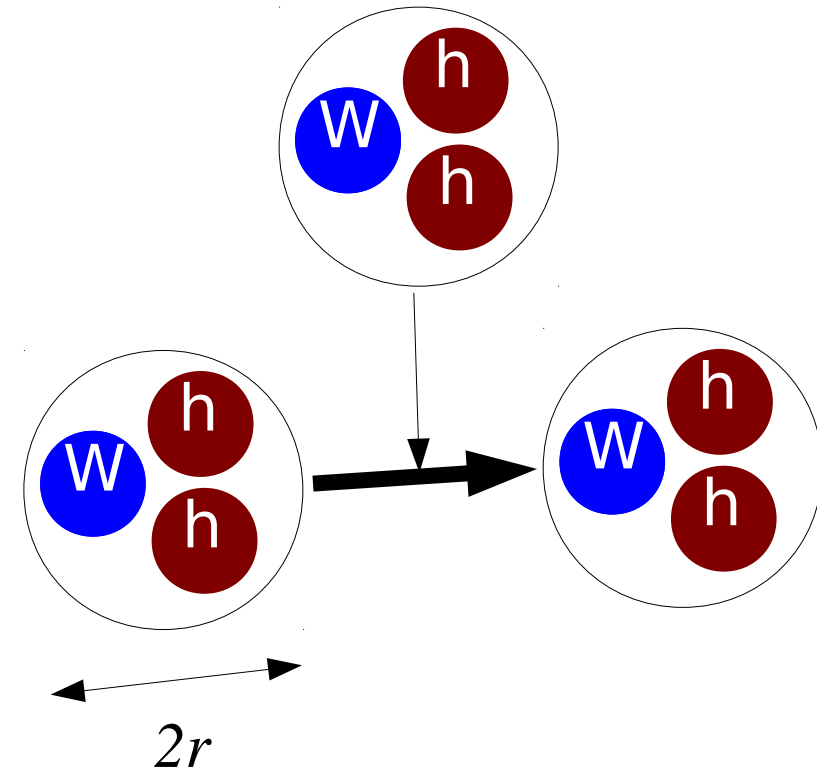


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$$F(q^2, q^2, q^2) = 1 - \frac{q^2 \langle r^2 \rangle}{6} + \dots$$



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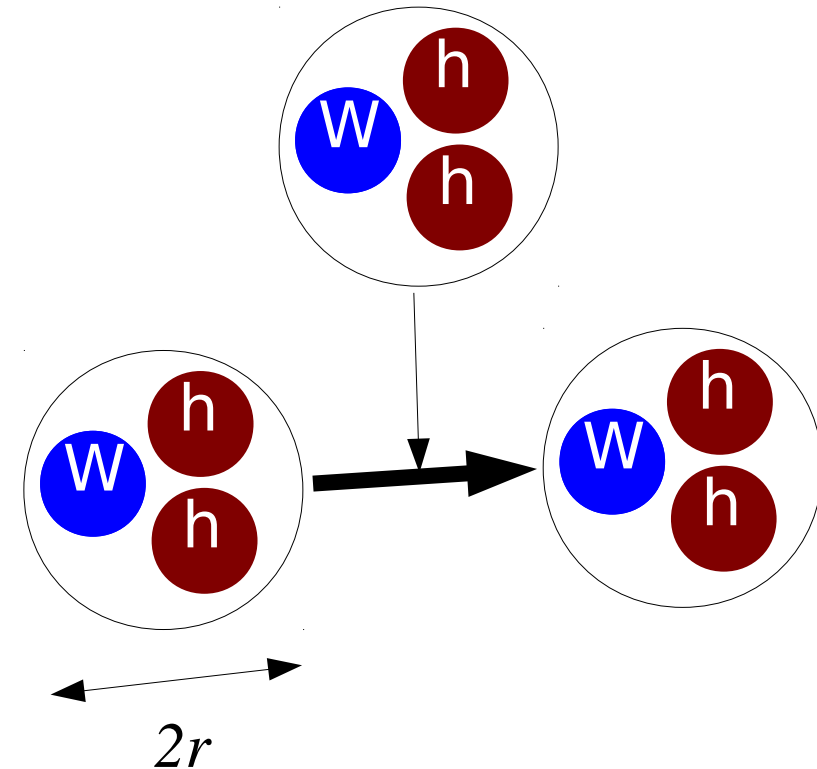
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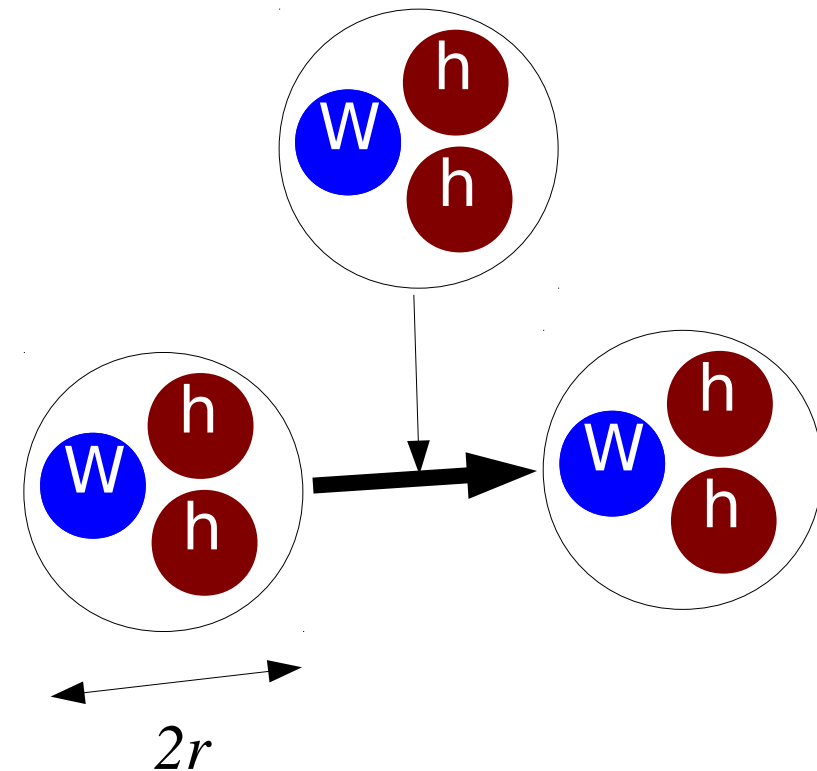
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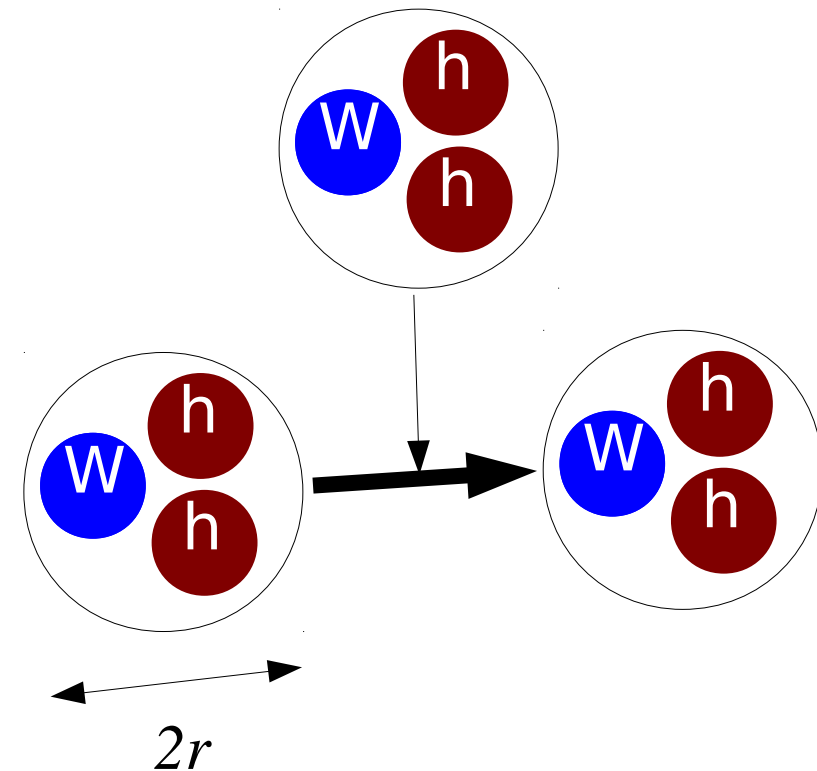
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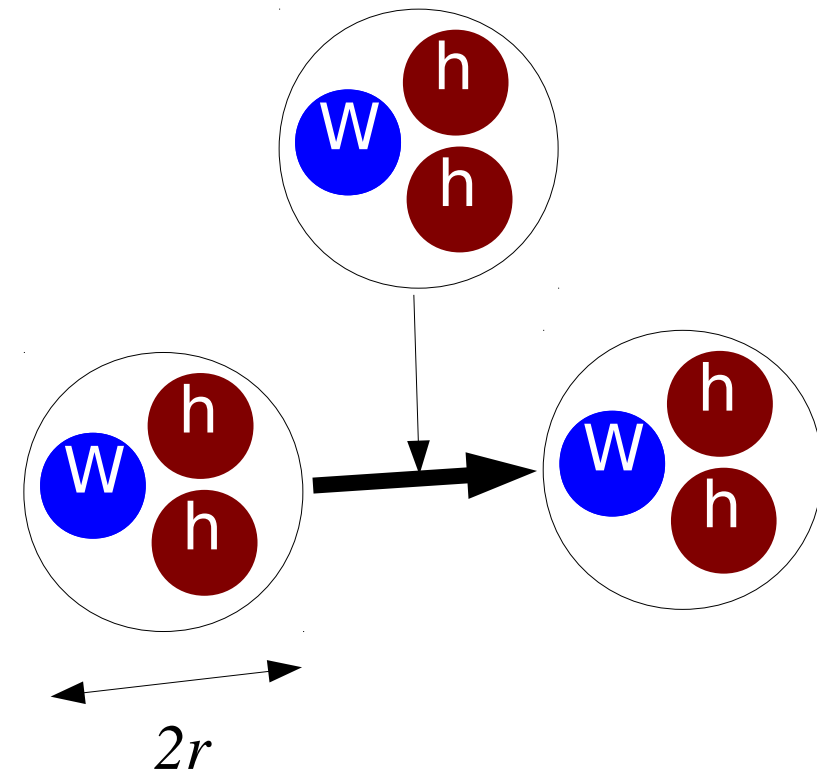
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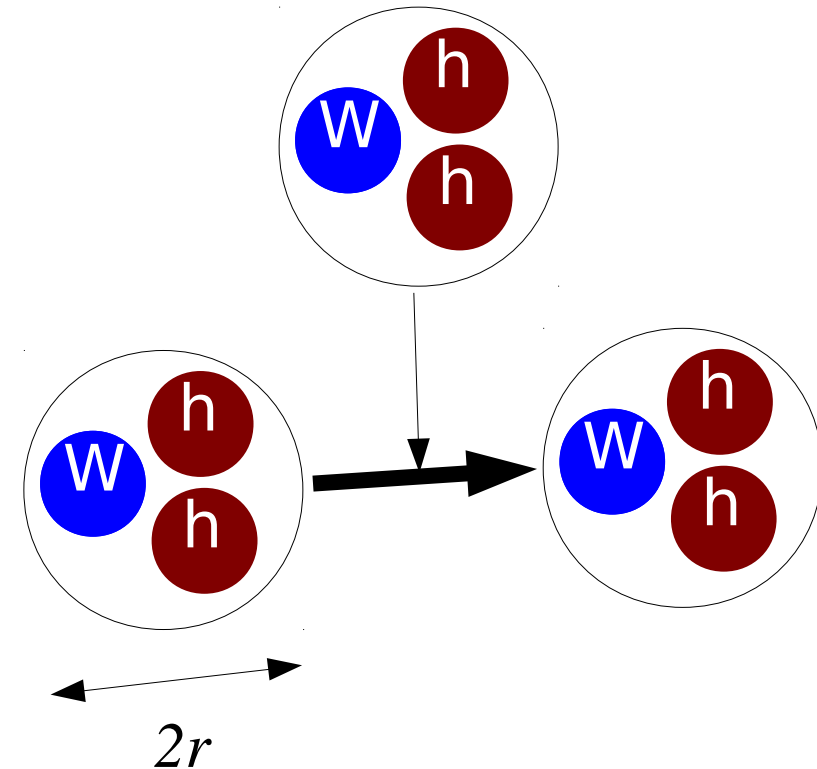
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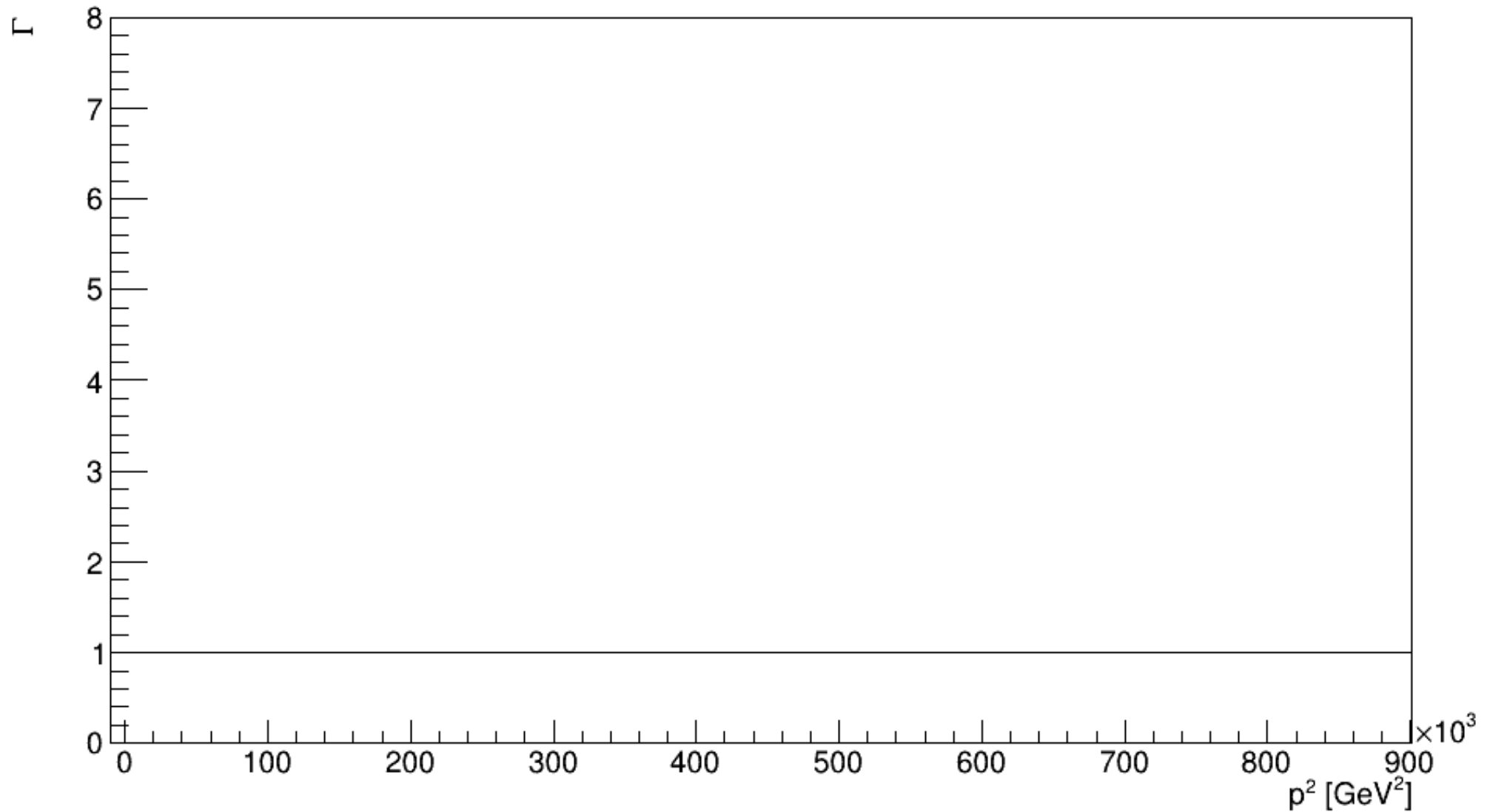


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 - Experimentally hard, but possible

Bound states as extended objects

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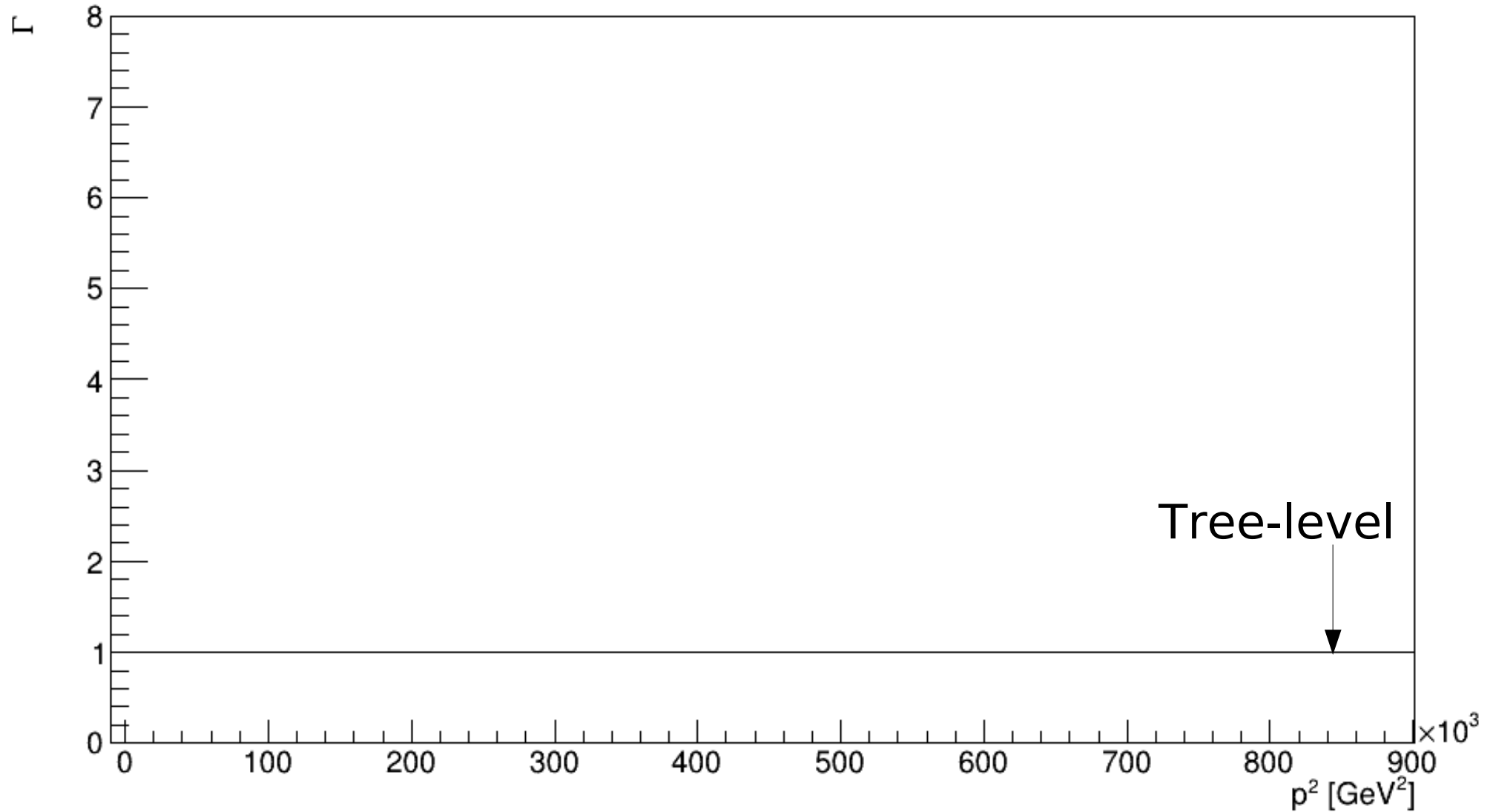
Vector form factor



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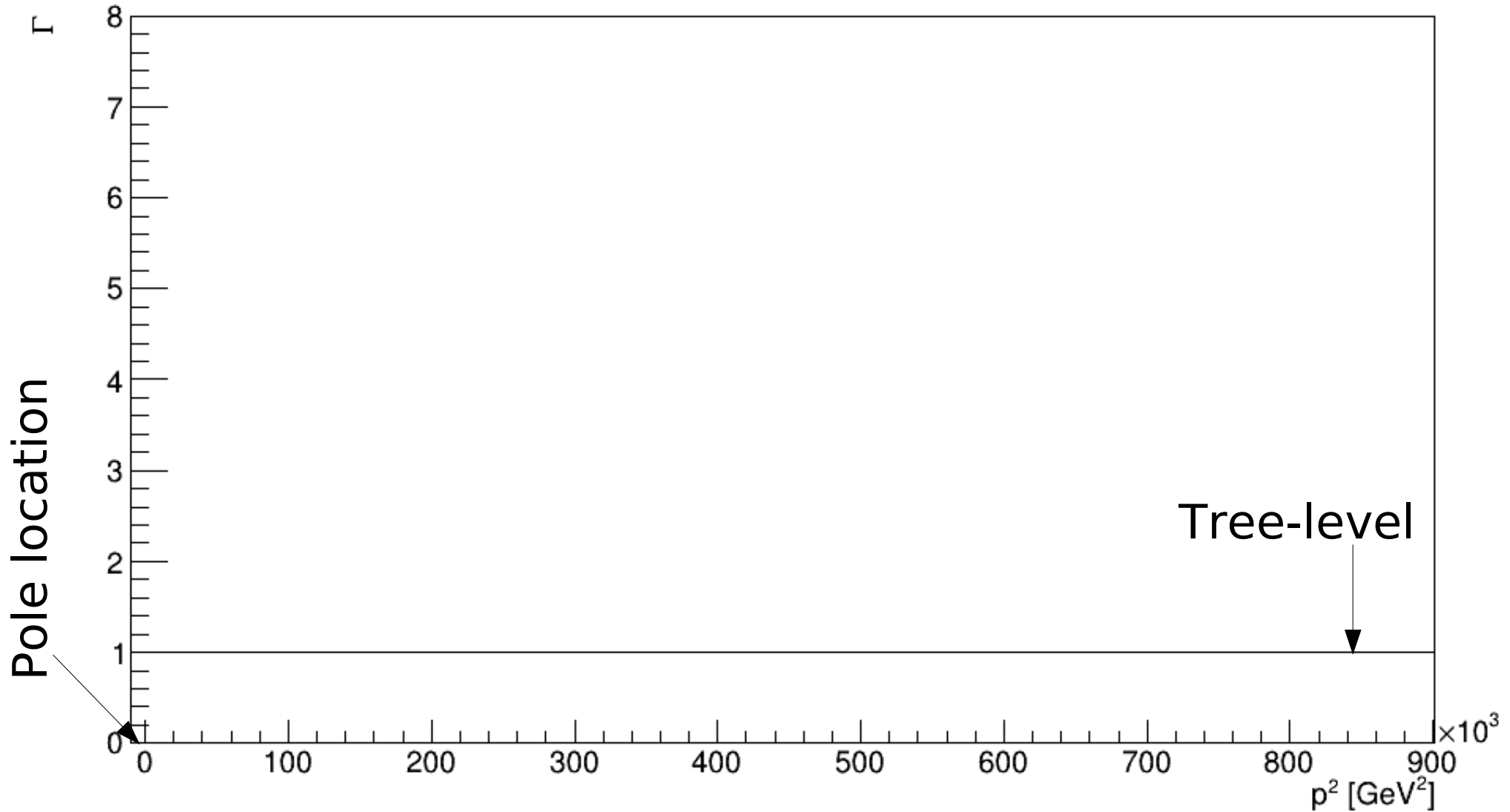
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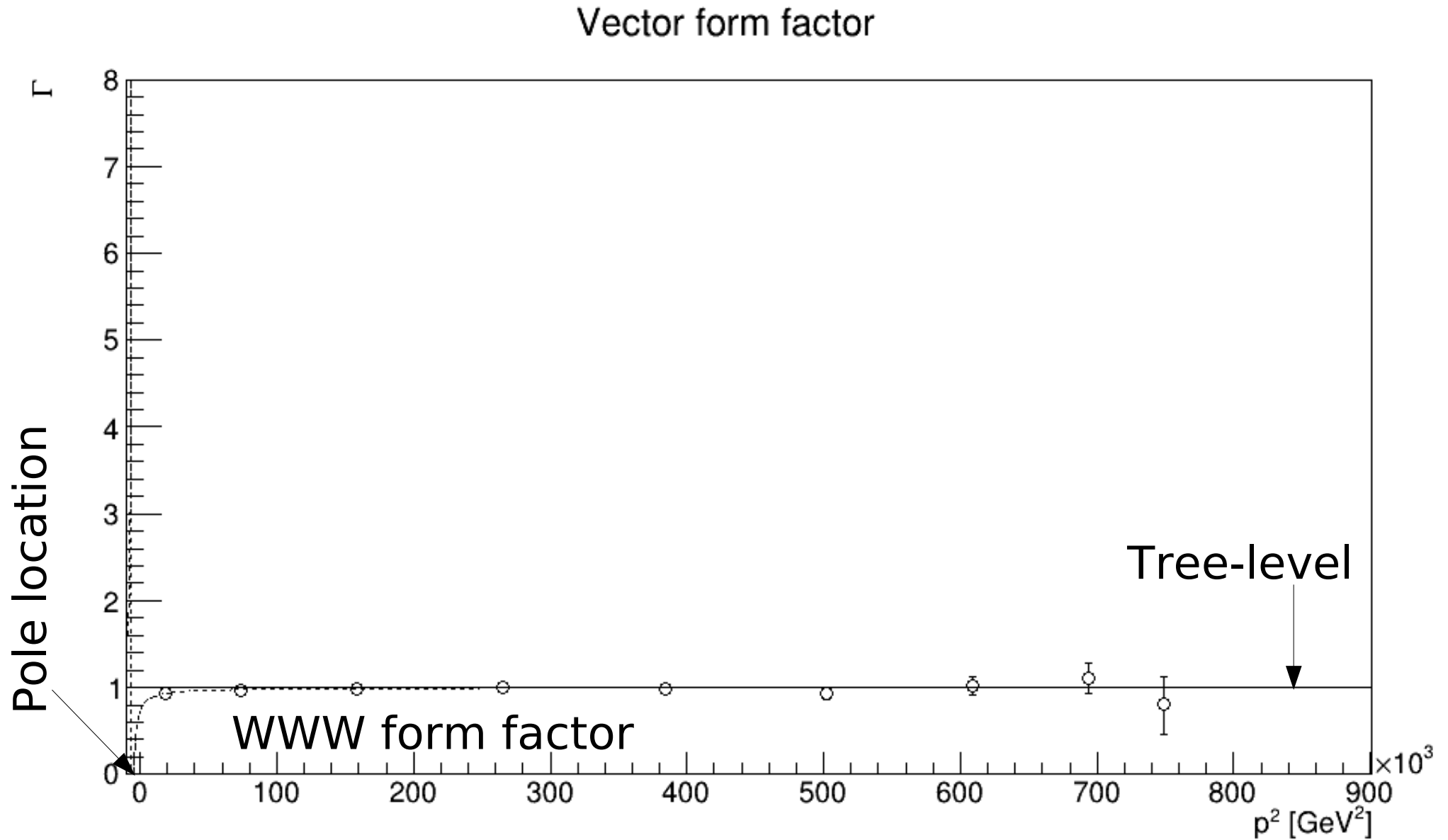
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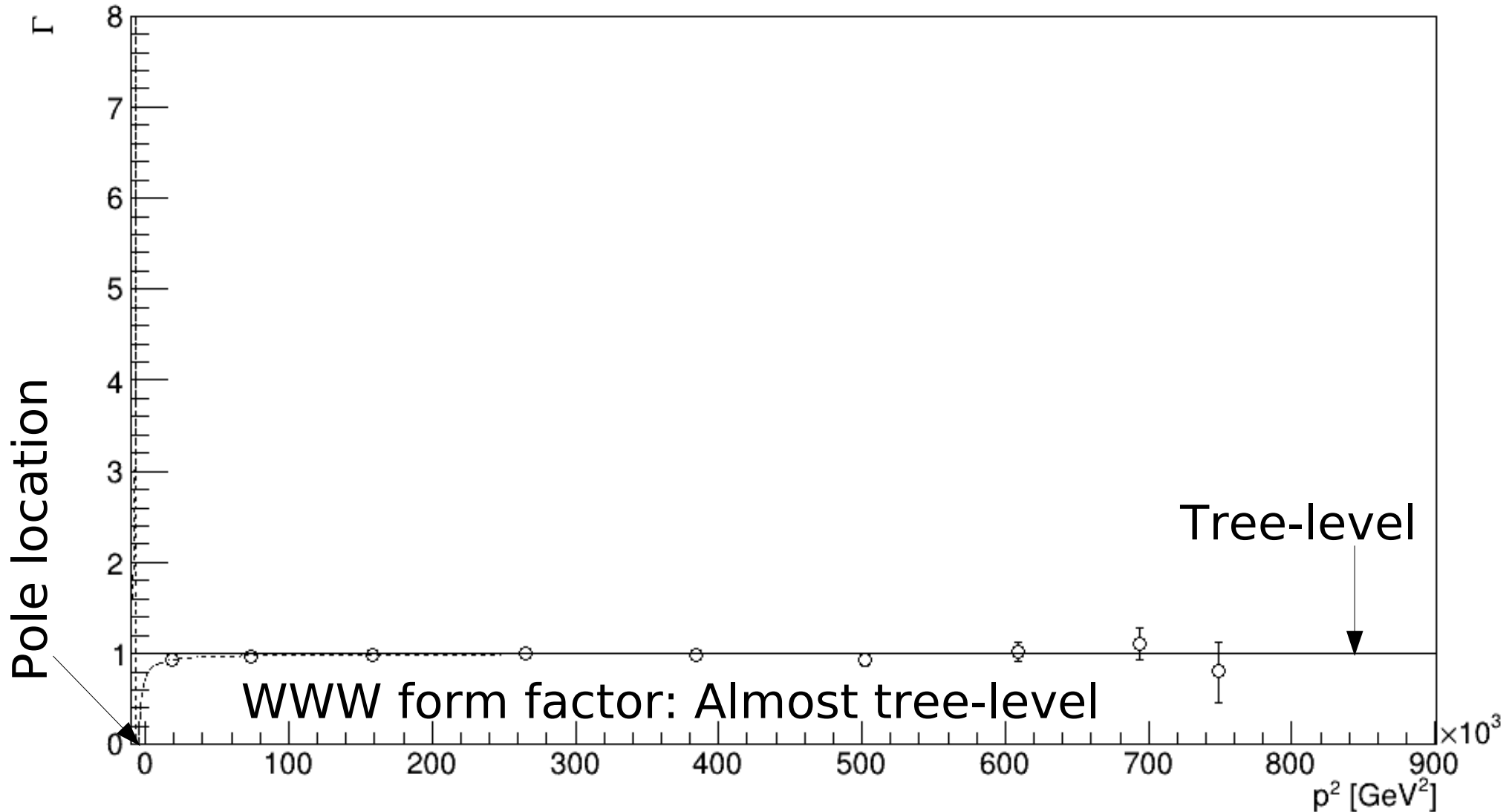
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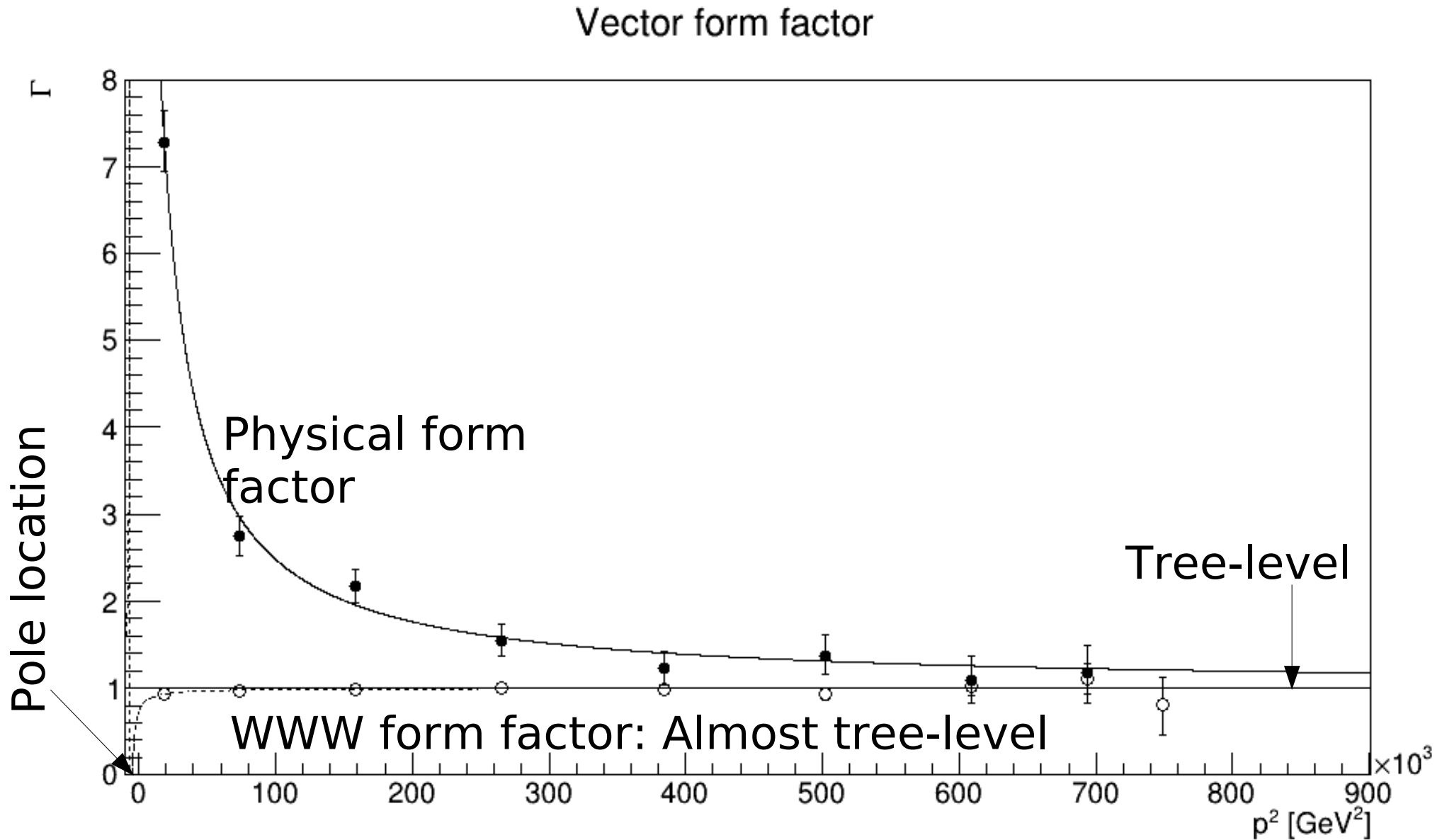
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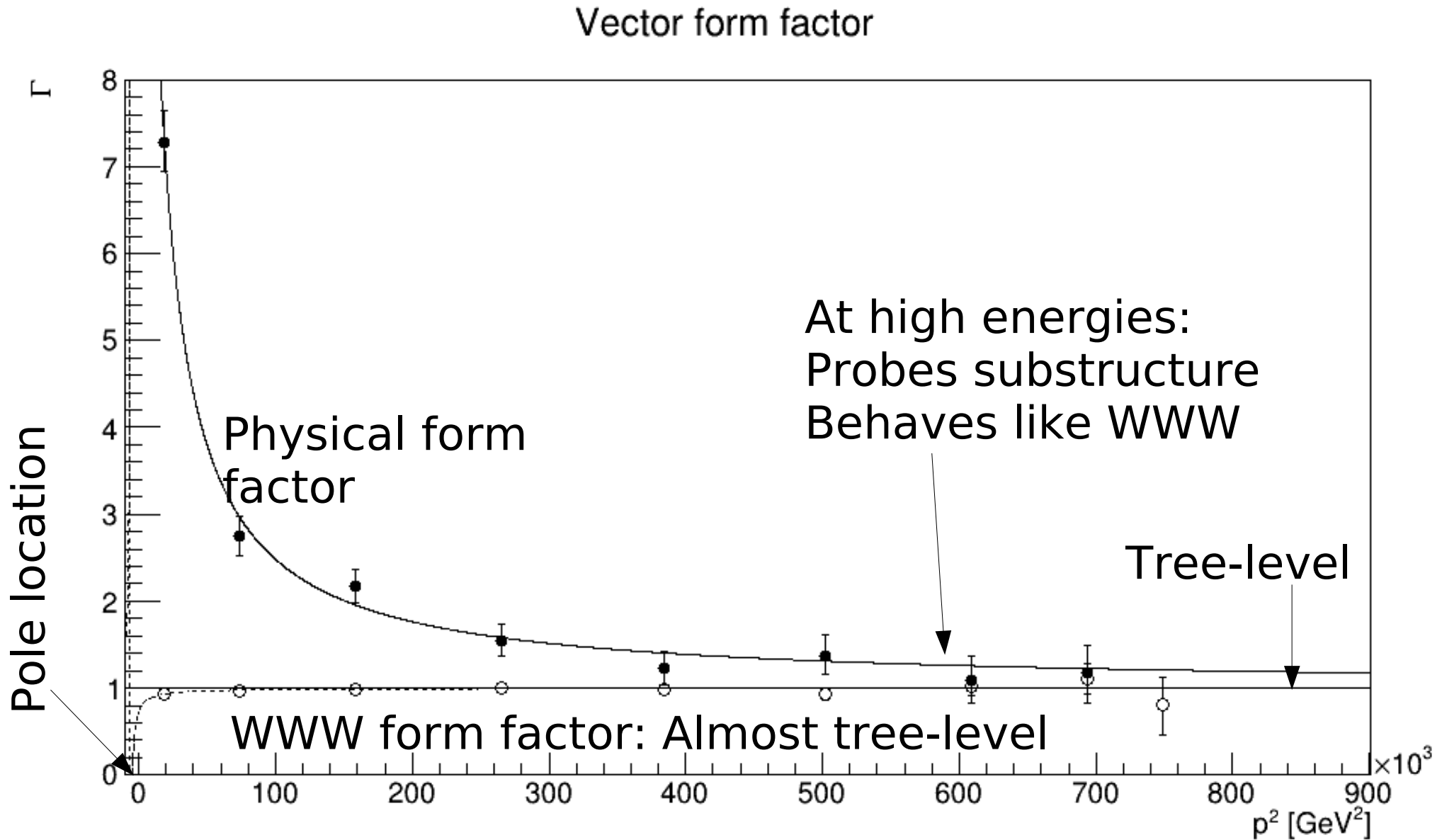
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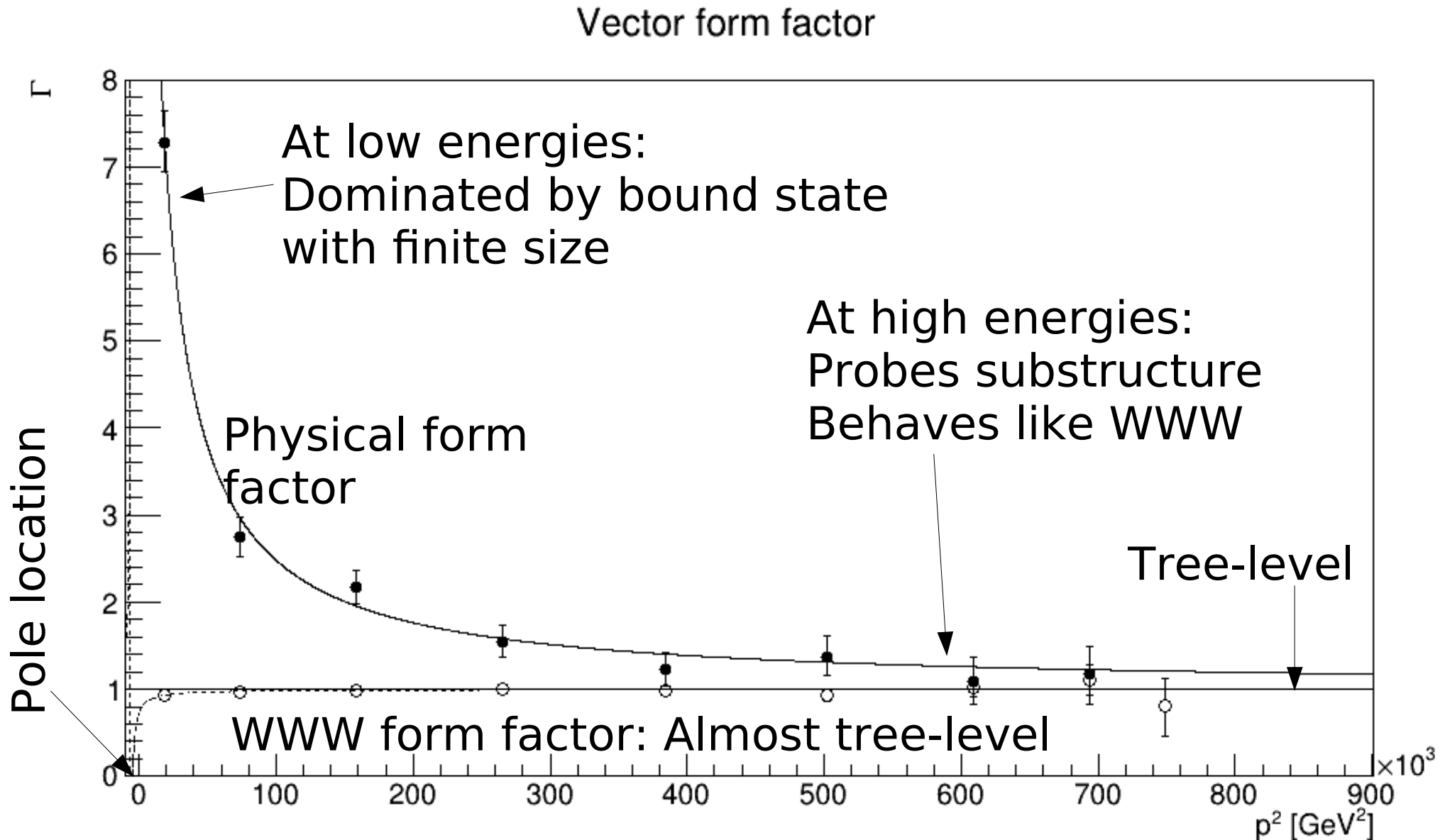
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Bound states as extended objects

[Maas,Raubitzke,Törek'18]



- Physical $mr \sim 2$ while gauge-dependent W has $mr \sim 0.5i$

Exploring implications

-

Full standard model

Flavor

[Fröhlich et al.'80,
Egger, Maas, Sondenheimer'17]

- Flavor has two components
 - Global $SU(3)$ generation
 - Local $SU(2)$ weak gauge (up/down distinction)

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- Gauge-invariant state, but custodial doublet

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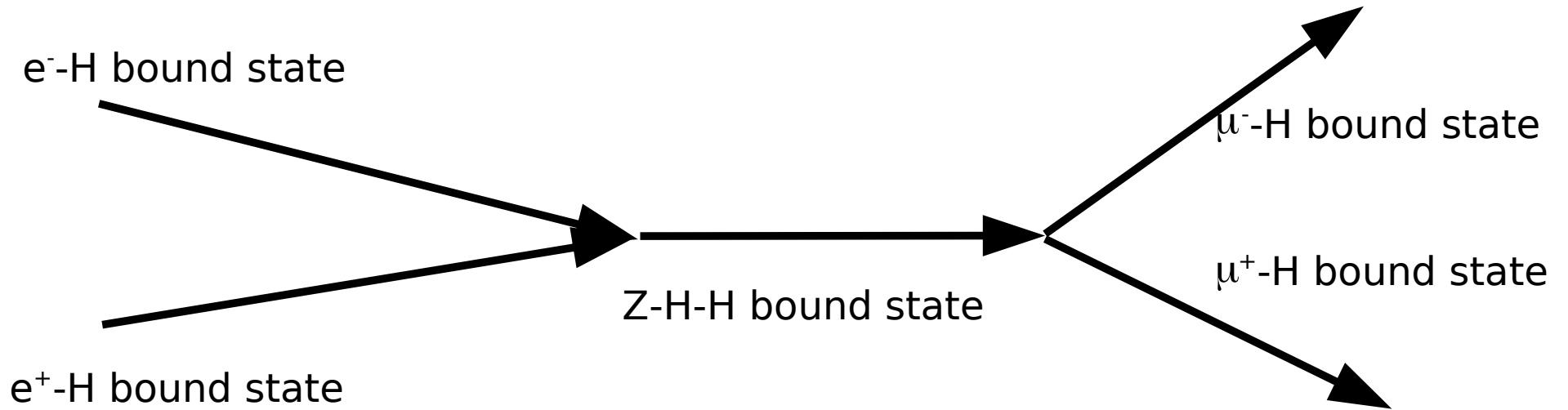
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How events looks like (LEP/ILC)

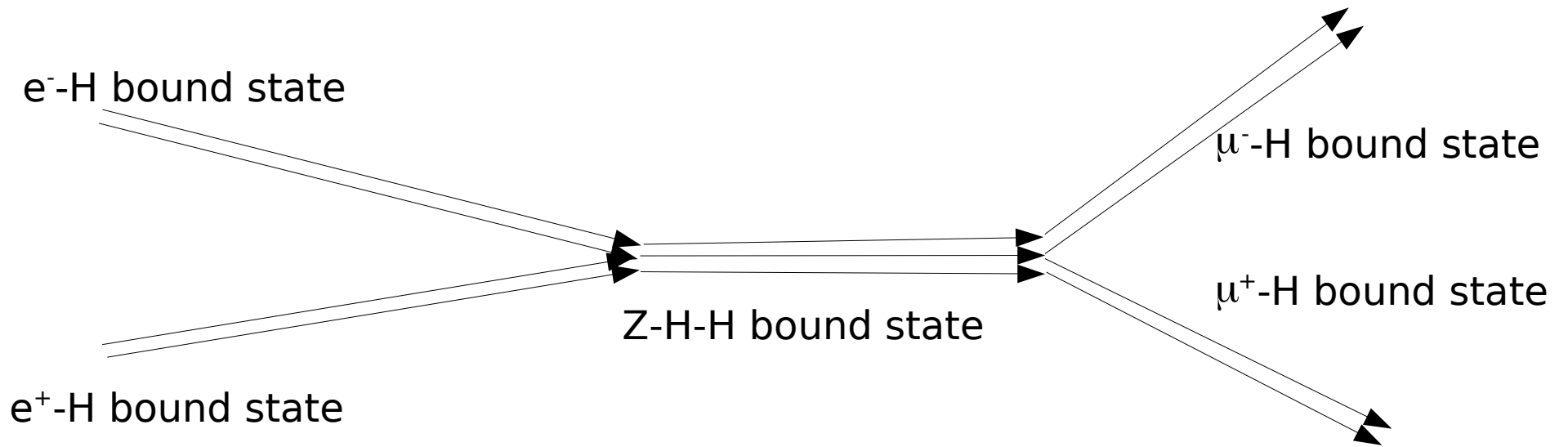
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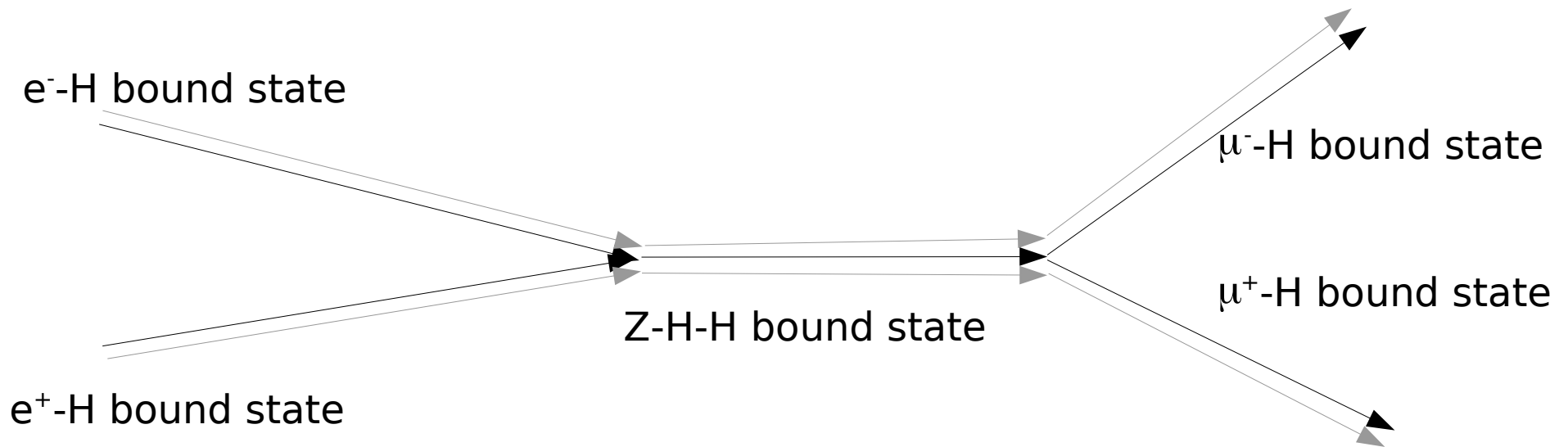
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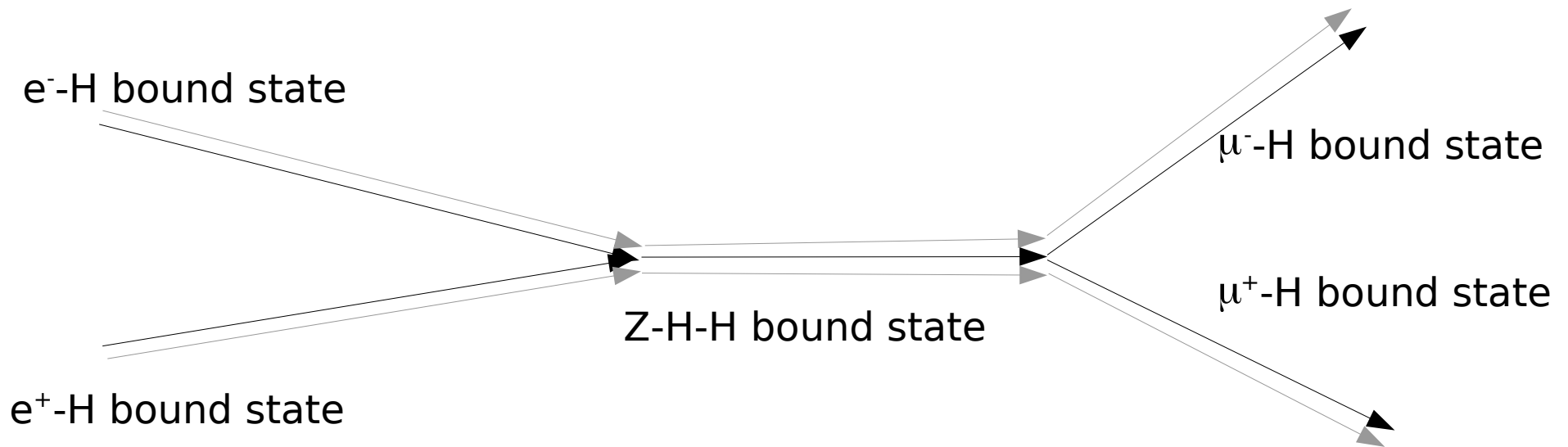
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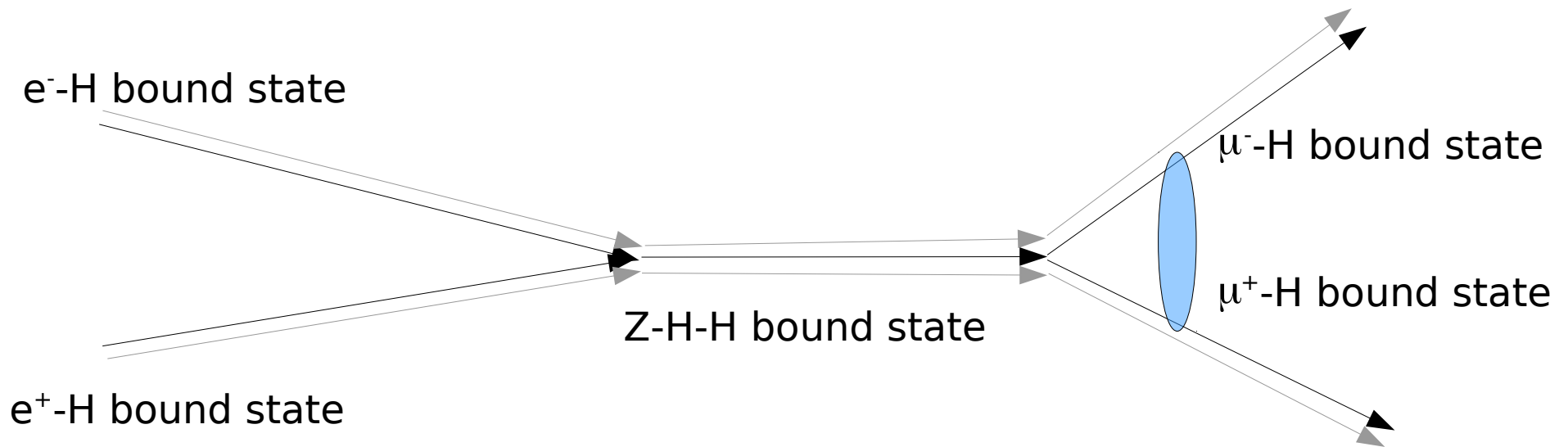
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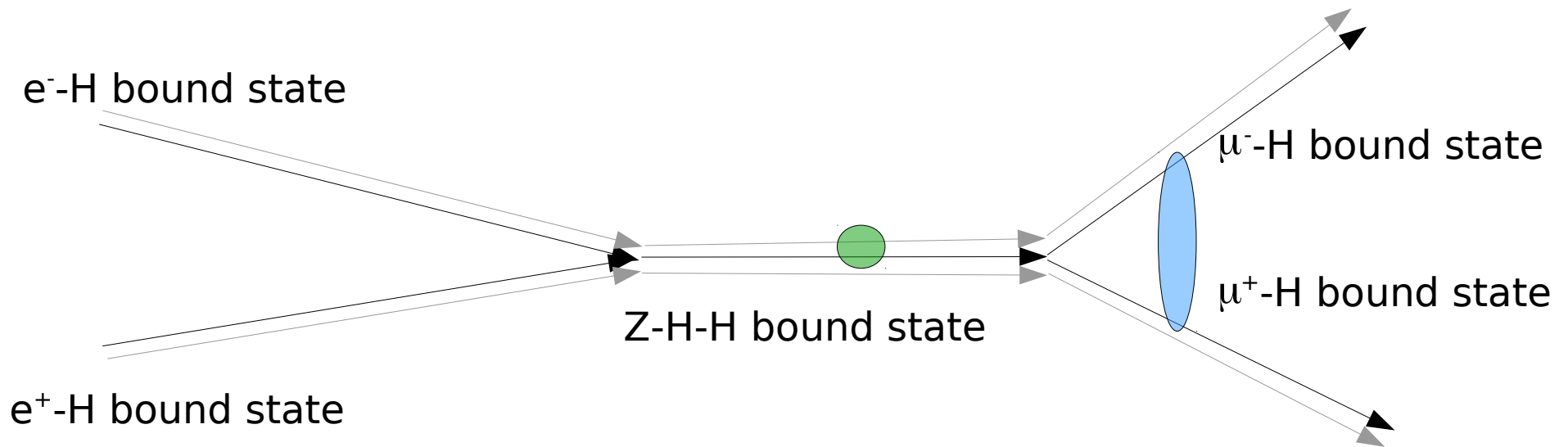
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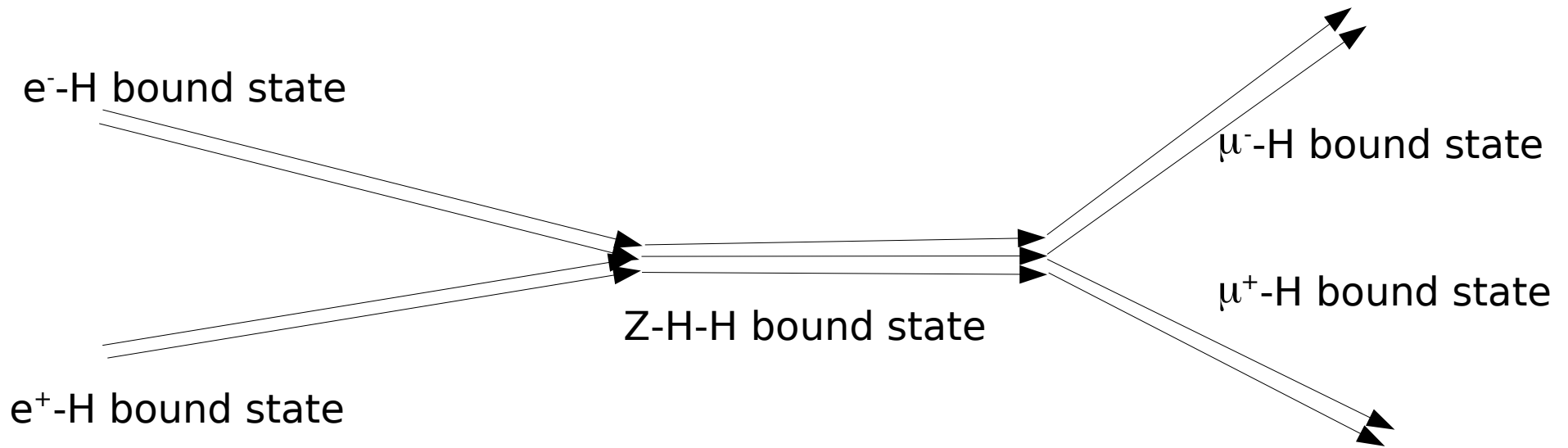
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 - **Ordinary ones**: Large and detected
 - **New ones**: **Small**, require more sensitivity

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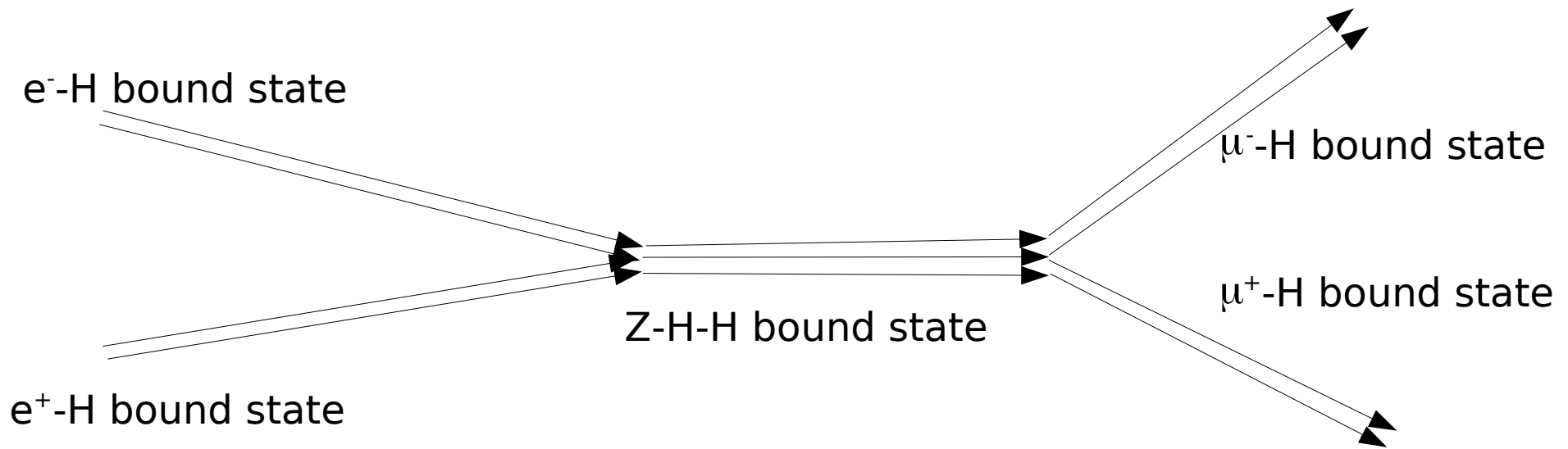
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- Description of impact?

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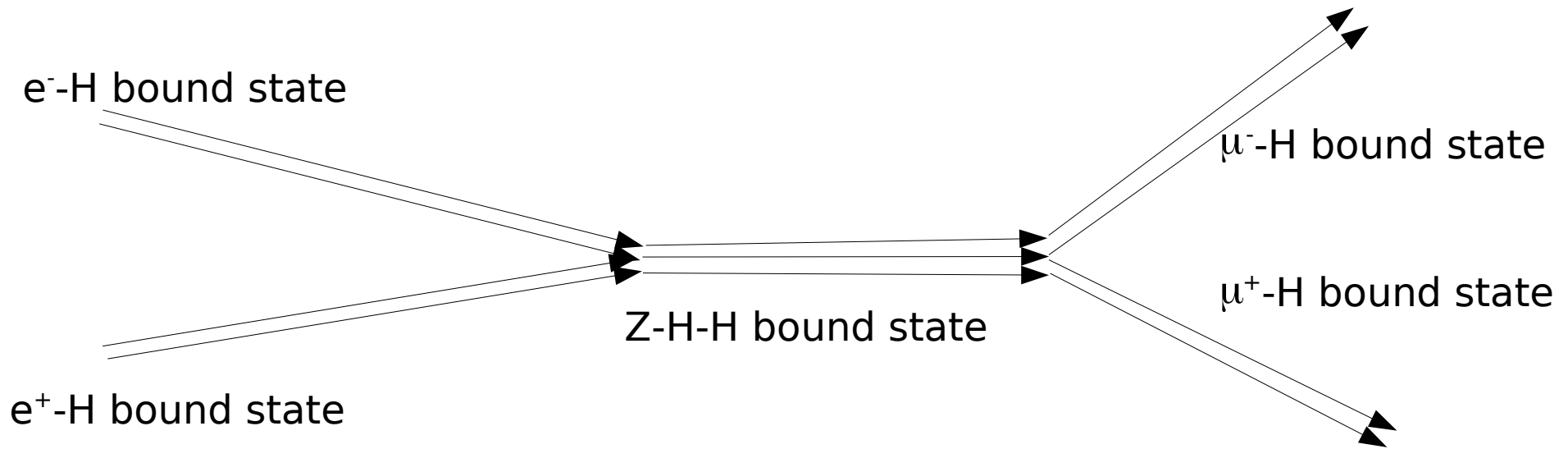
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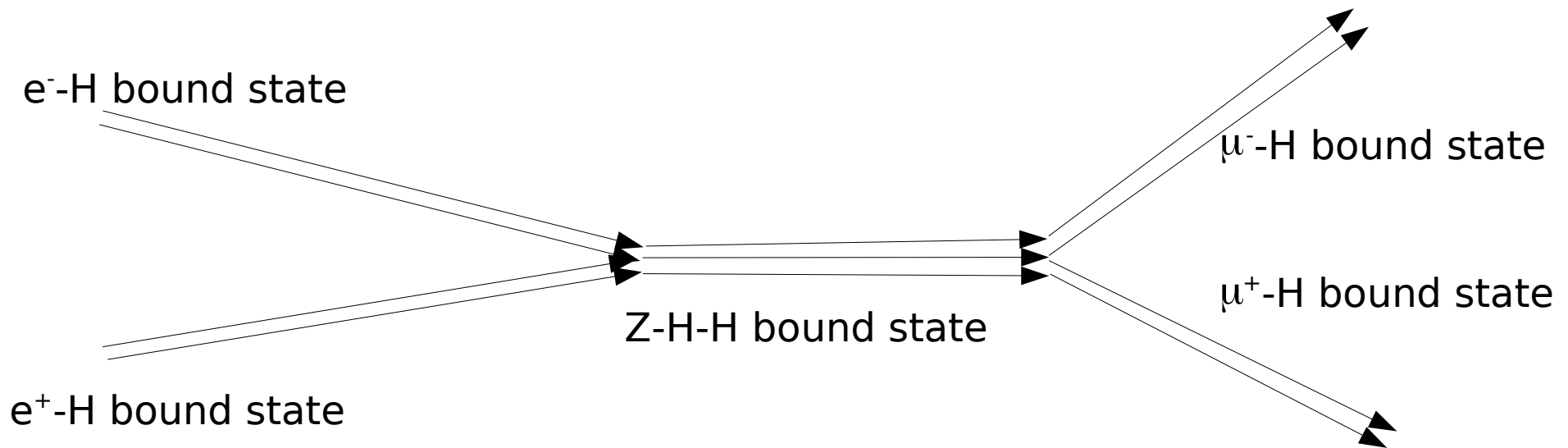


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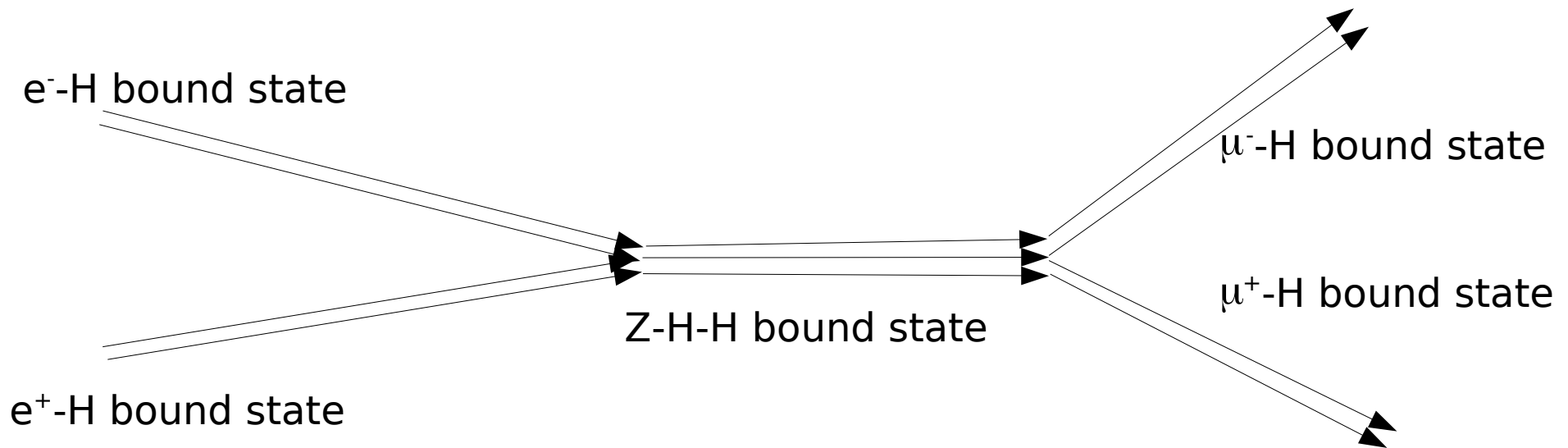
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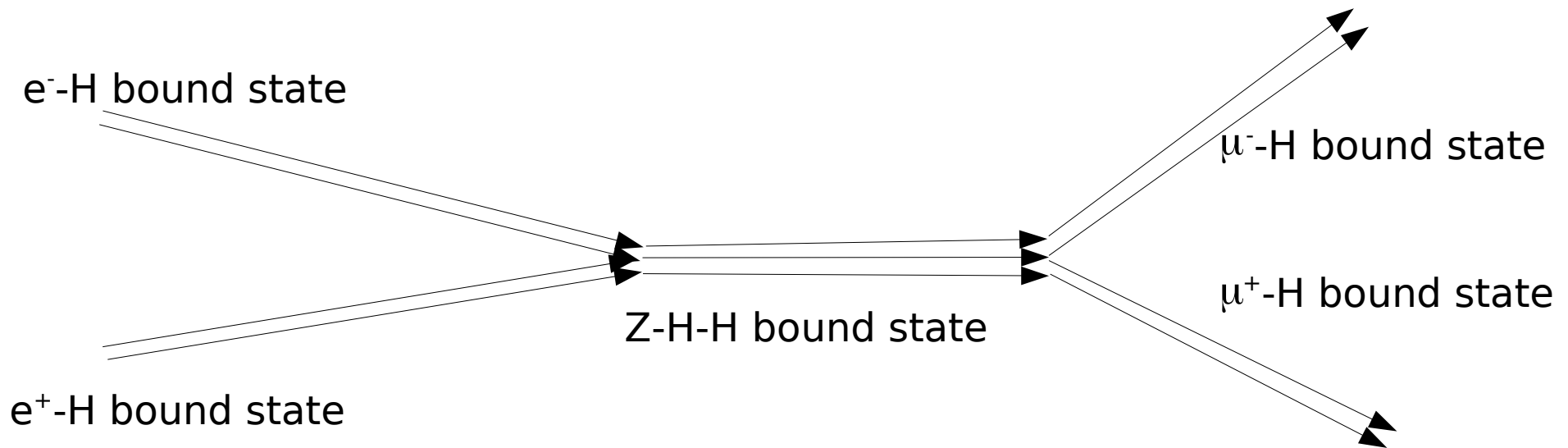
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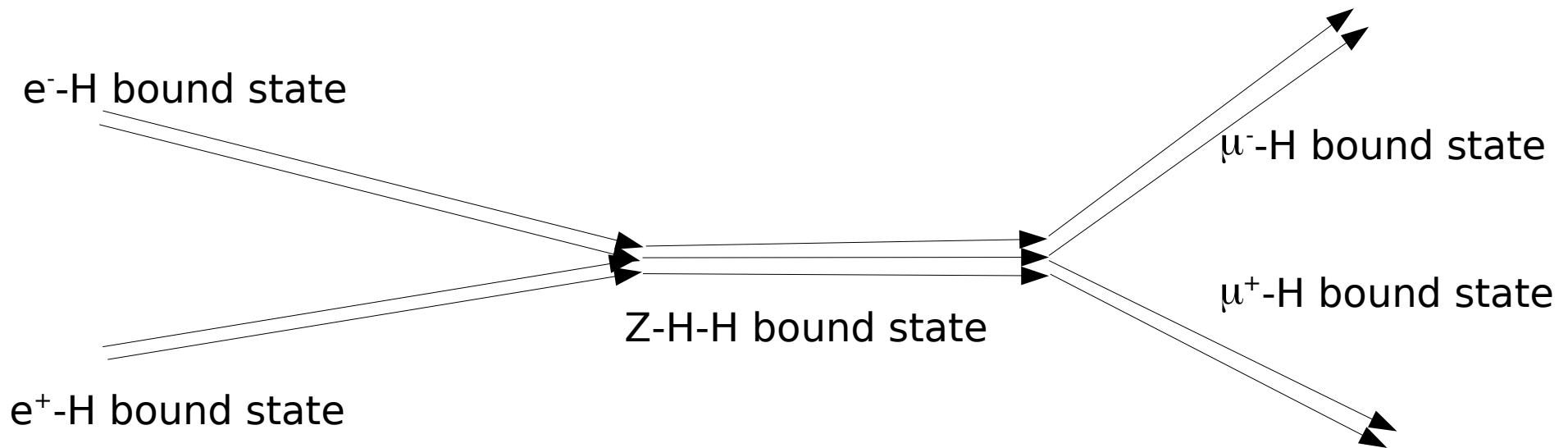
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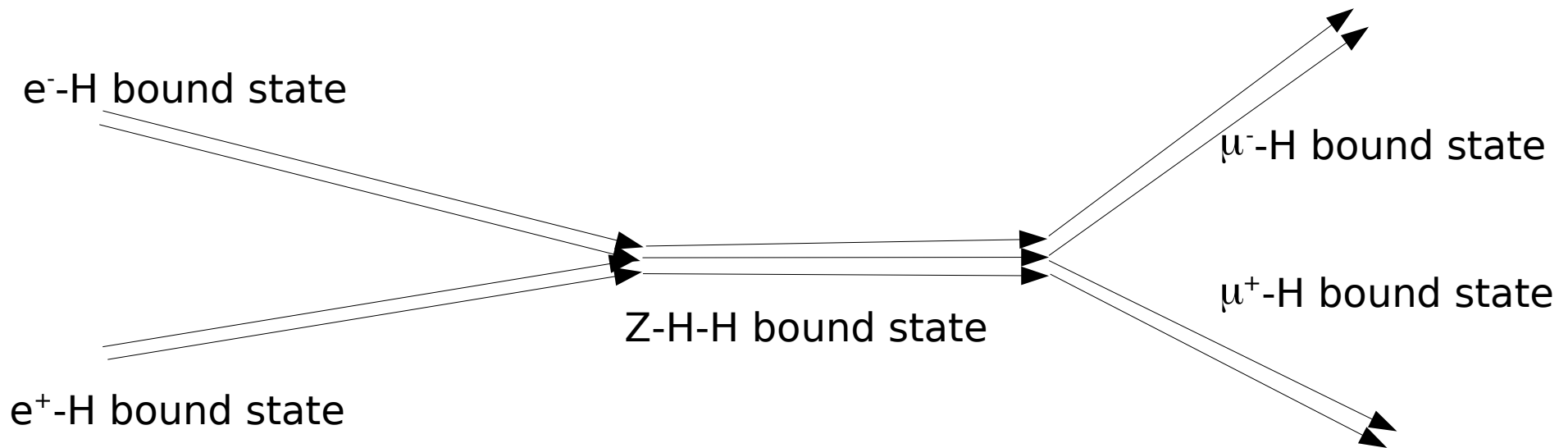
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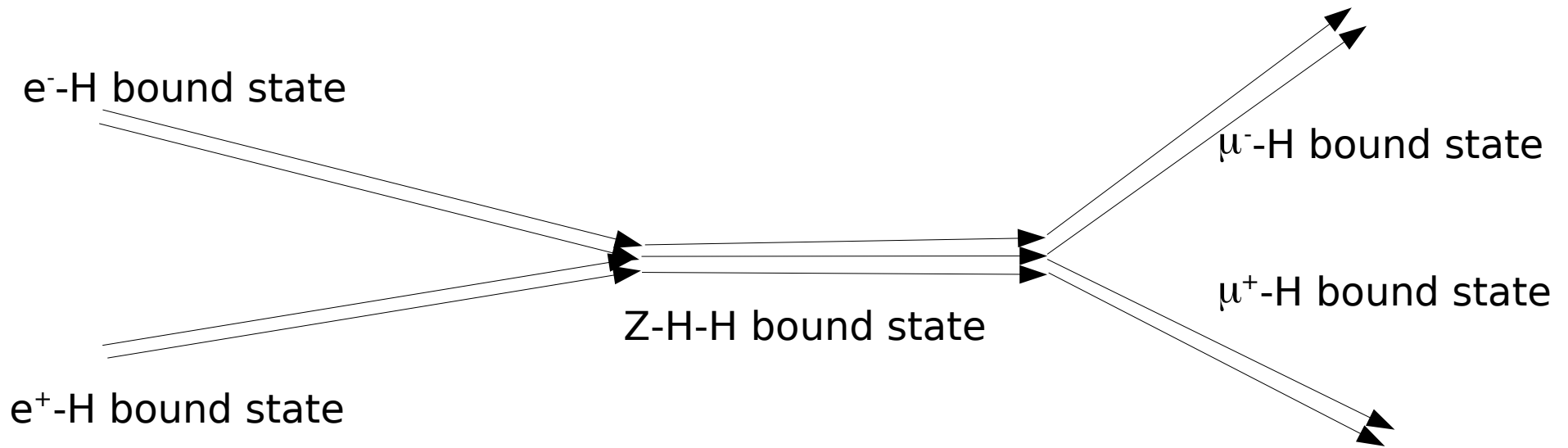
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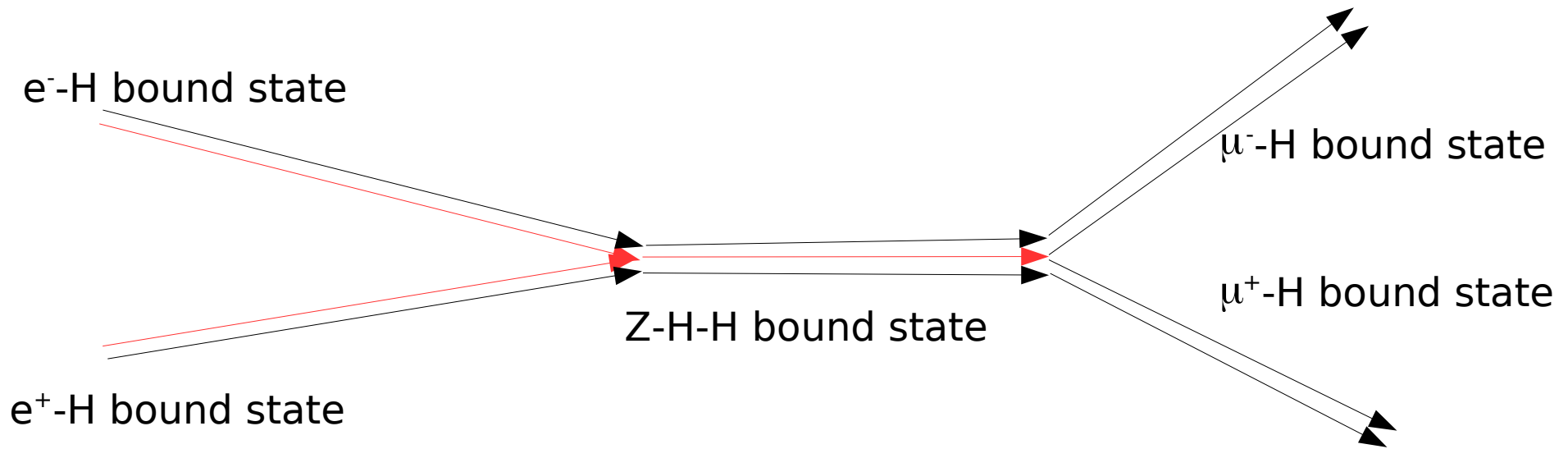
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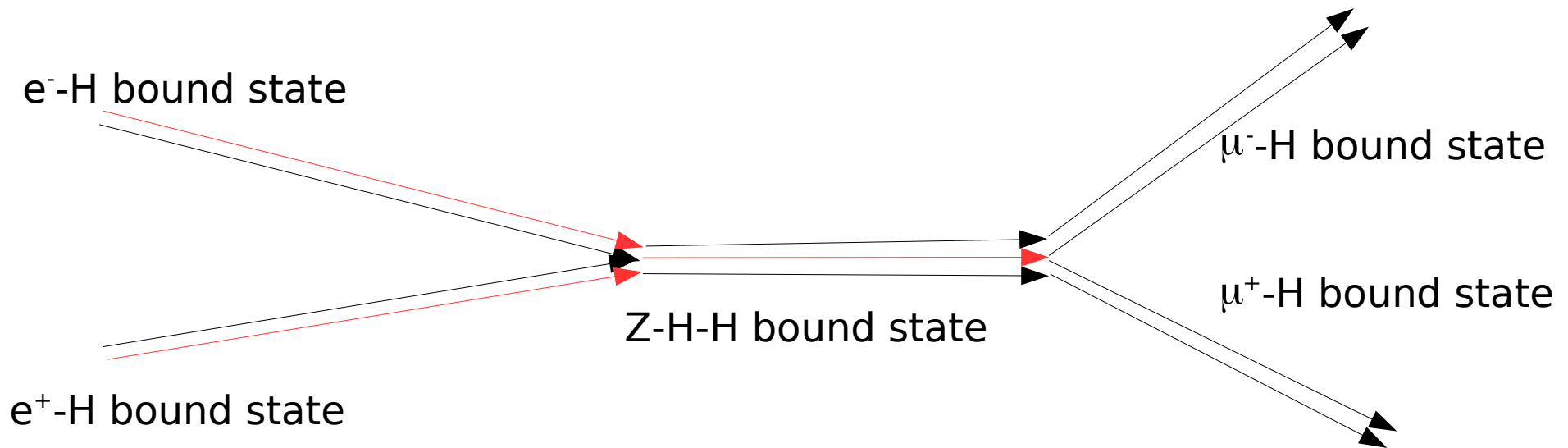
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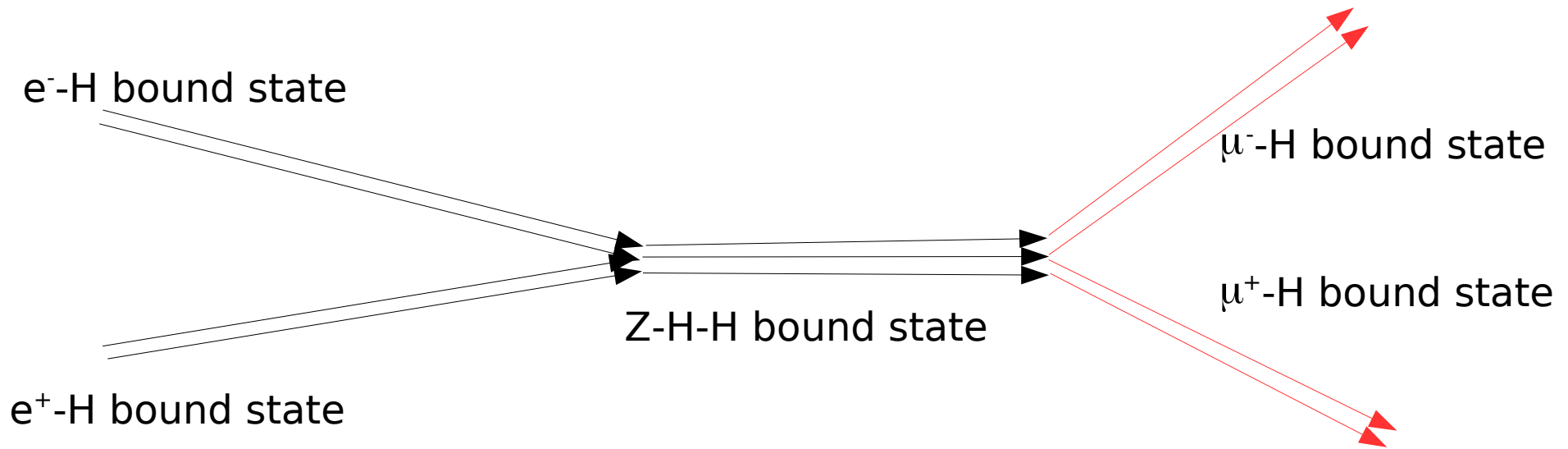
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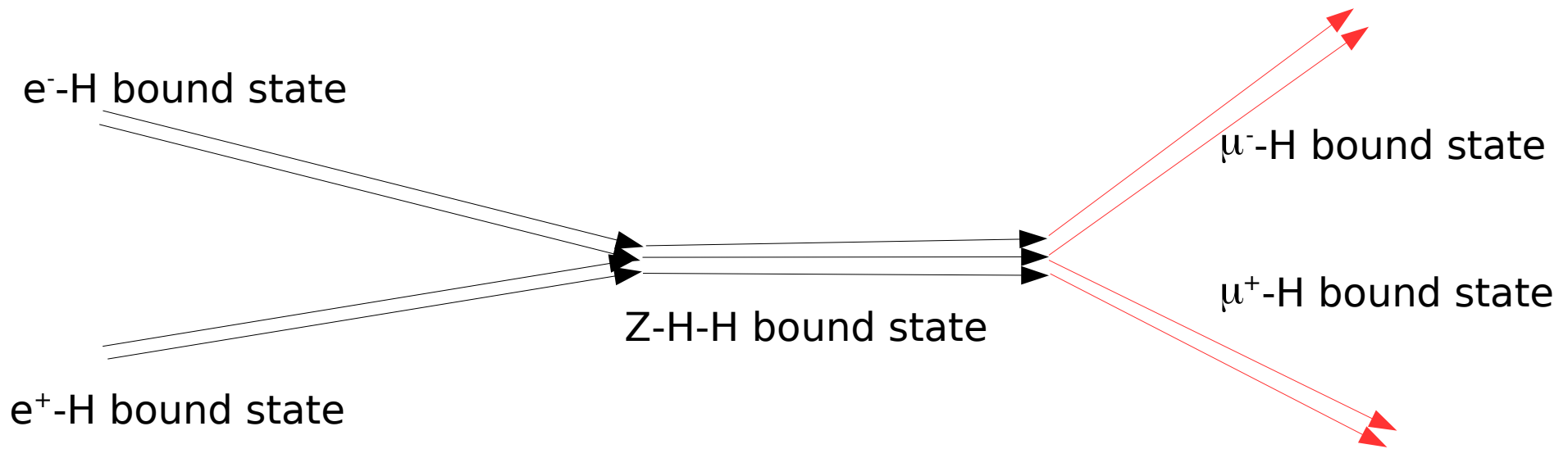
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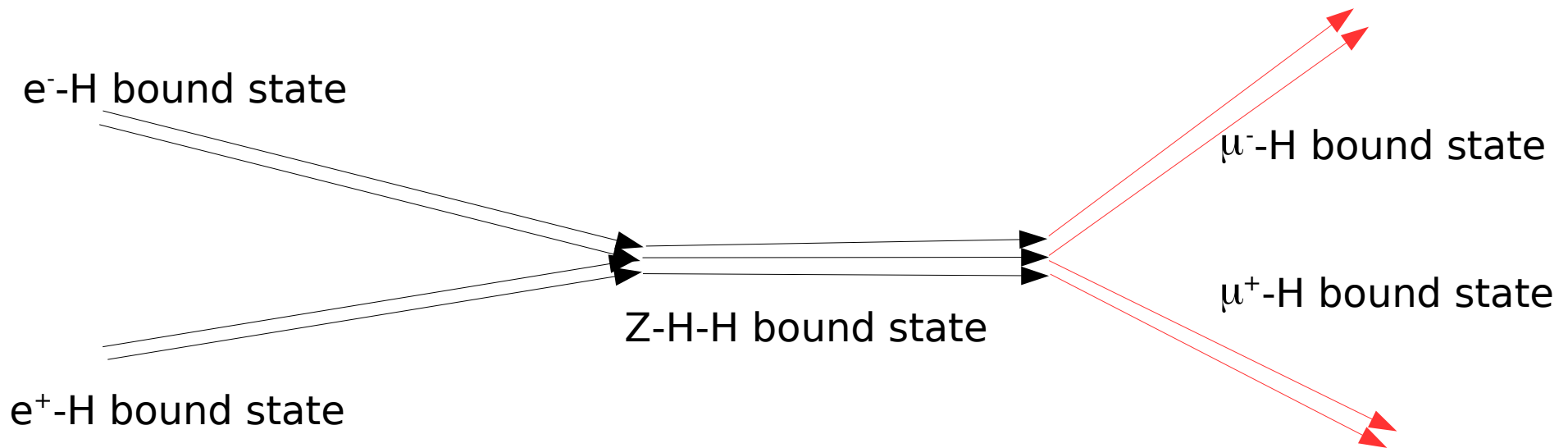
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- LHC?

Flavor of hadrons

[Egger, Maas, Sondenheimer'17]

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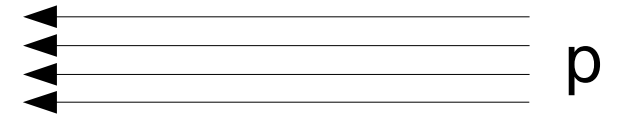
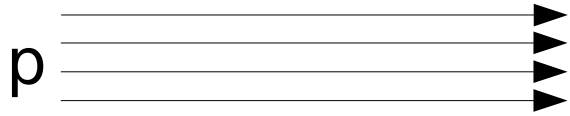
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 - Strong couplings to Higgs: tops, weak gauge bosons

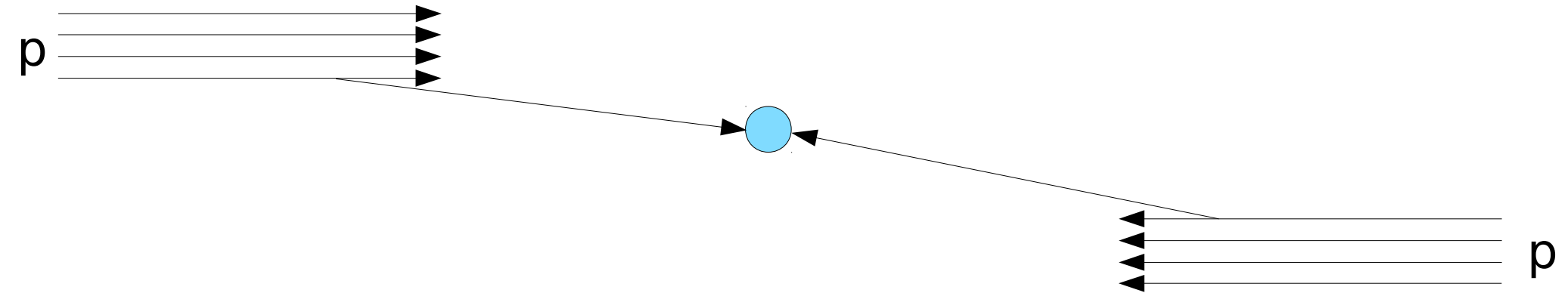
Constraining the valence Higgs

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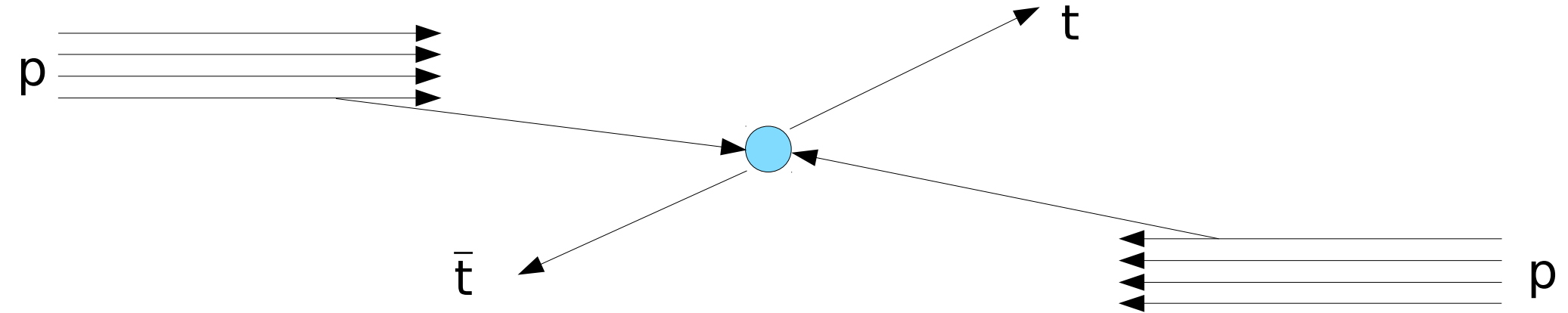
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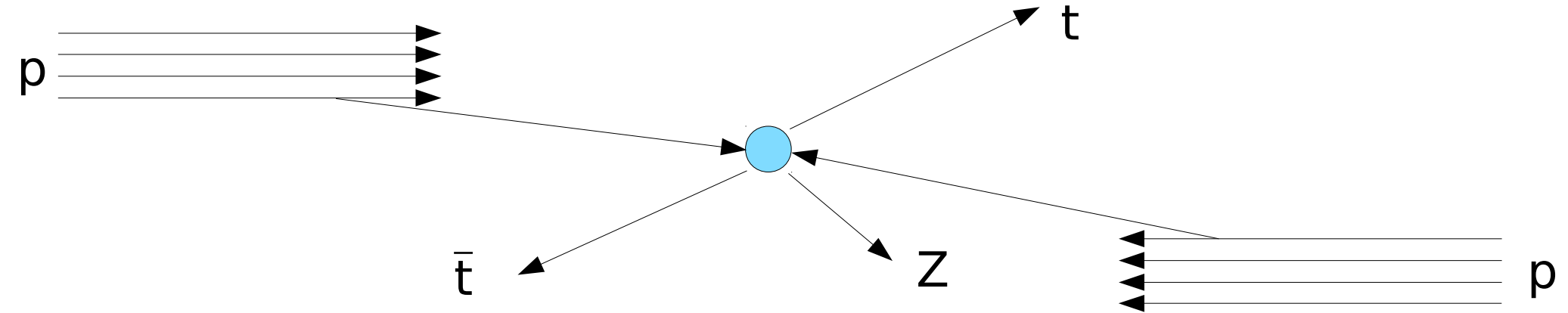
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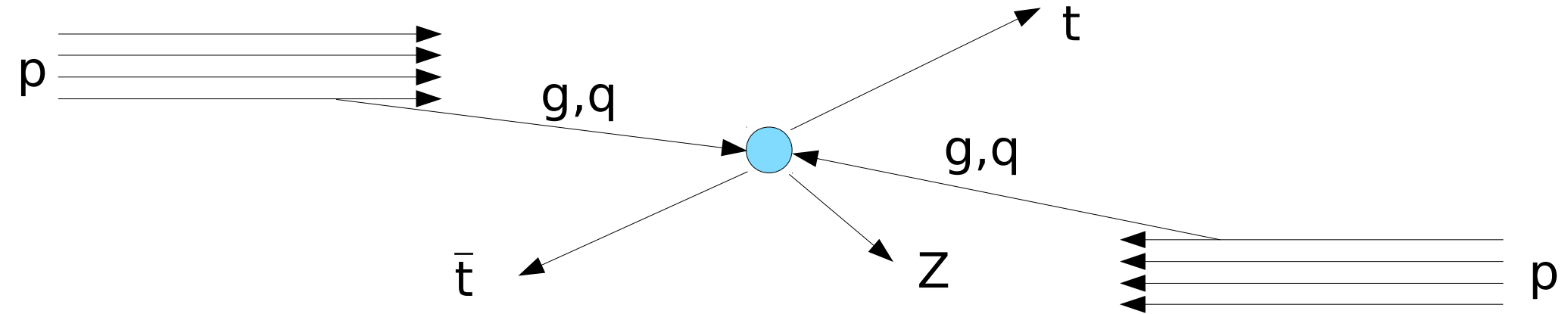
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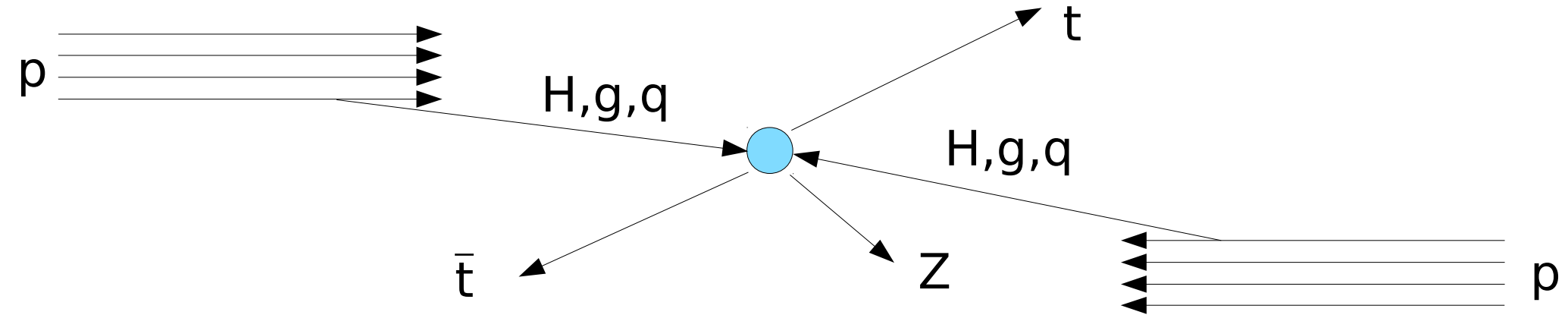
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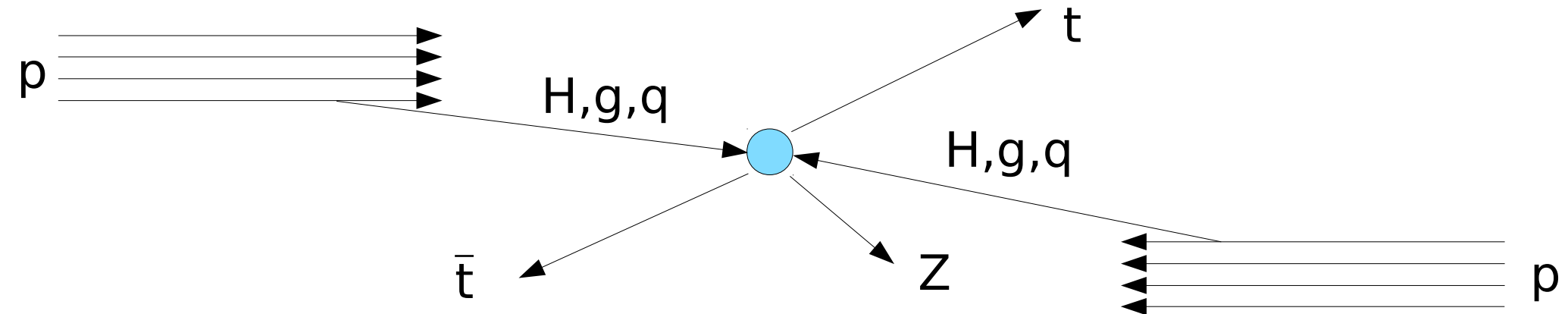
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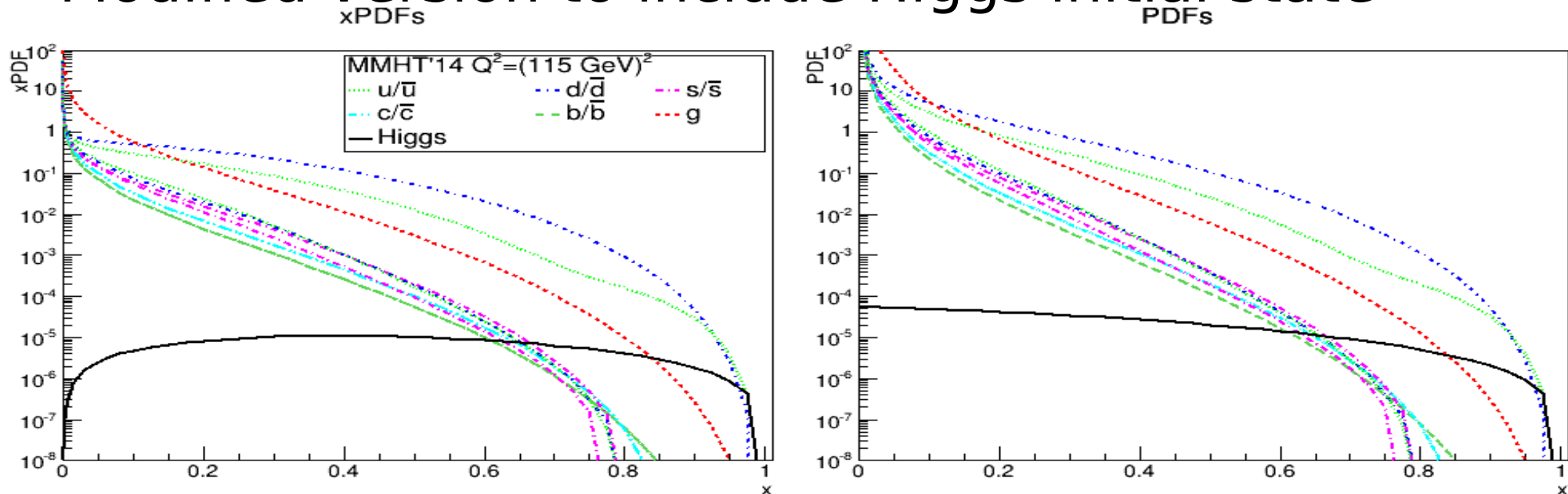
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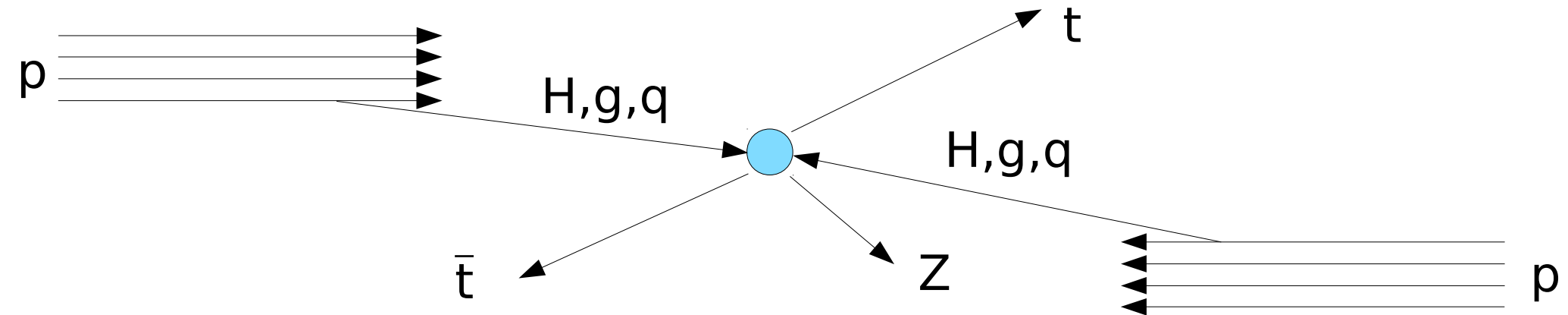
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Starting guess: Higgs PDF still 'condensate'-like

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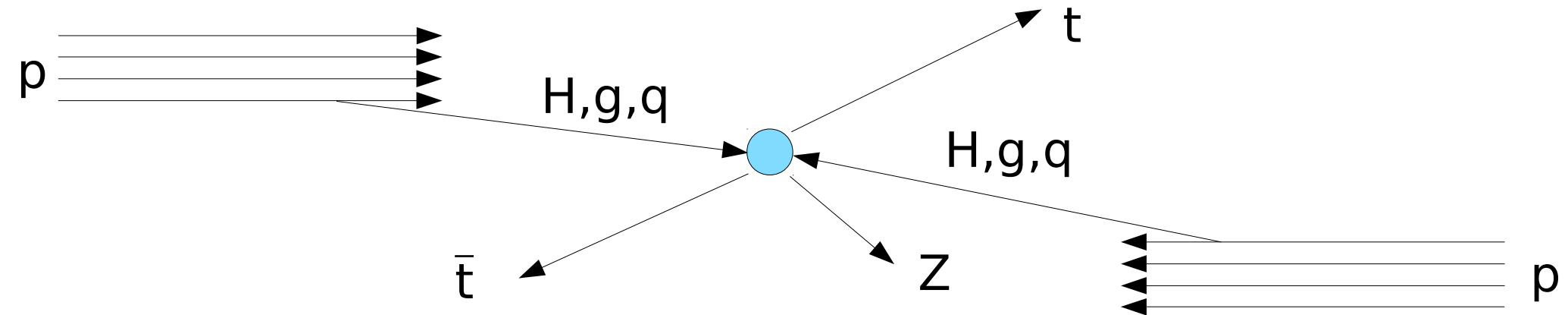
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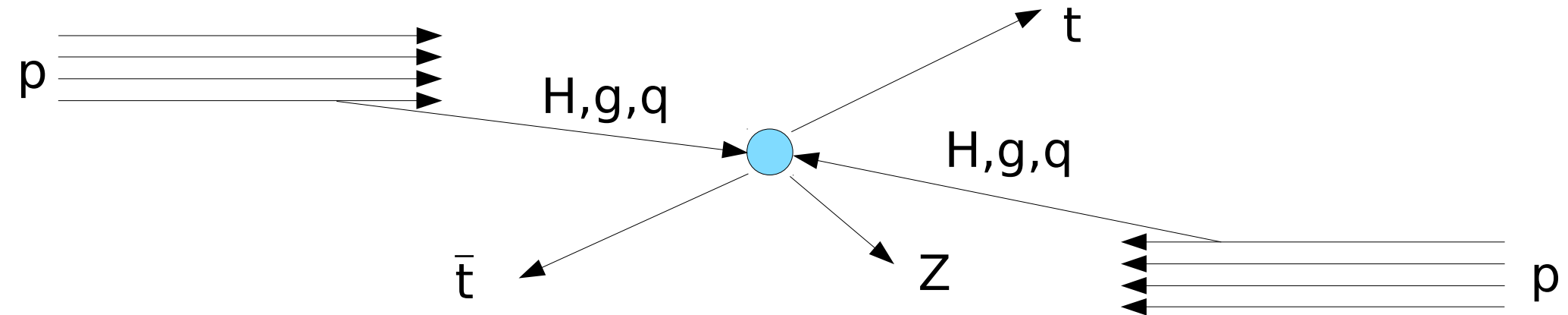
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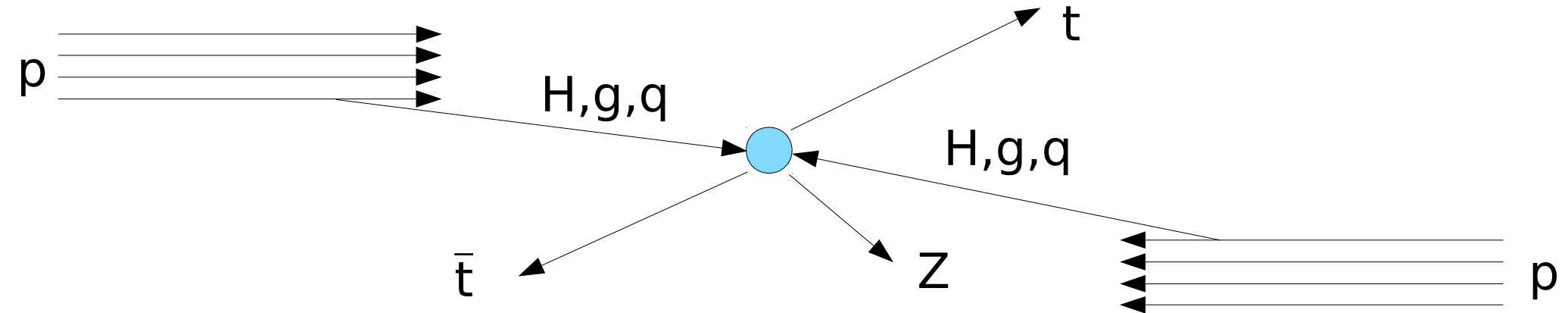
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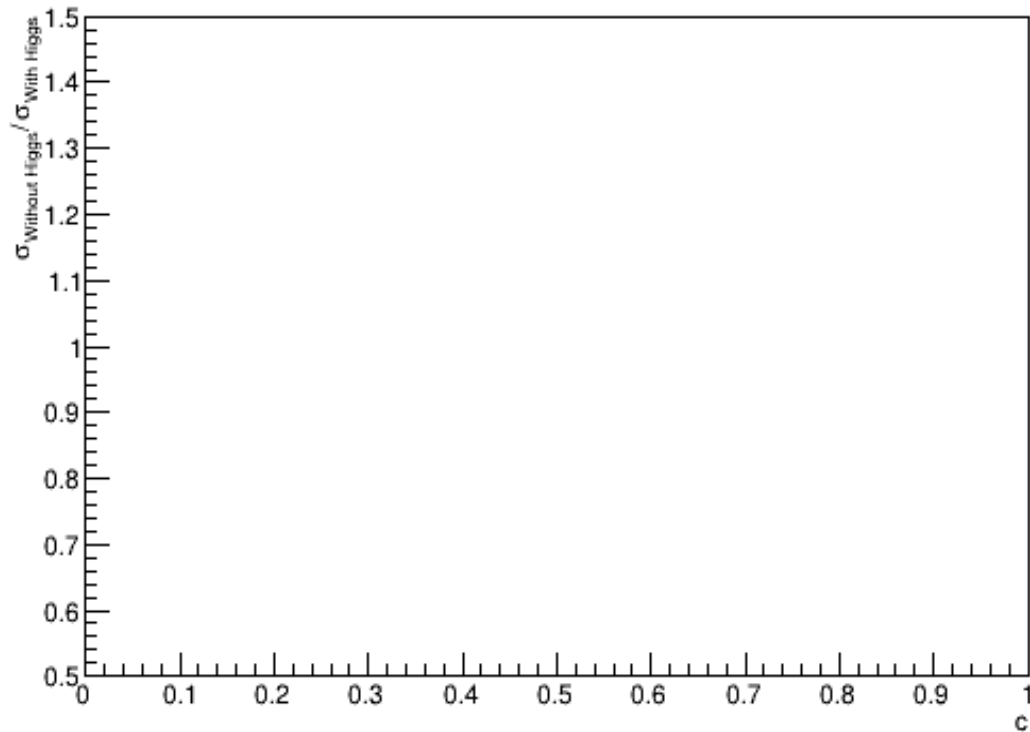
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- Creates full events
 - Every particle with all properties
 - Calculations of cross sections

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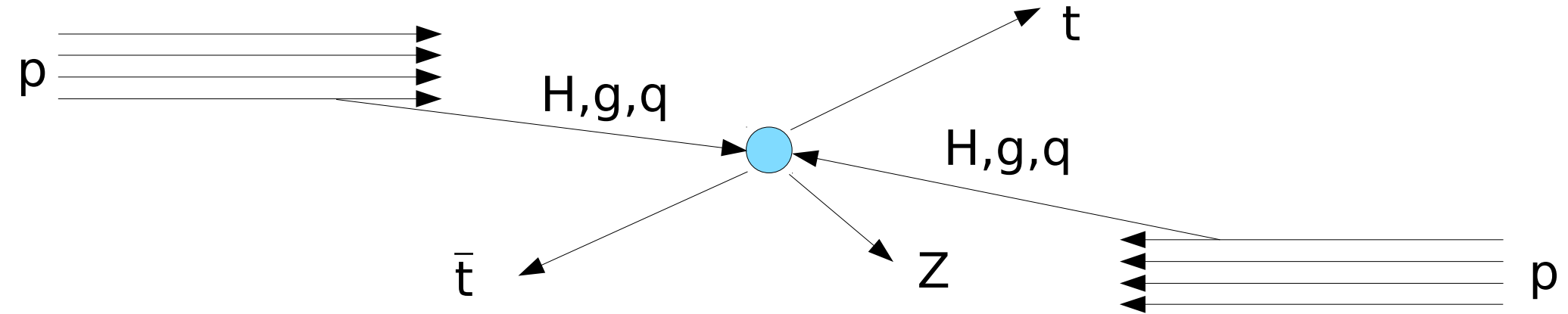
Normalized deviation from XS for $\bar{t}Z$



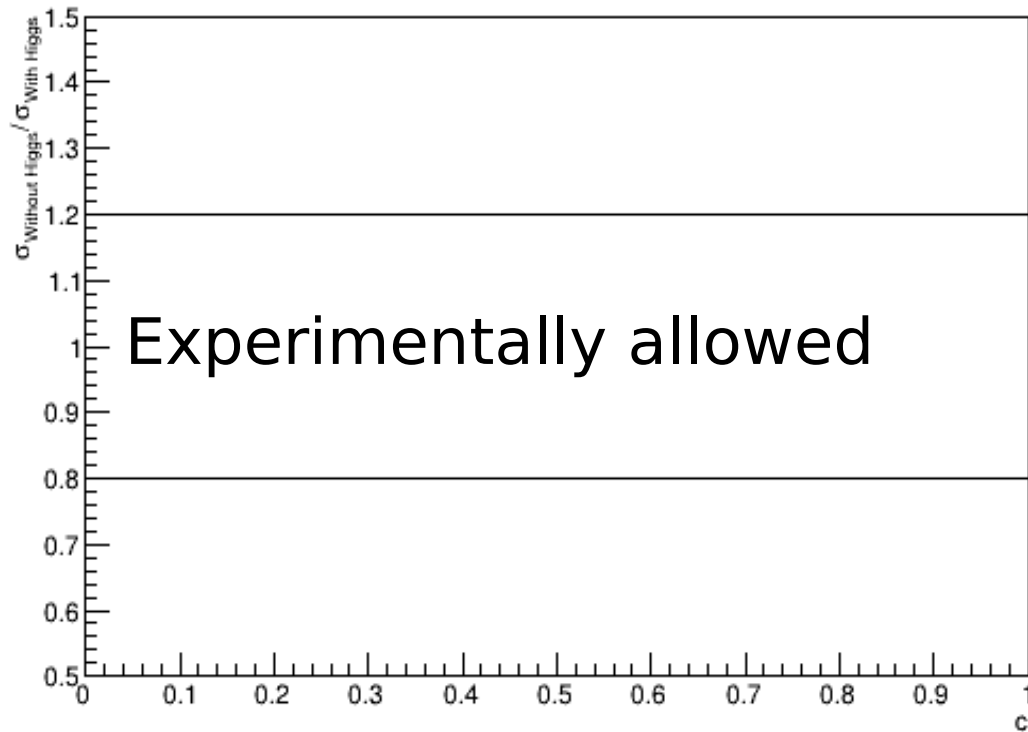
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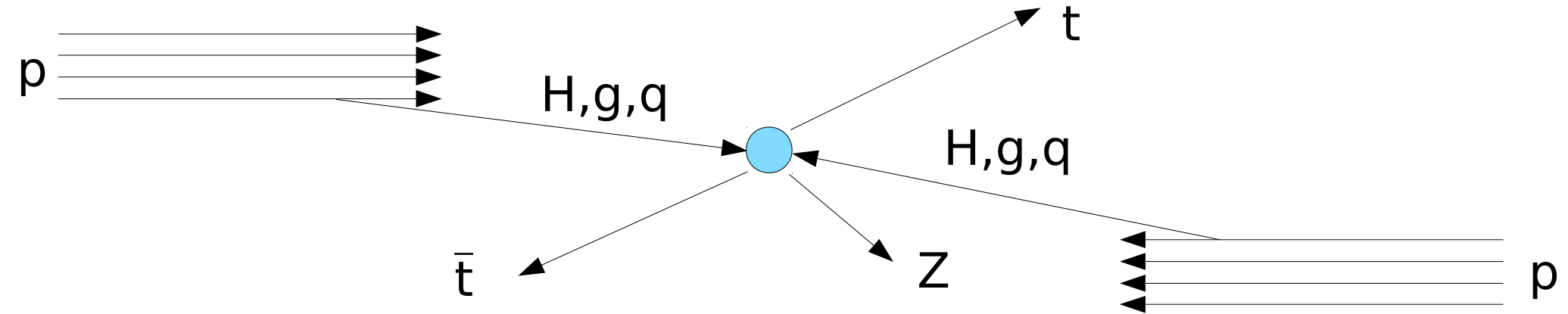
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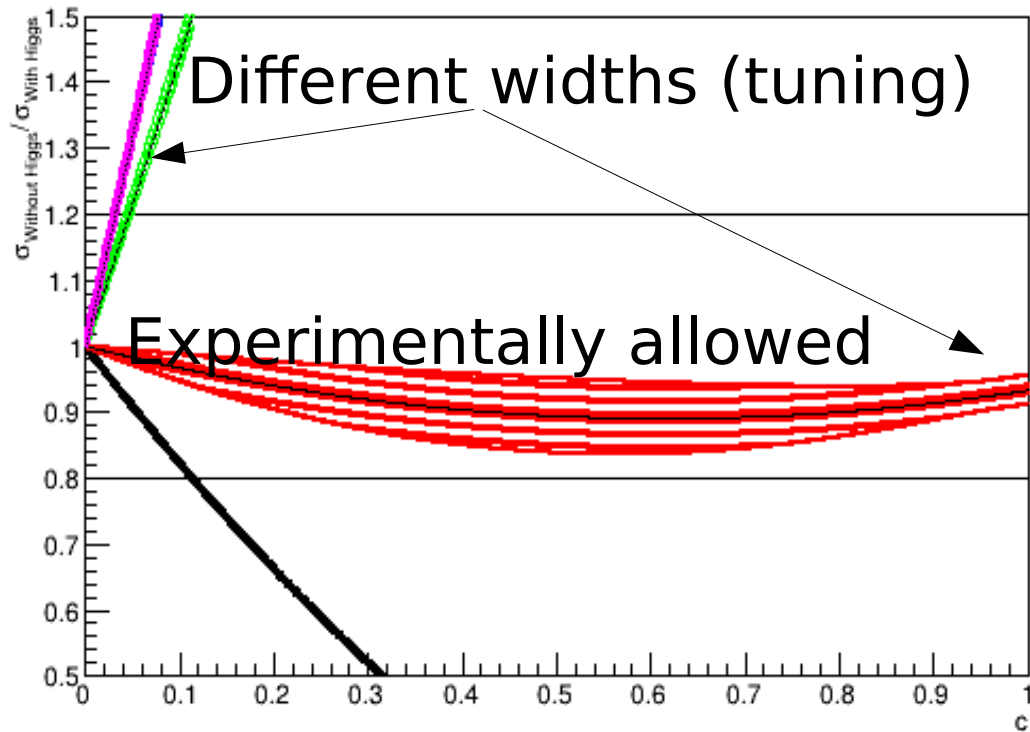
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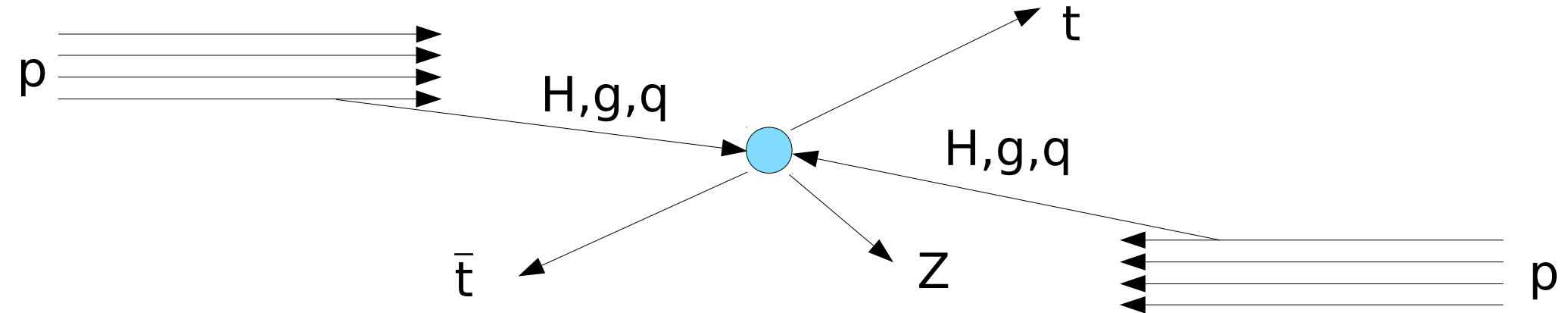
Normalized deviation from XS for $t\bar{t}Z$ **PRELIMINARY**



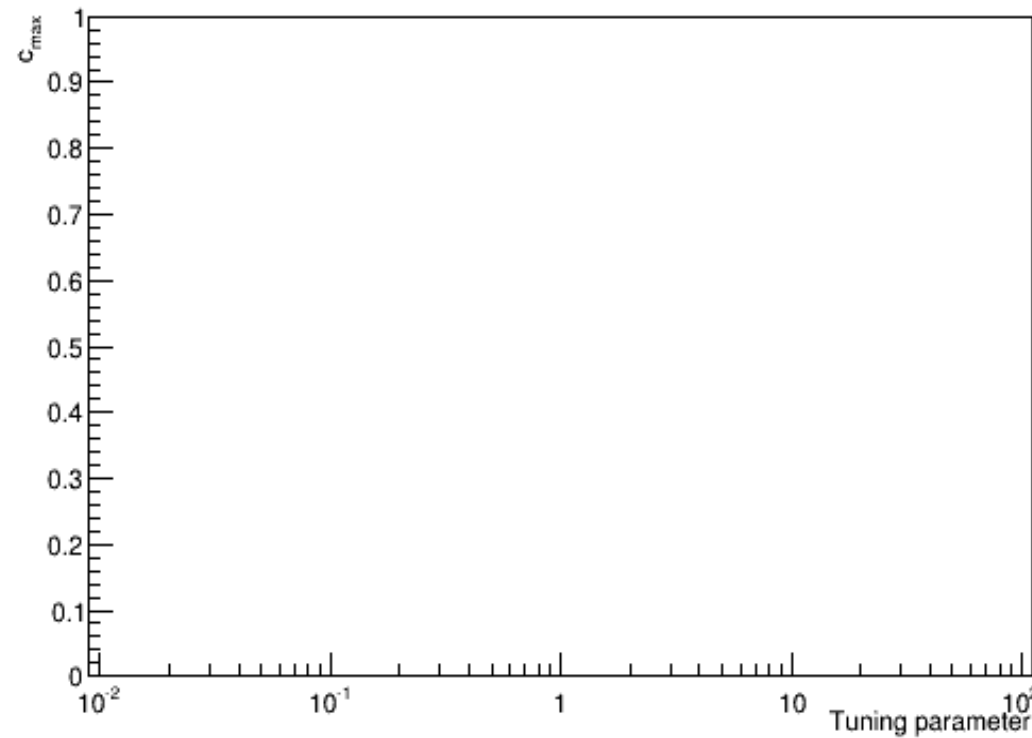
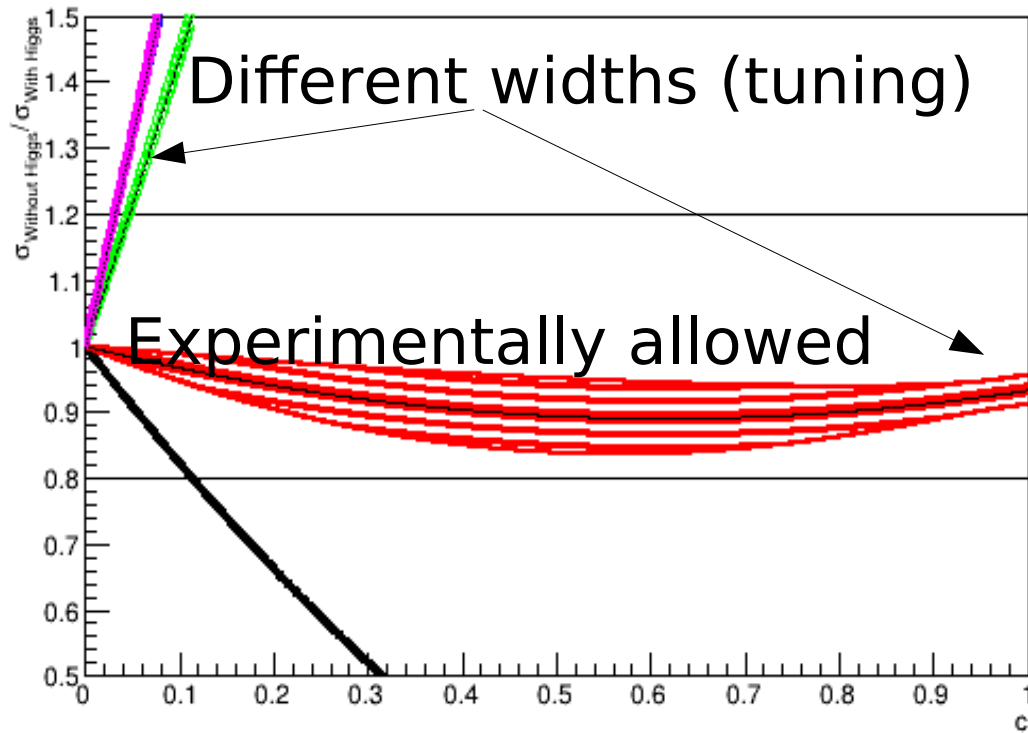
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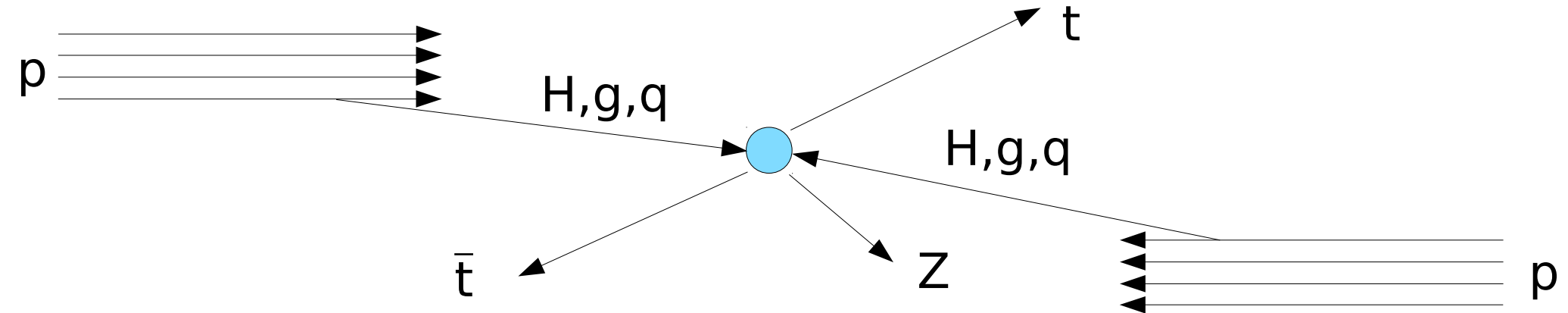
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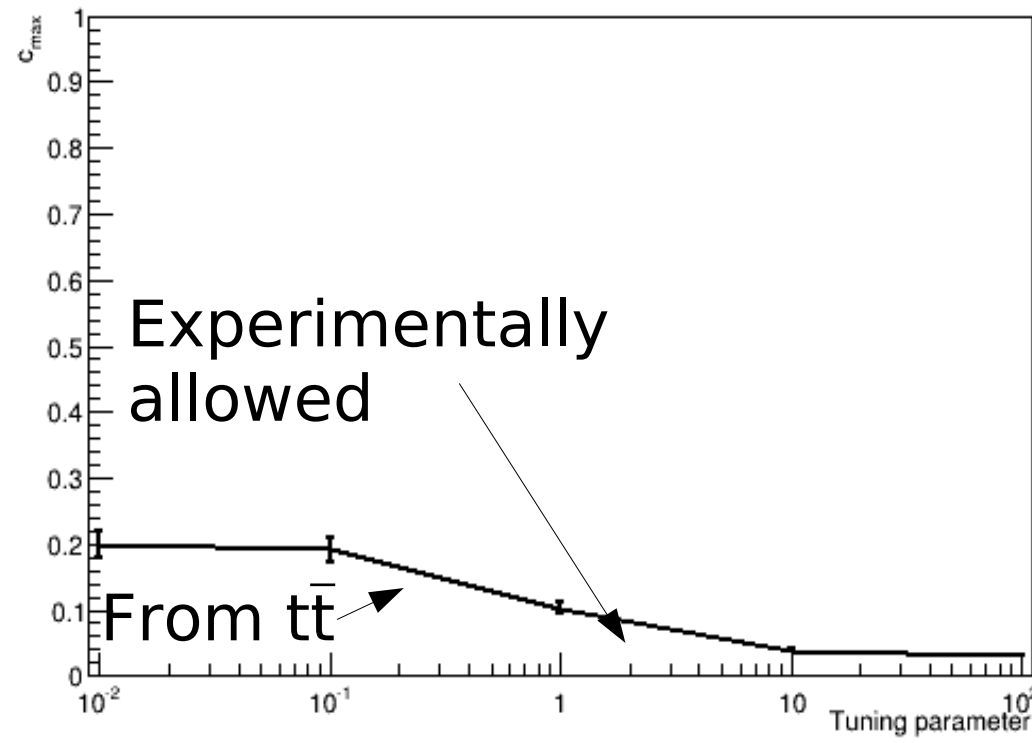
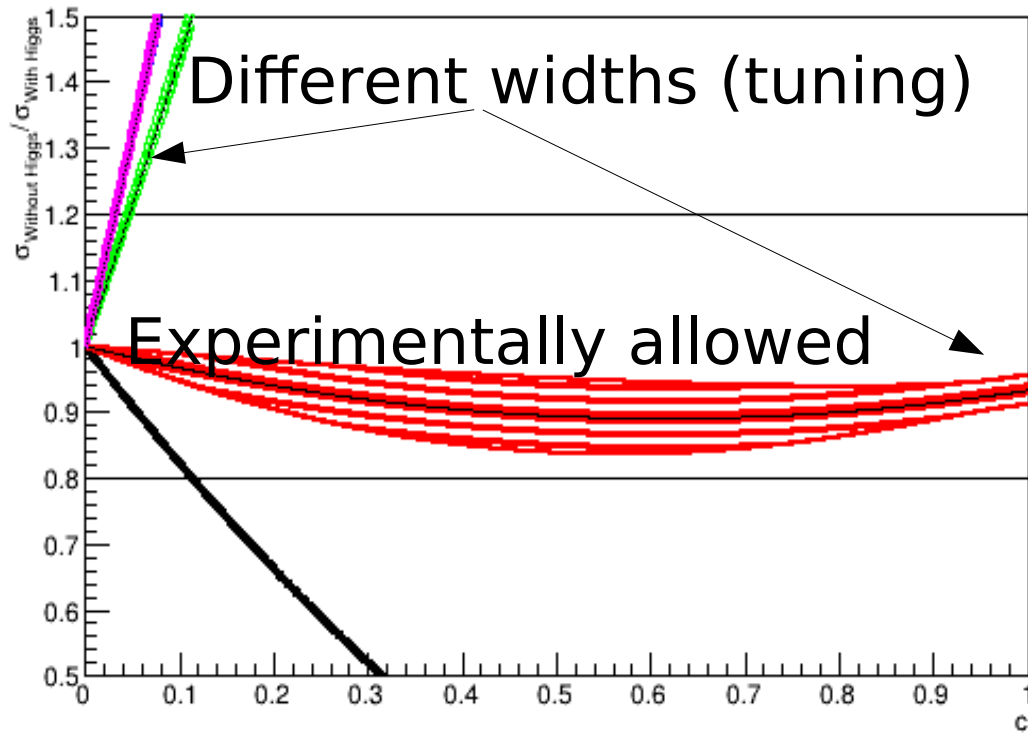
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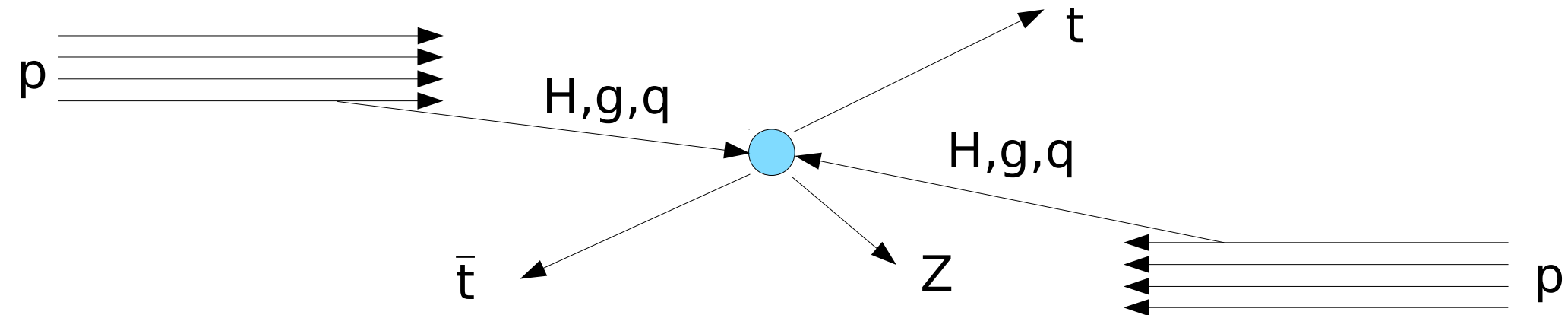
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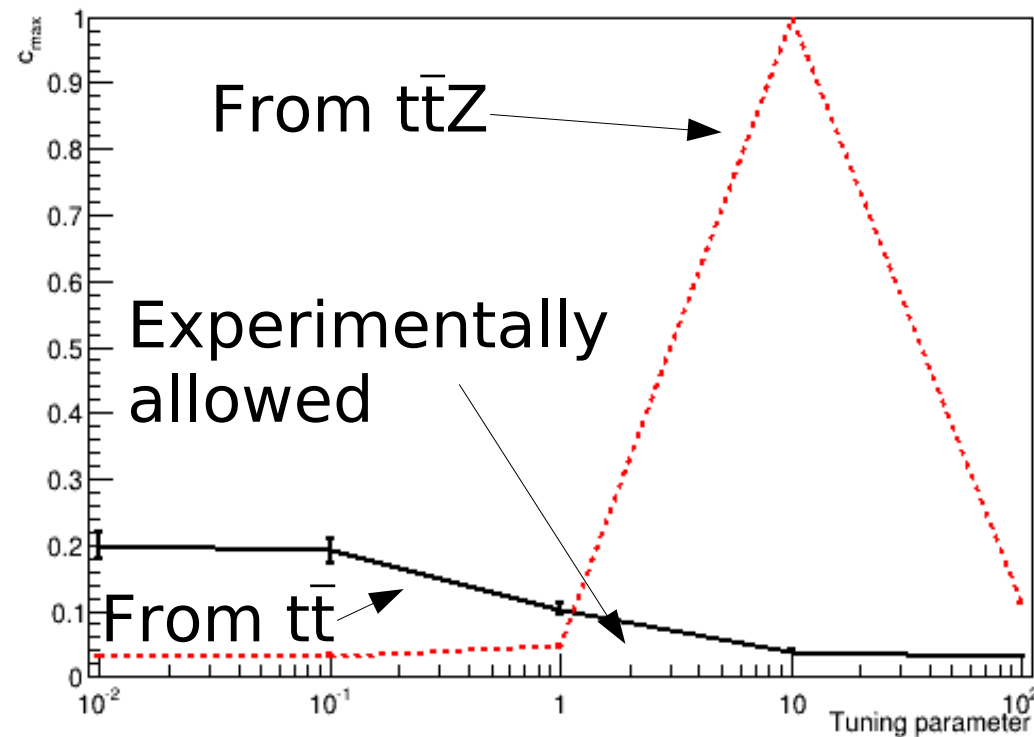
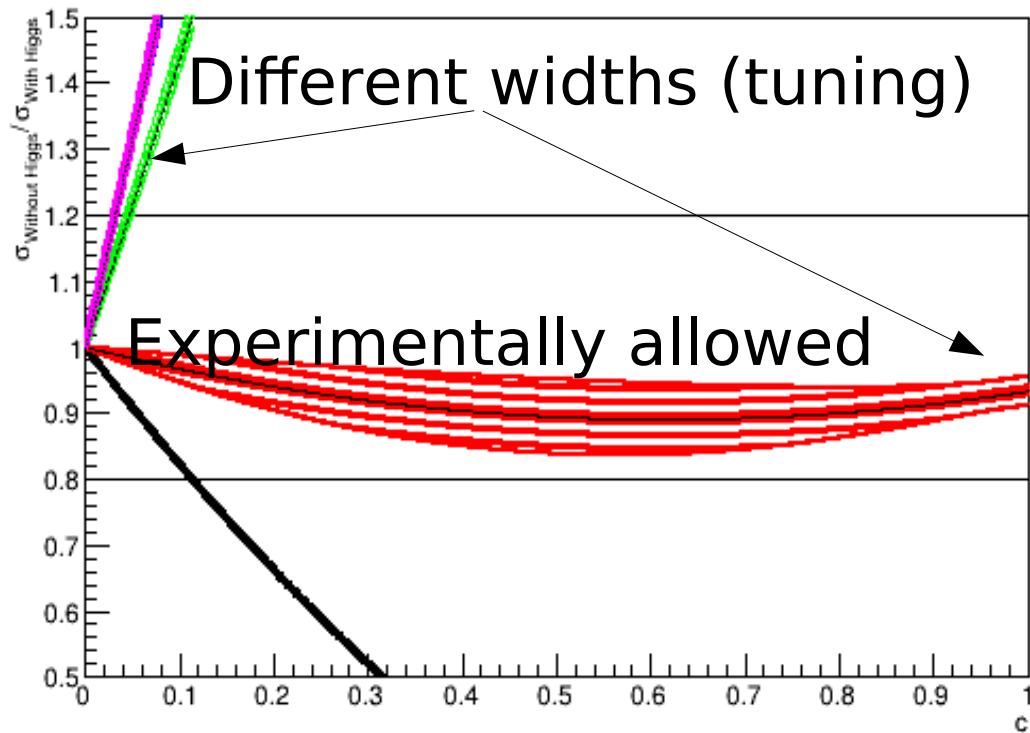
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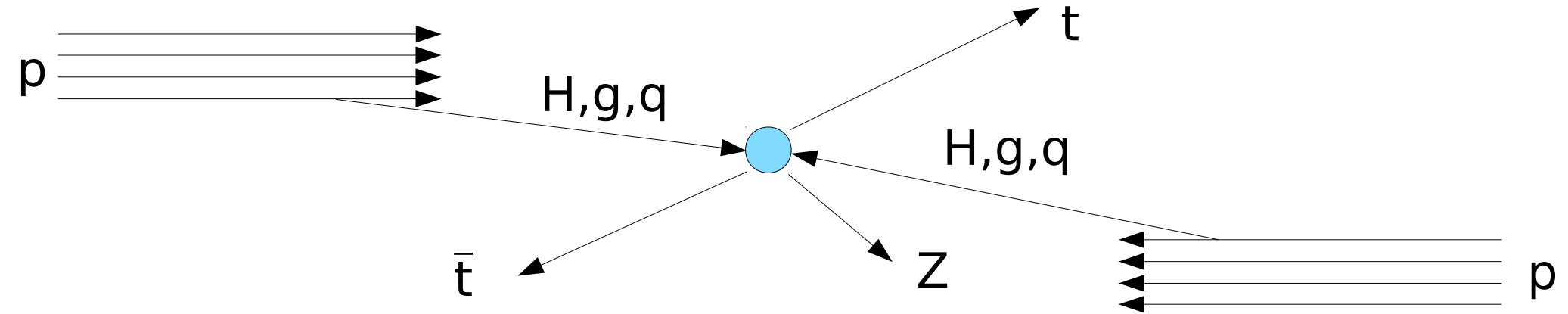
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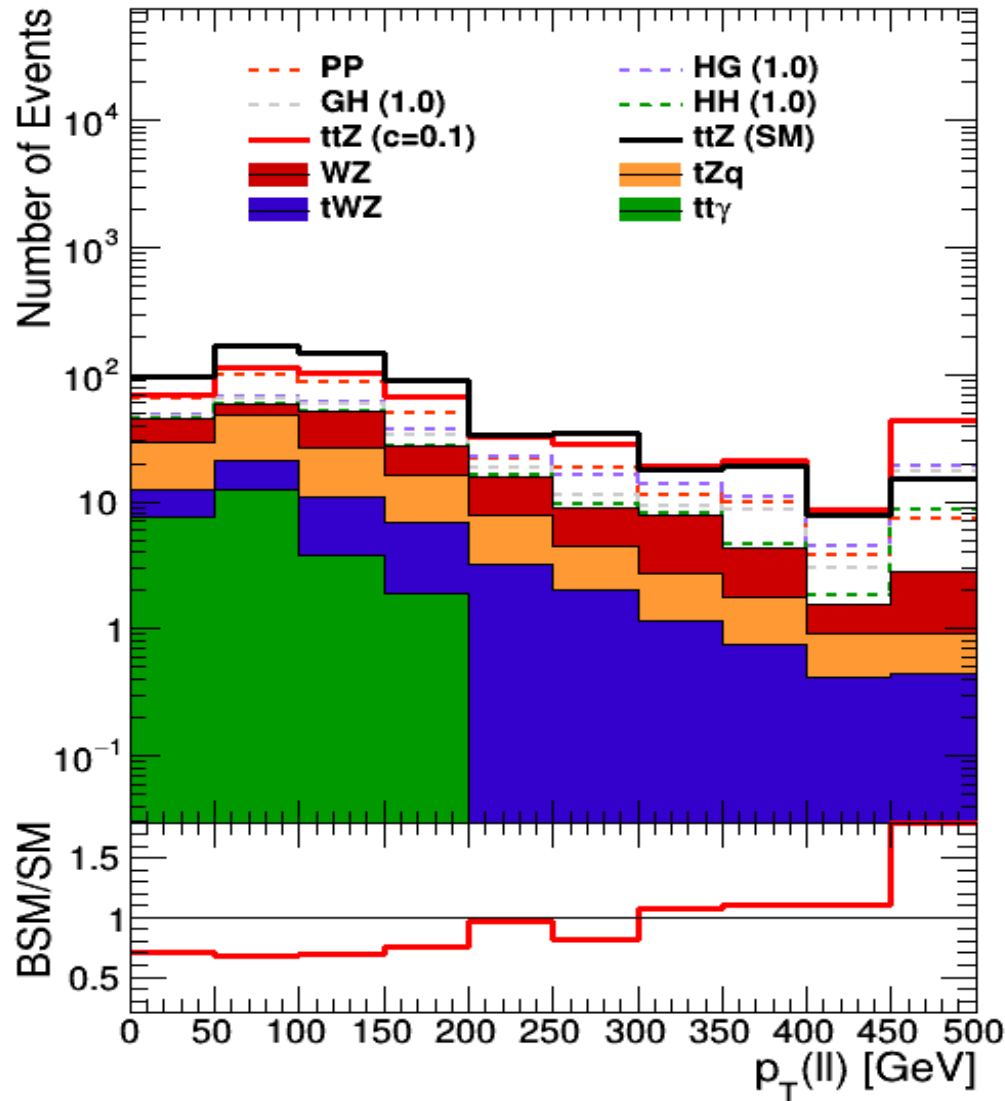


Add: Partial differential crosssections, CMS detector simulation

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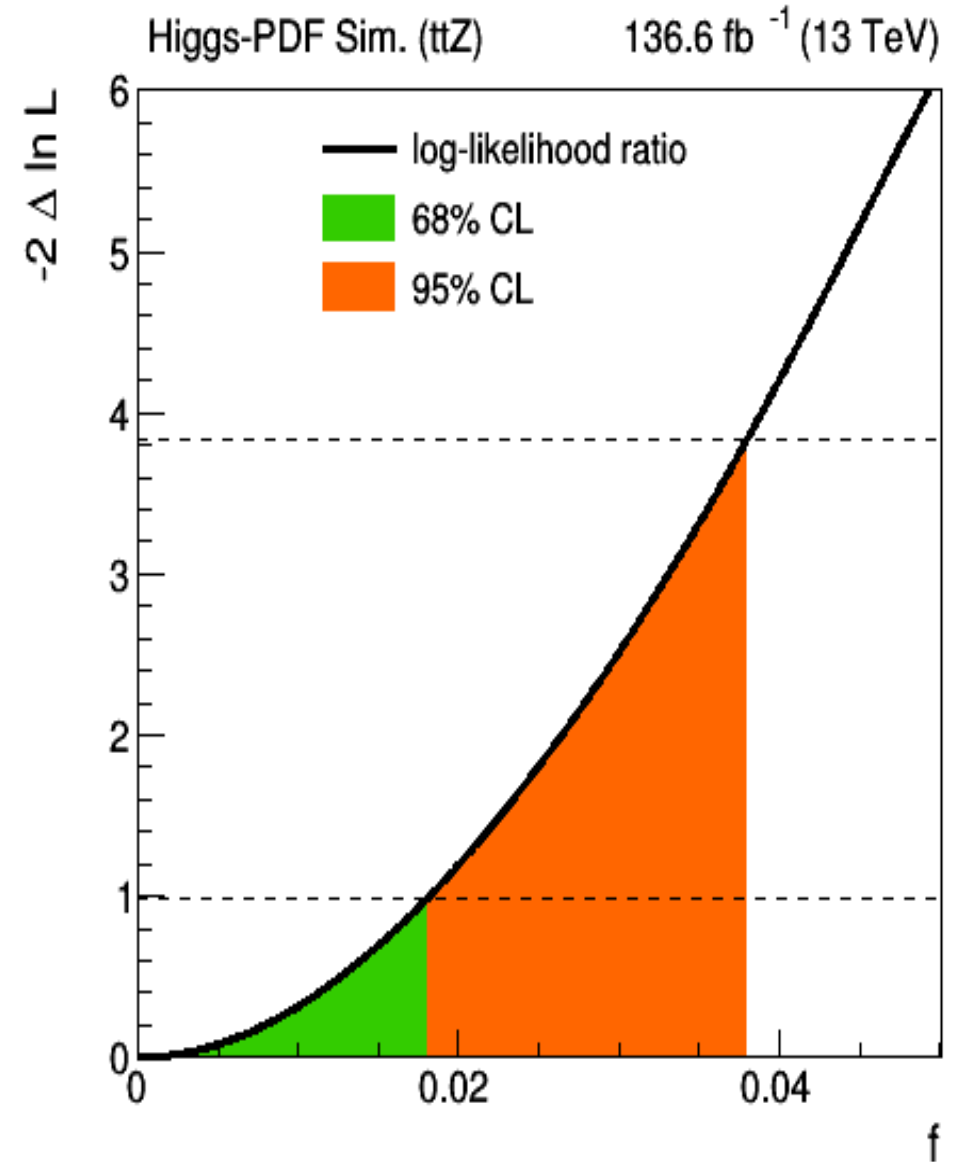
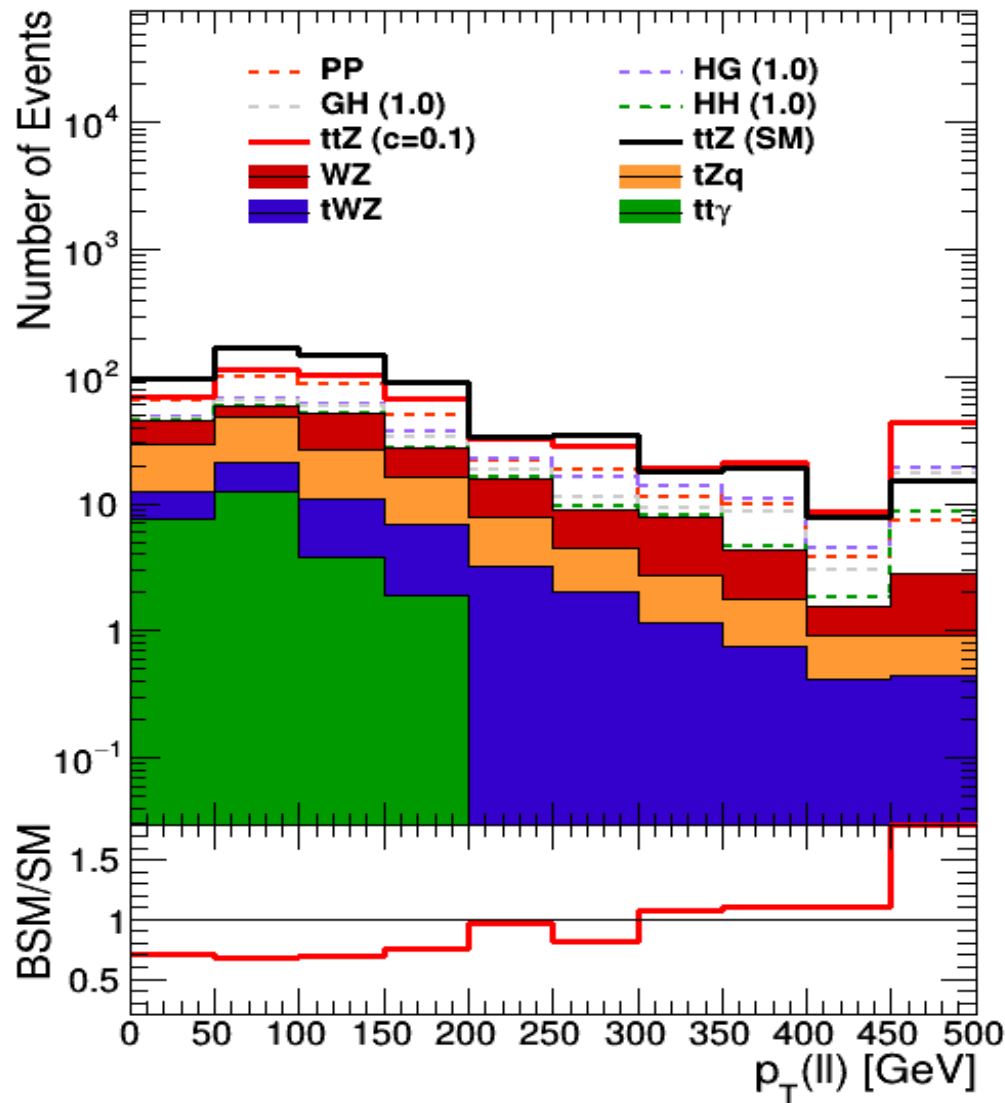


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New physics

-

Qualitative changes

Beyond the standard model

[Maas'15
Maas, Sondenheimer, Törek'17]

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Maas, Sondenheimer, Törek'17]

- Standard model is special
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A toy model

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- Global U(1) custodial (flavor) symmetry

- Acts as (right-)transformation on the scalar field only

$$W_\mu^a \rightarrow W_\mu^a \qquad h \rightarrow \exp(ia) h$$

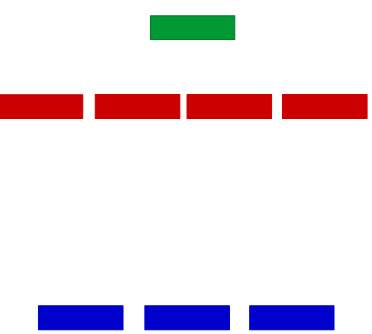
Spectrum

Gauge-dependent
Vector

Mass

0

'SU(3) → SU(2)'

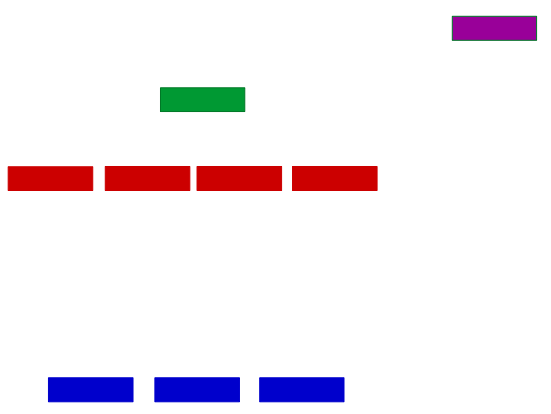
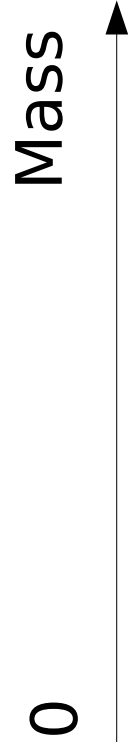


Spectrum

Gauge-dependent

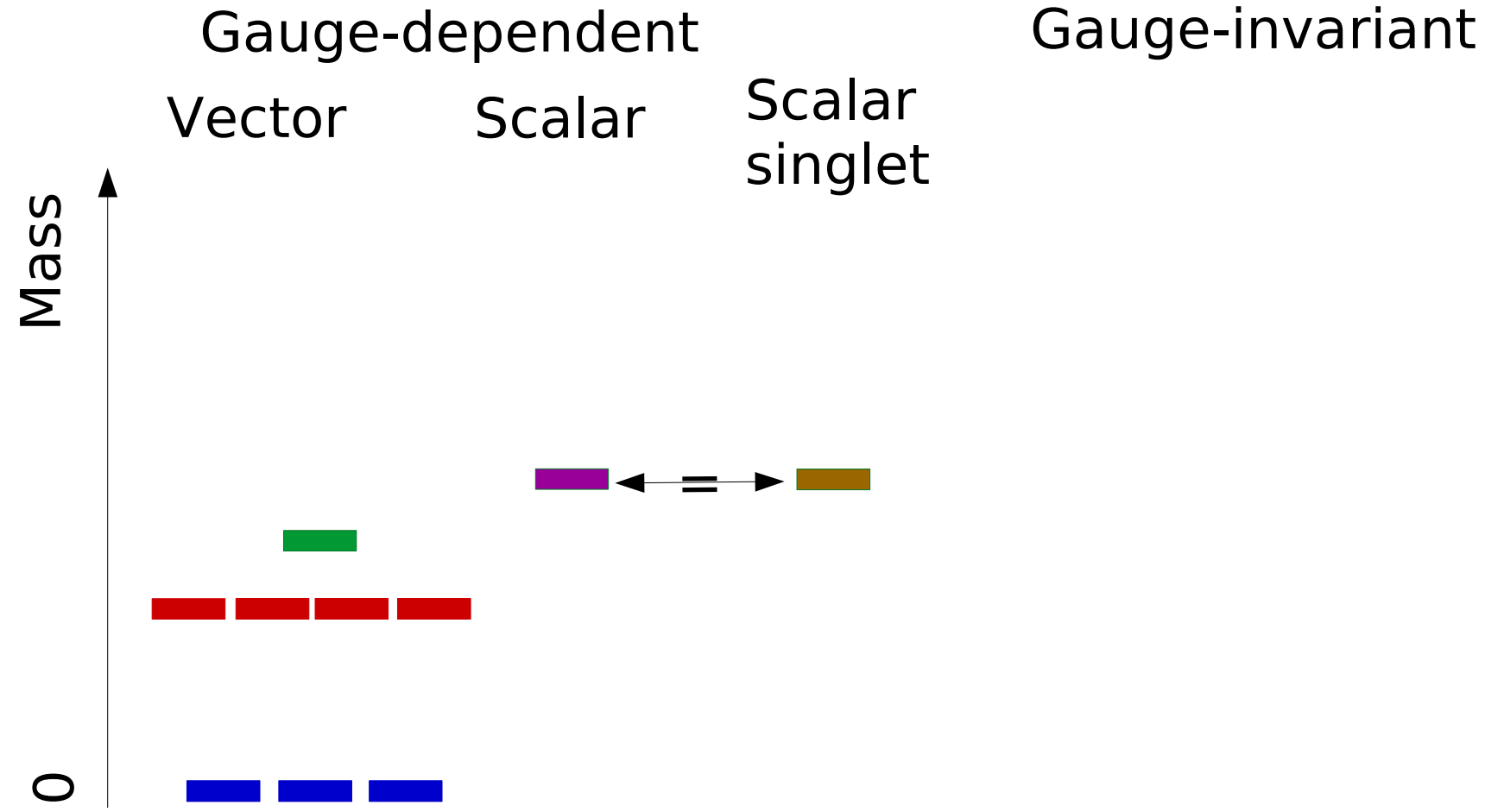
Vector

Scalar



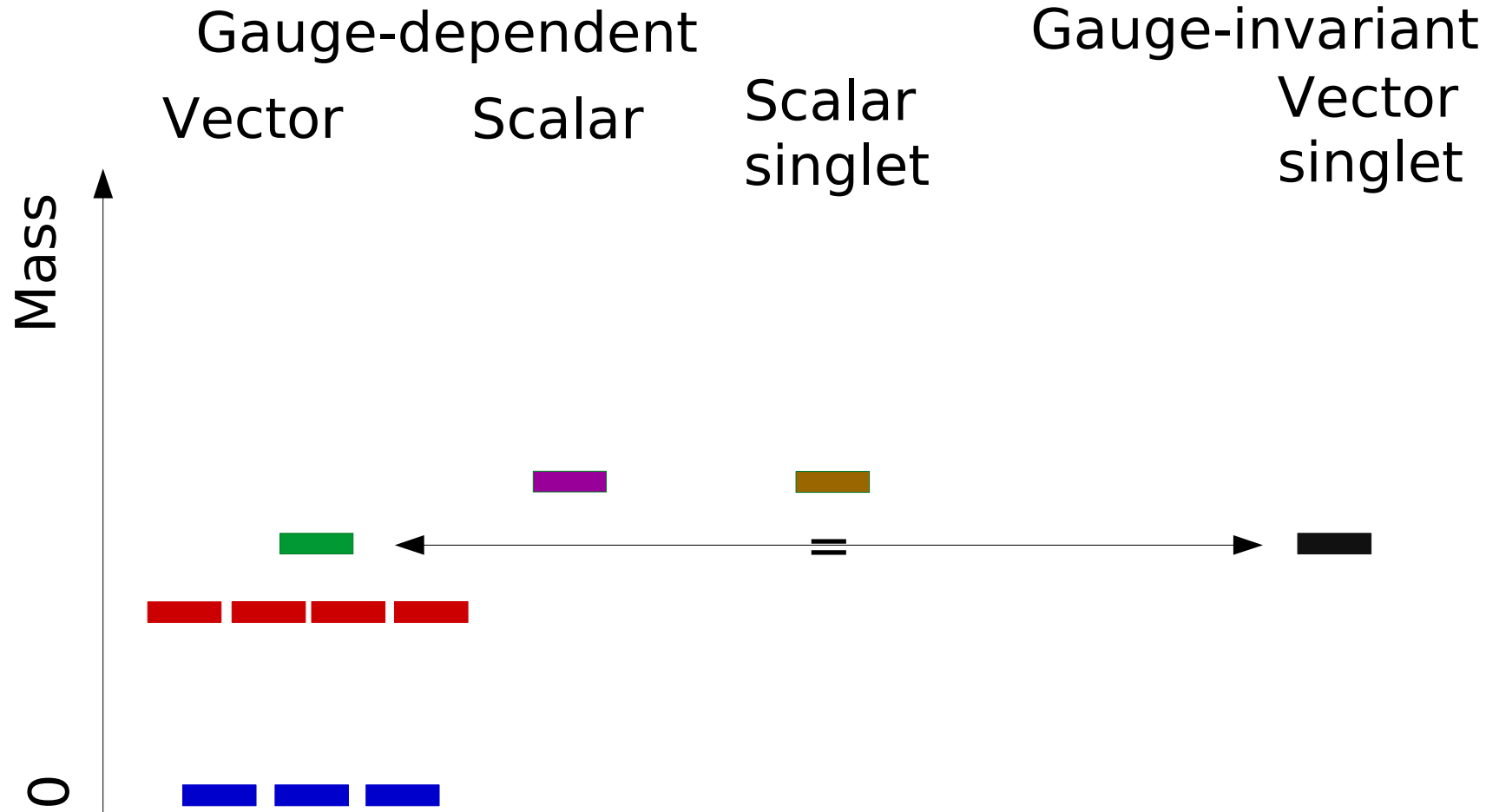
Spectrum

[Maas & Törek'16,'18
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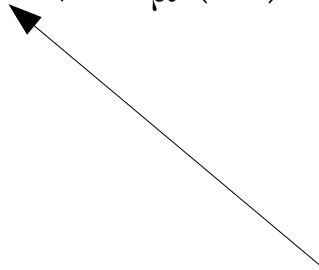
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Matrix from
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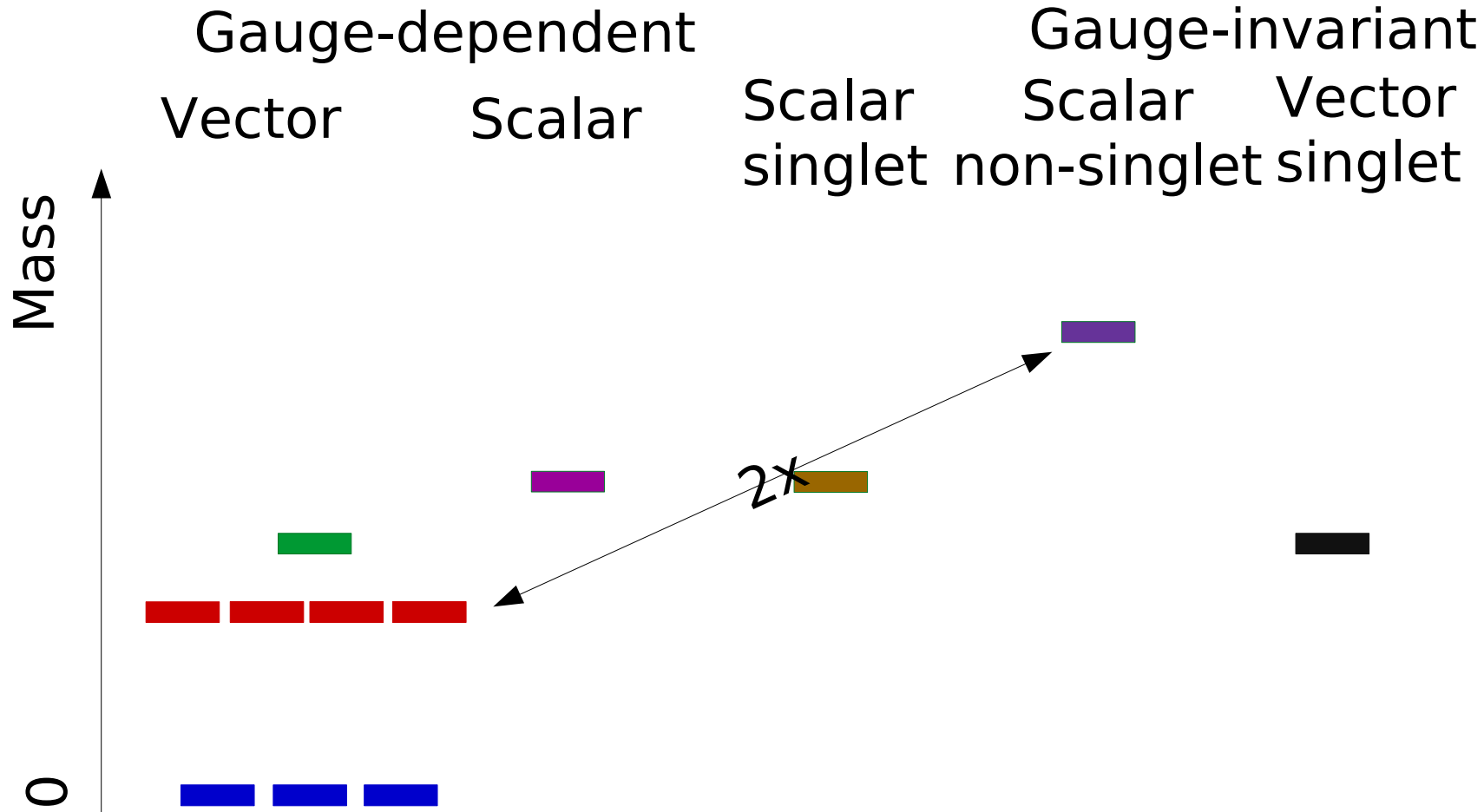
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Only one state remains in the spectrum
at mass of gauge boson 8 (heavy singlet)

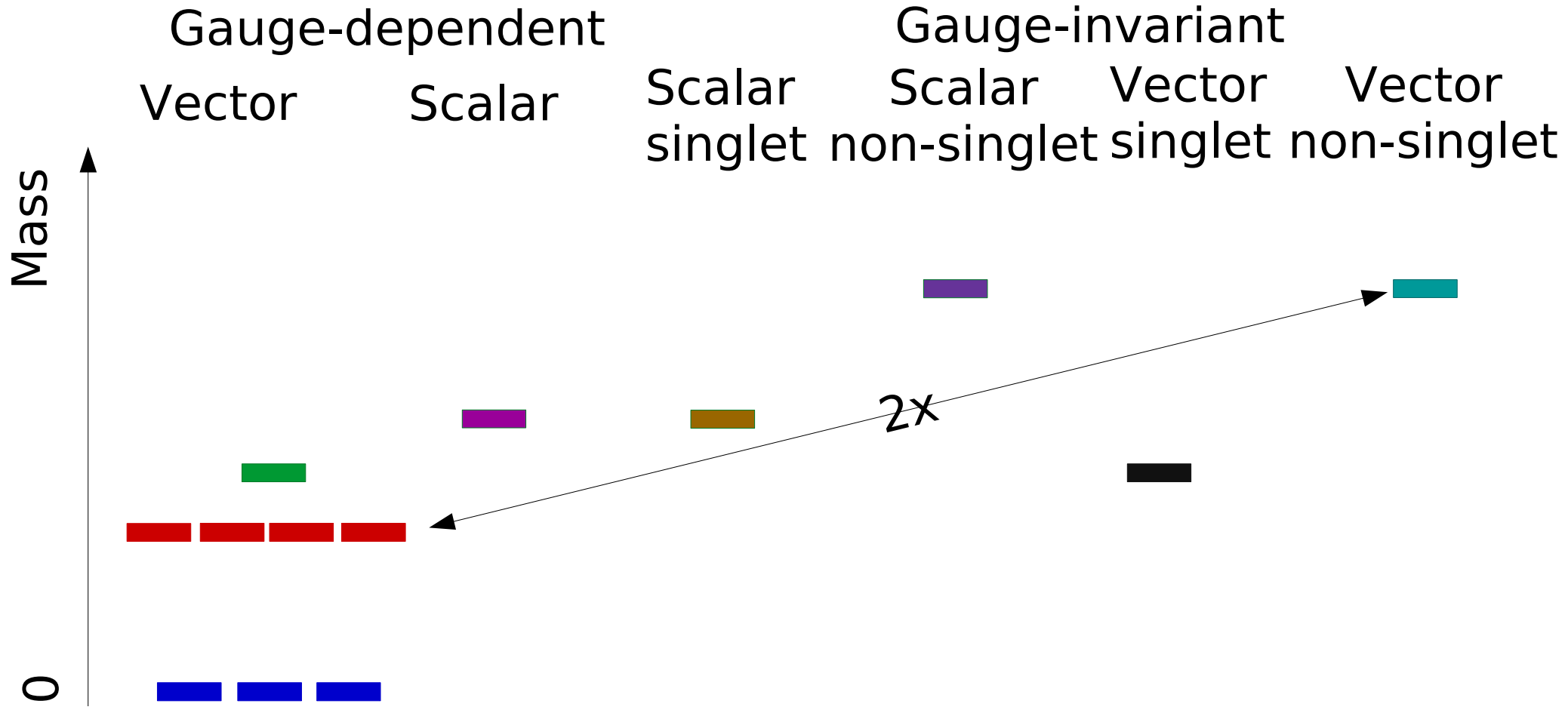
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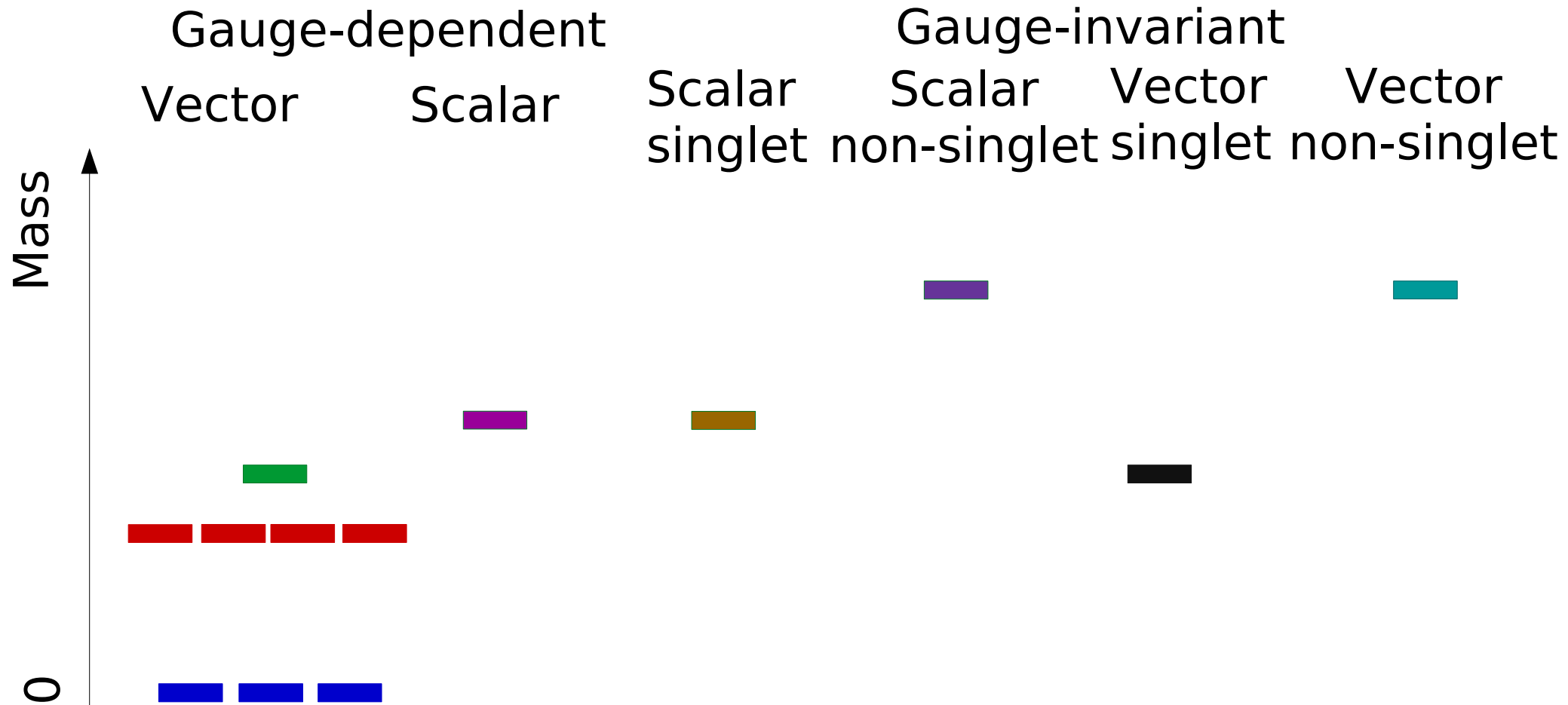
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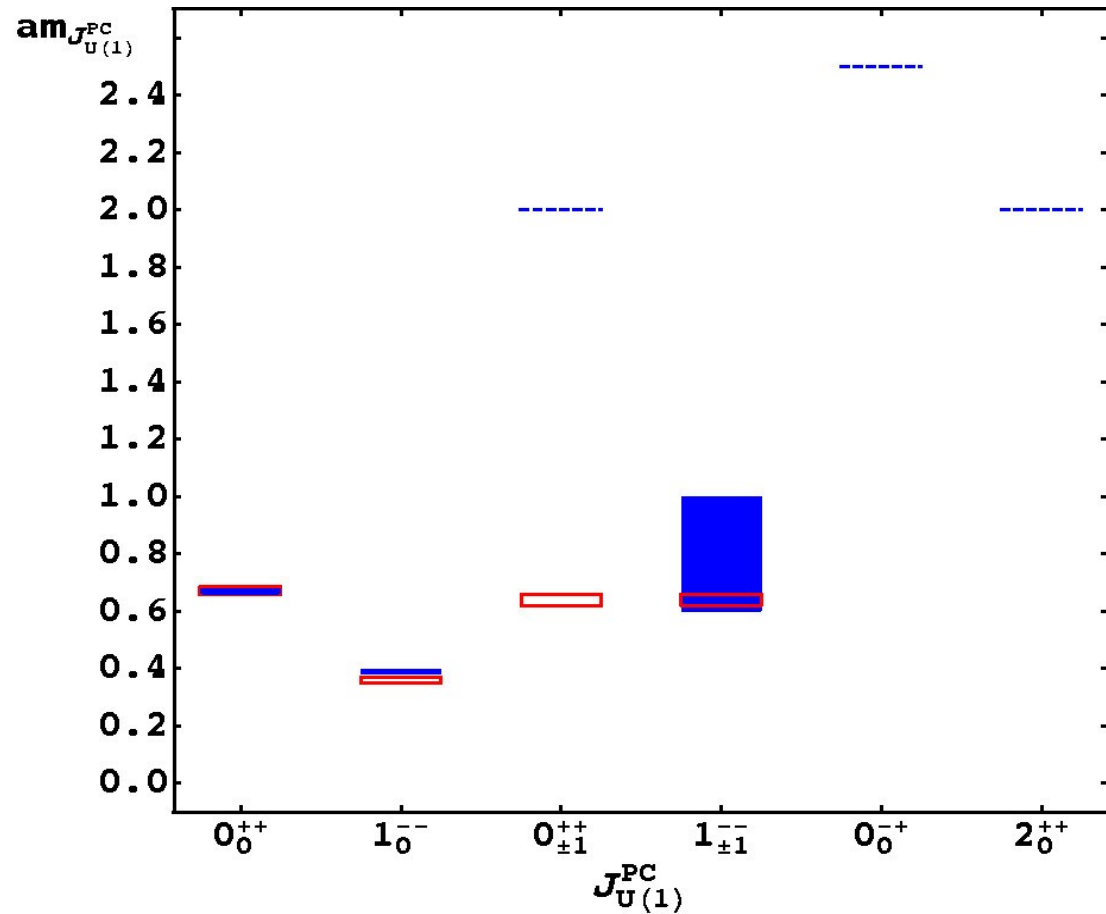


- Qualitatively different spectrum
- No mass gap!

Spectrum

[Maas & Törek'16,'18
Maas, Sondenheimer & Törek'17]

Gauge-invariant
Scalar Scalar Vector Vector
singlet non-singlet singlet non-singlet

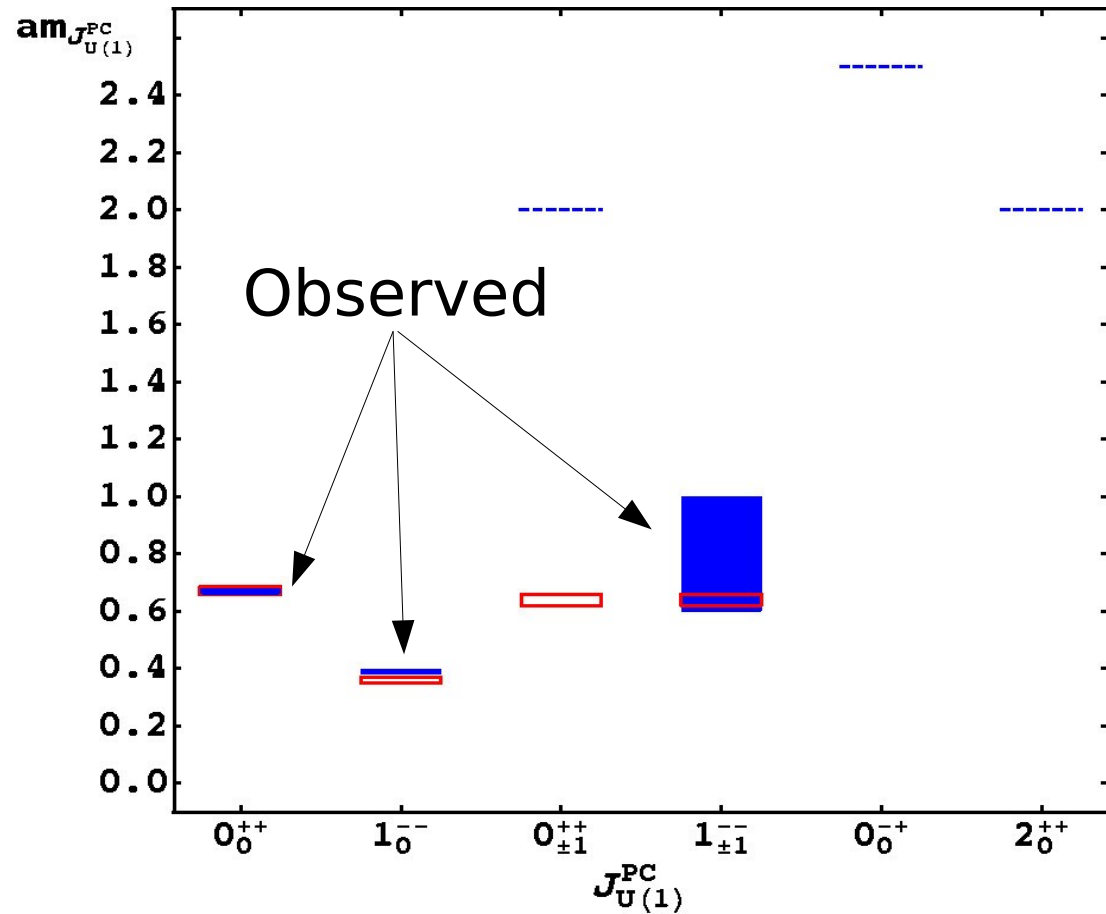


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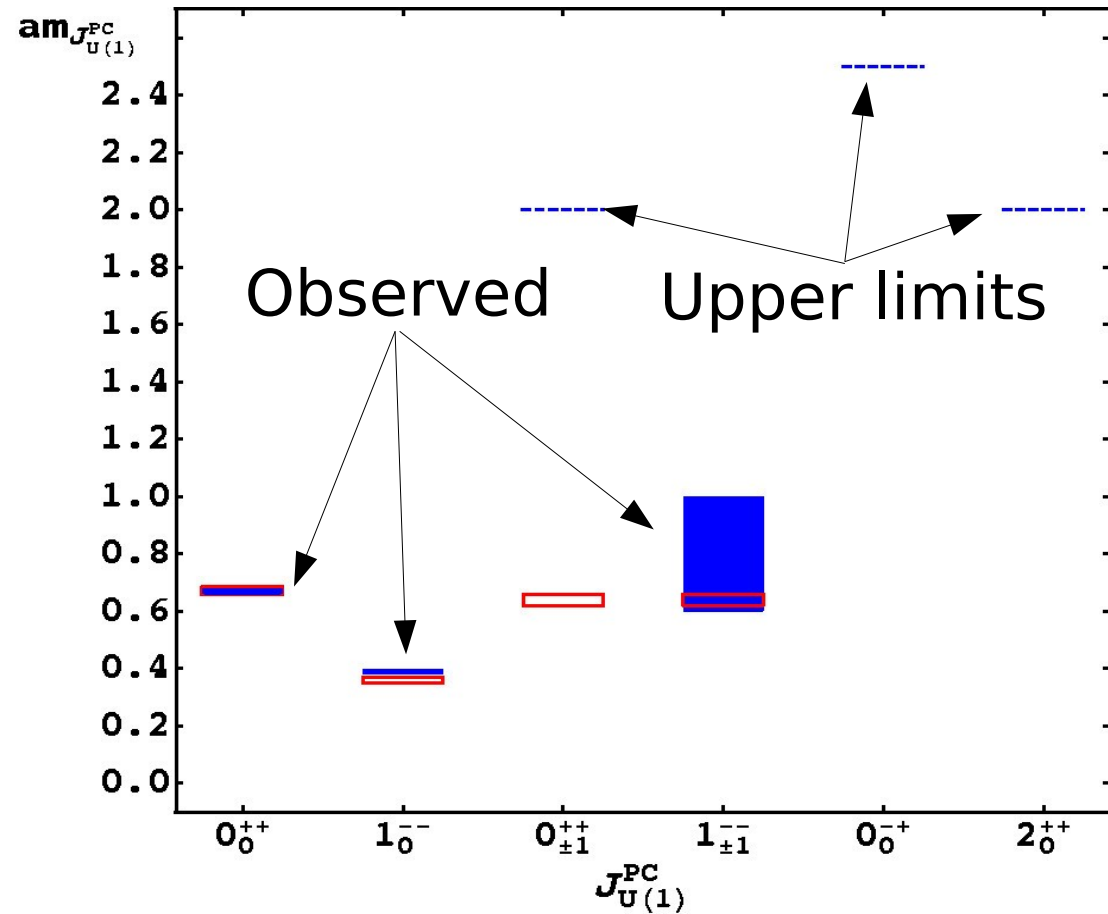


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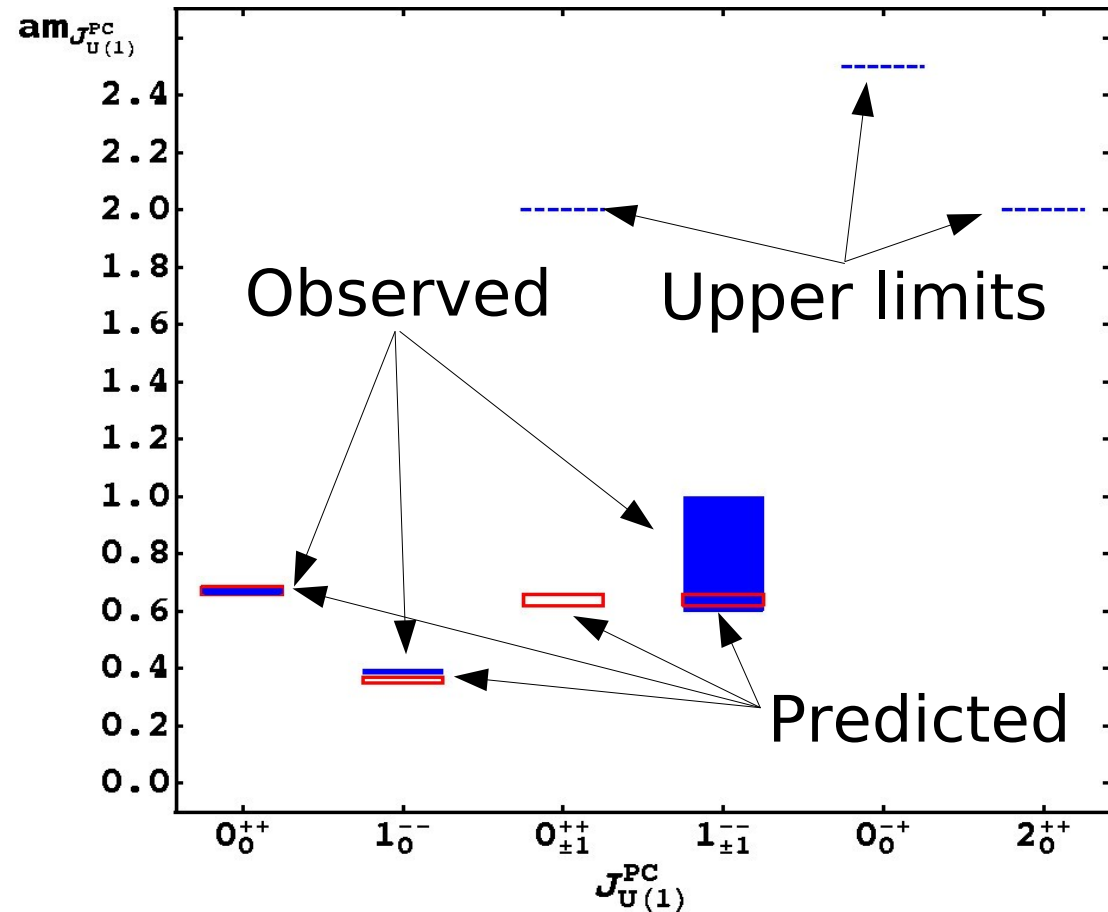


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- Qualitatively different spectrum
- Results in agreement with analytic predictions

Experimental consequences

Experimental consequences

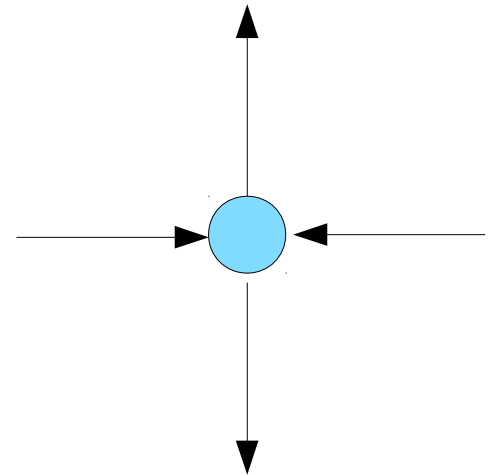
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- Add fundamental fermions

Experimental consequences

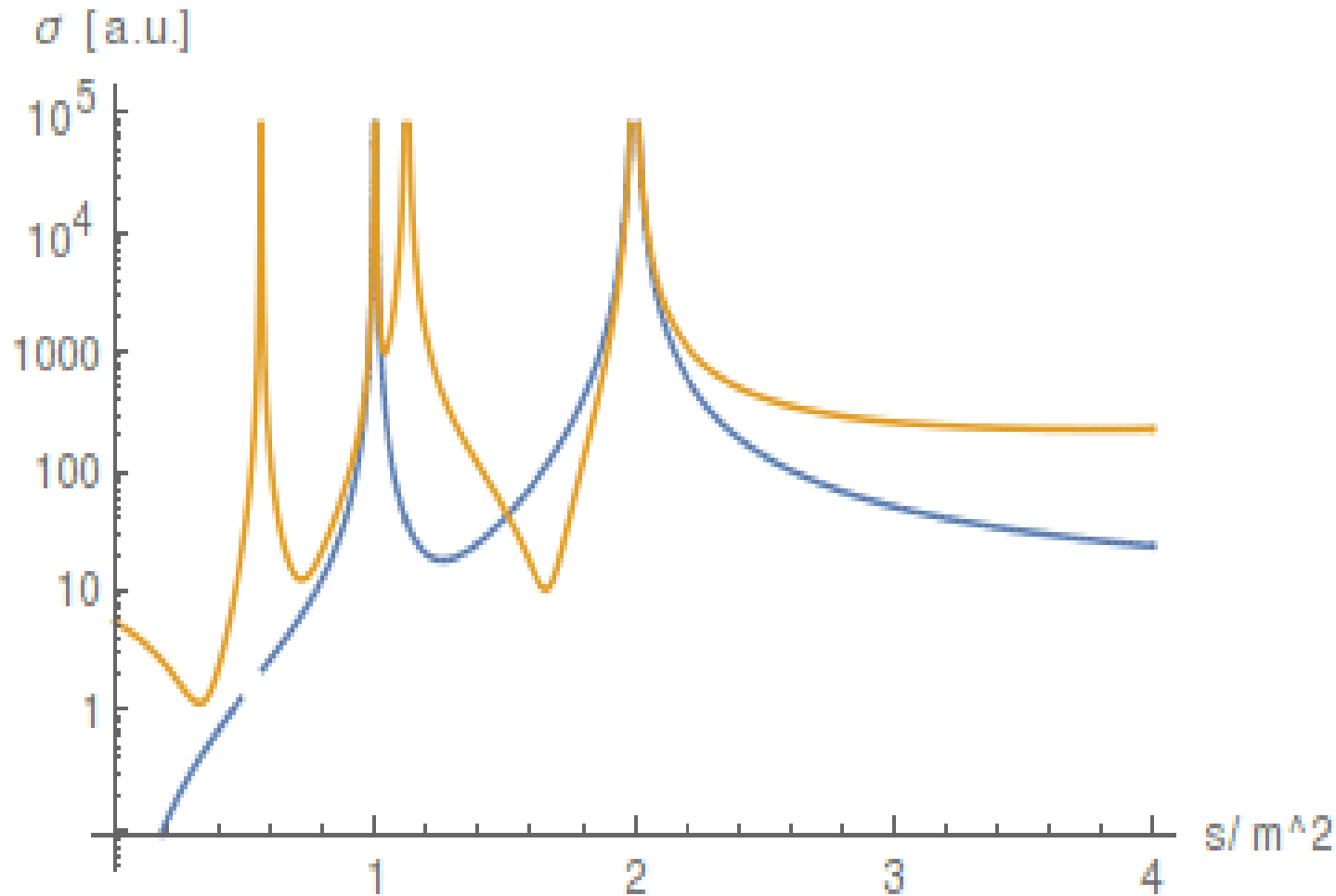
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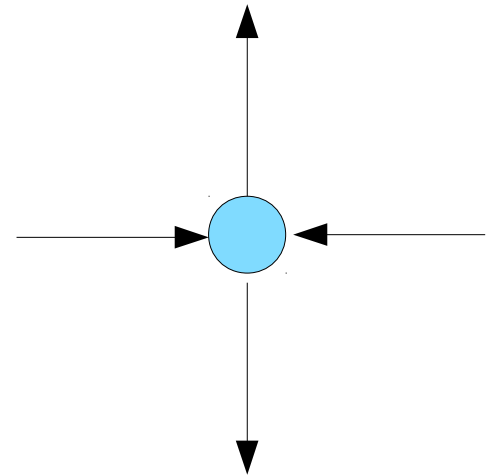
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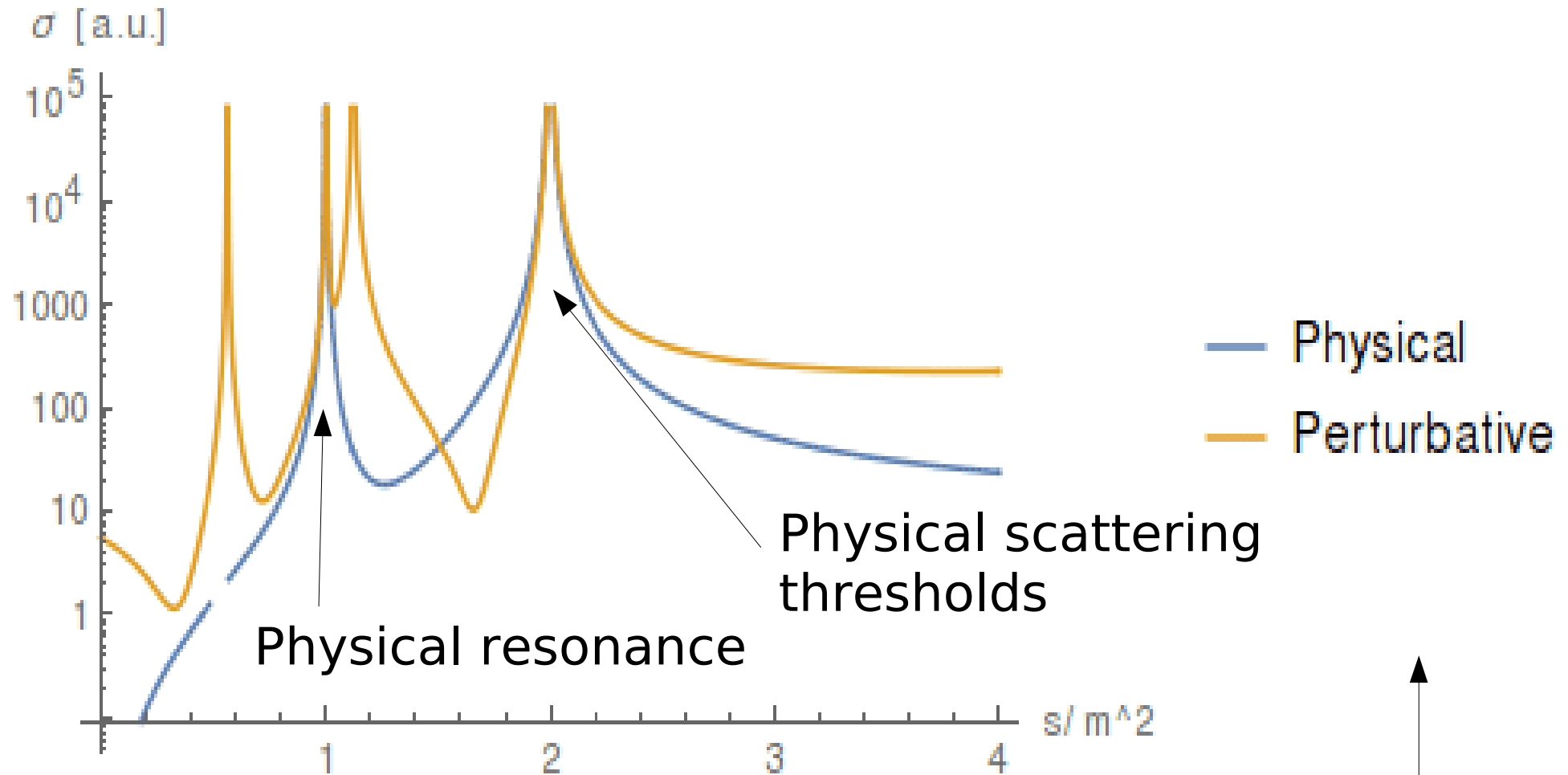
— Physical
— Perturbative

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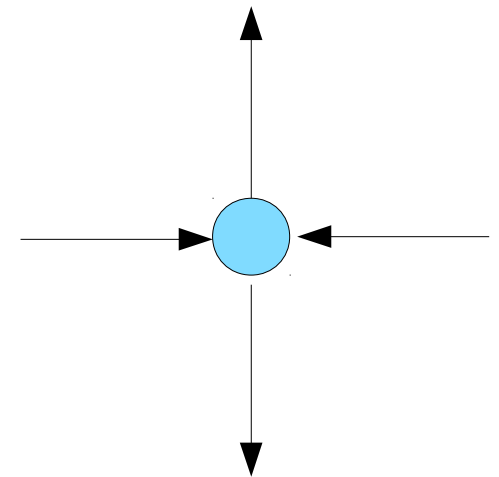


Experimental consequences

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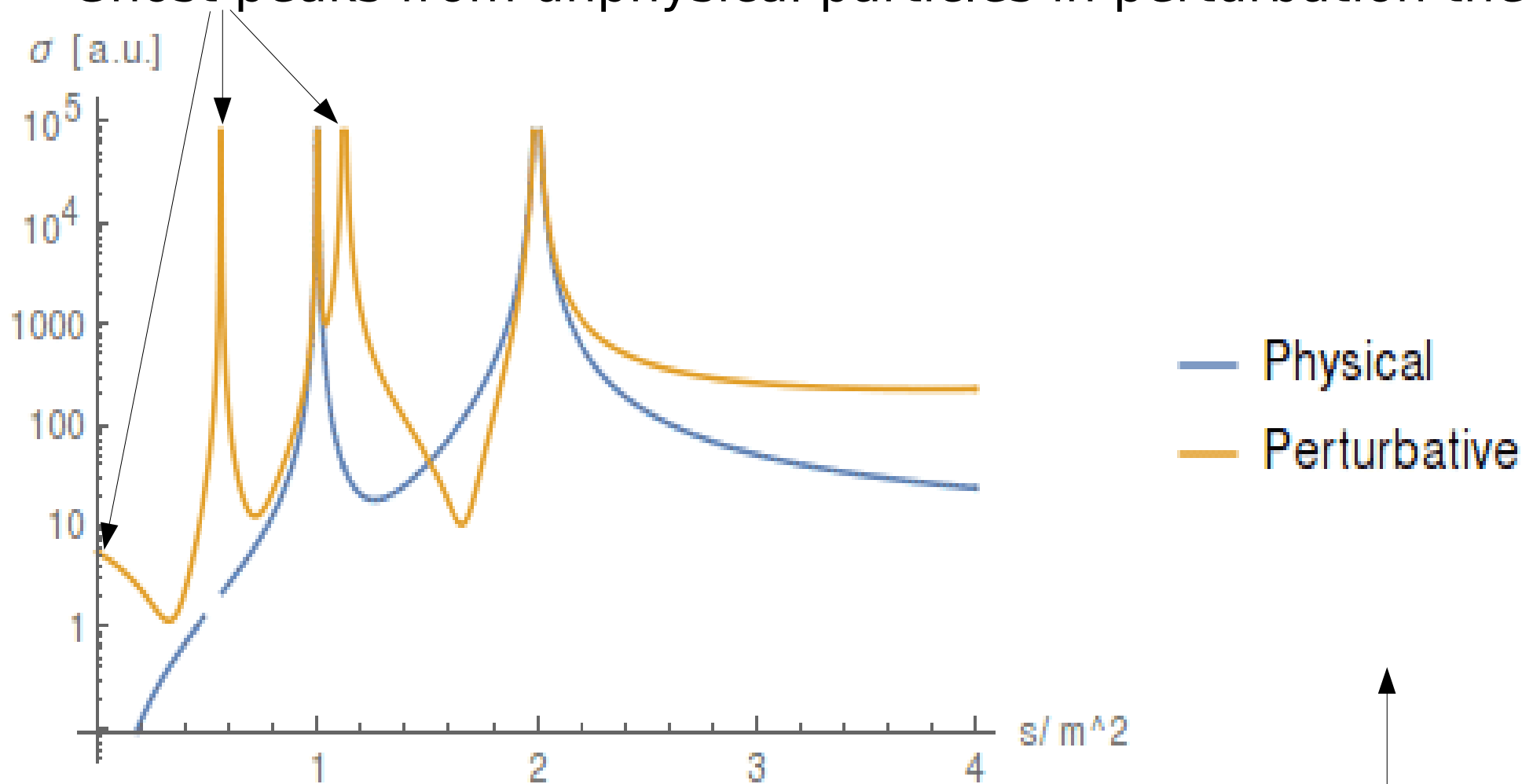
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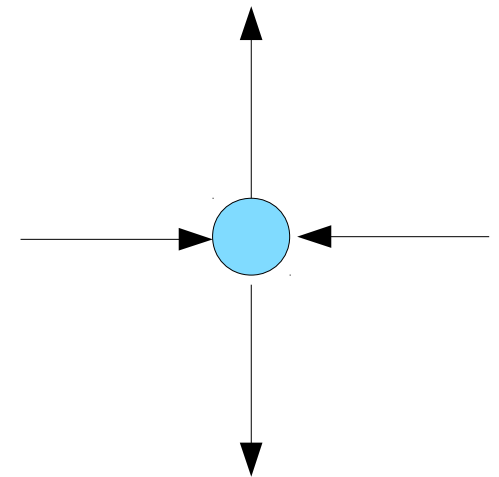
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Ghost peaks from unphysical particles in perturbation theory



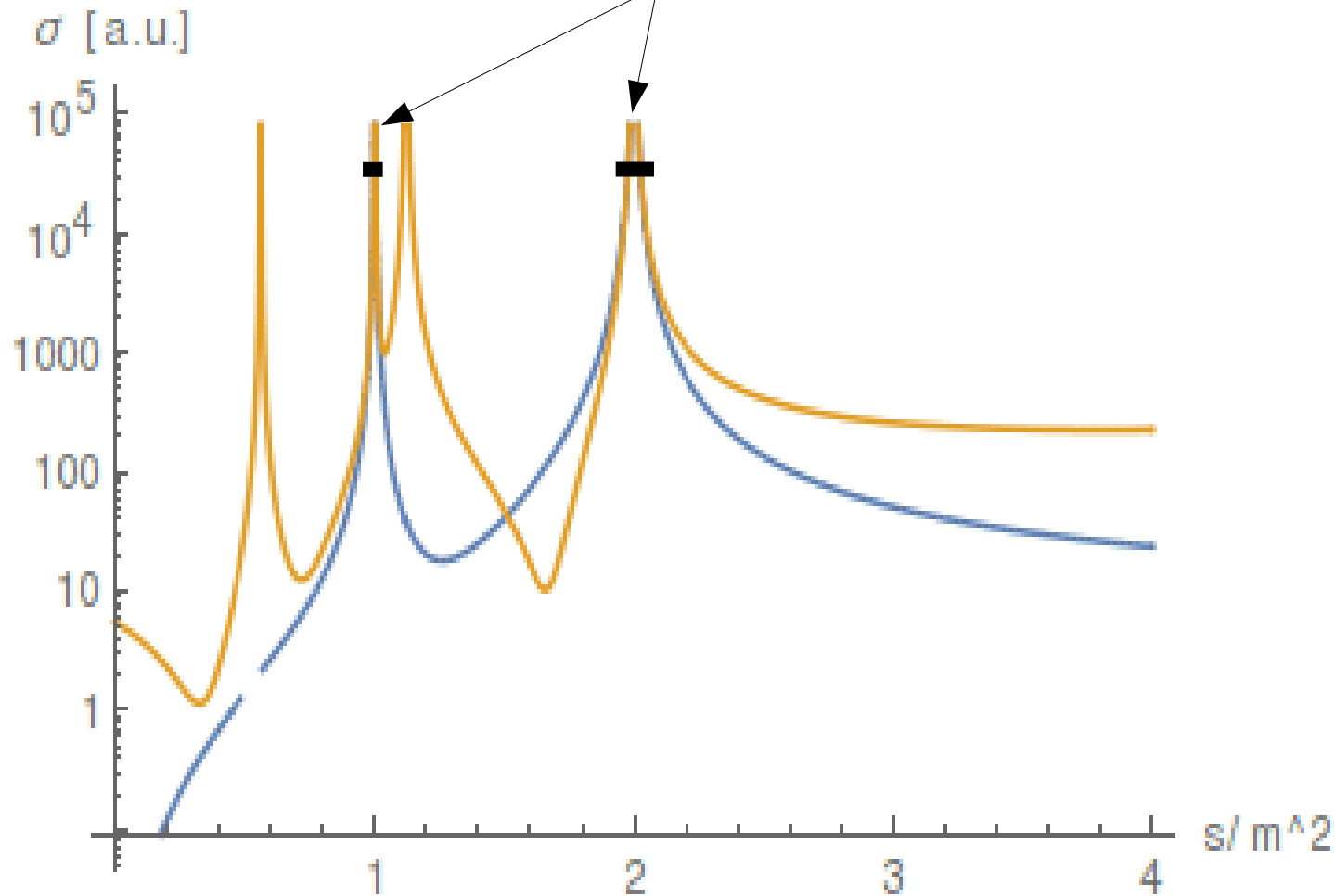
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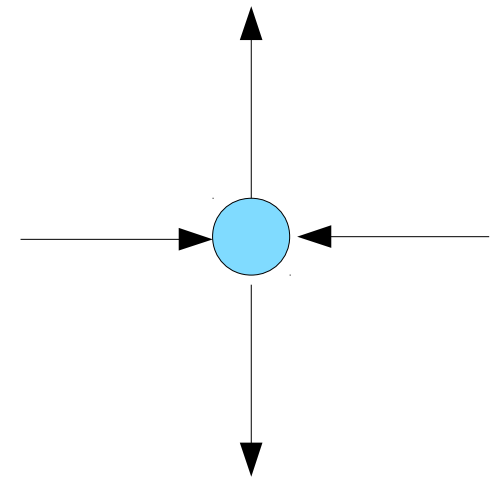
Experimental consequences

[Maas & Törek'18
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Close to true structures identical!



- Add fundamental fermions
- Bhabha scattering



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