

Nanoscience : Fundamentals and basic properties

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<http://physik.uni-graz.at/~uxh>

ASON-1, 19.-23.09.2010, Dubrovnik, Croatia



*Nanometer
is the „ruler“ at the atomic scale*

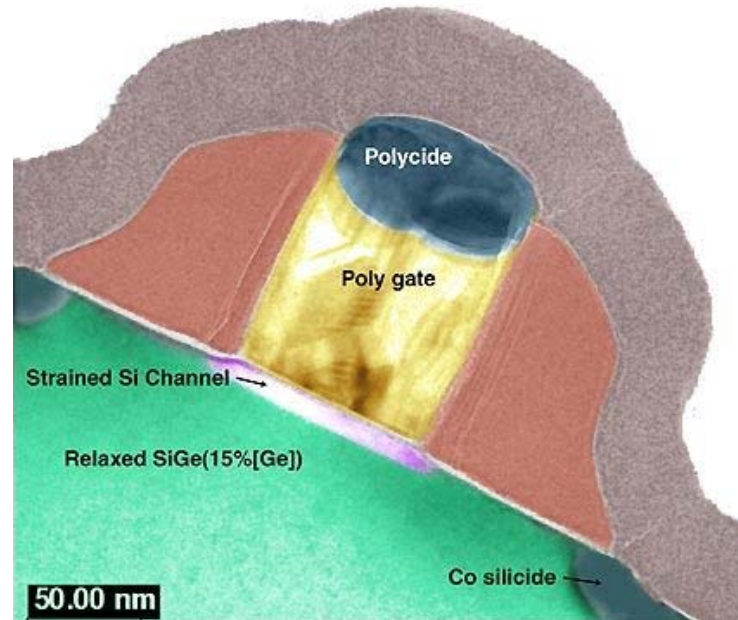
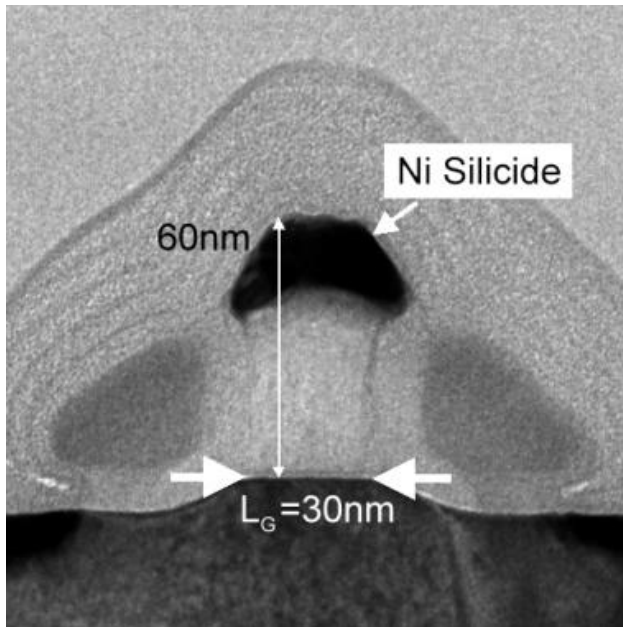
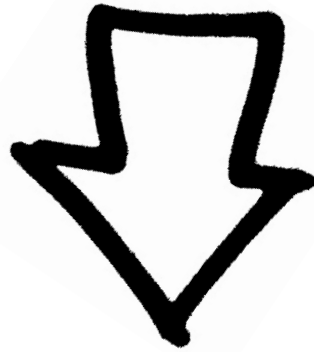


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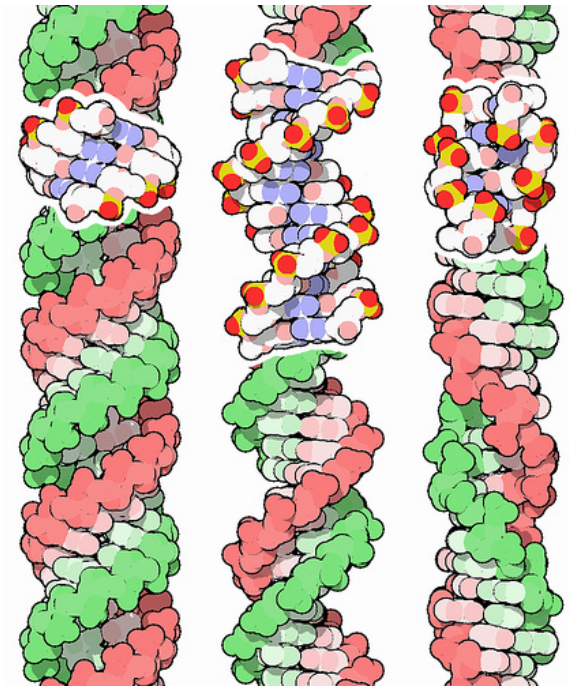
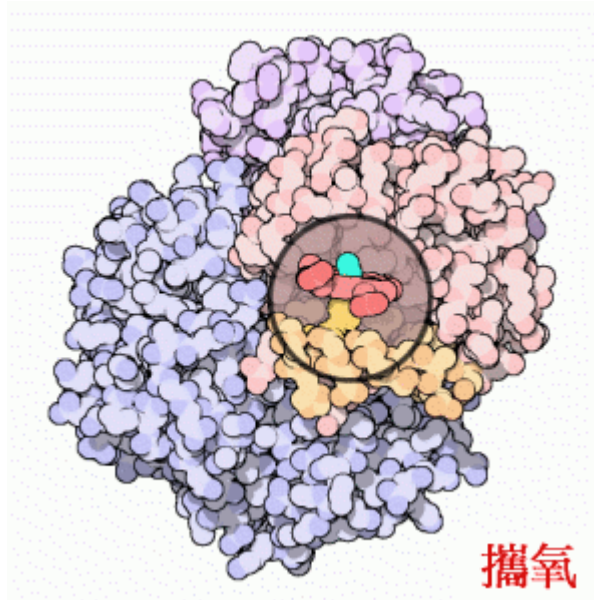
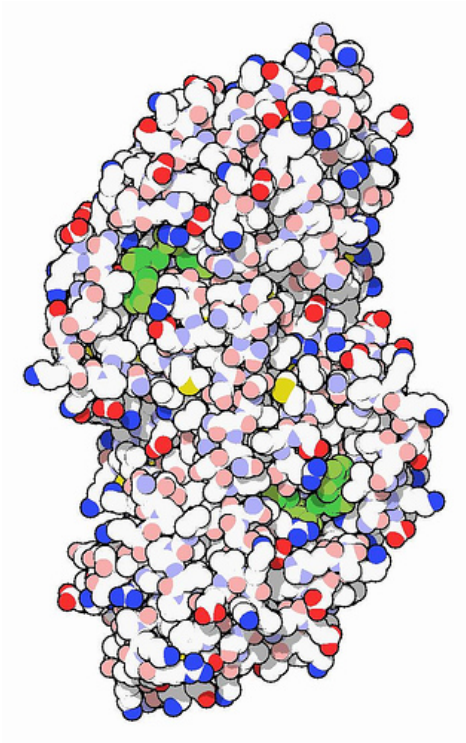


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*Technology is approaching nanoscale from „above“
... top – down approach*

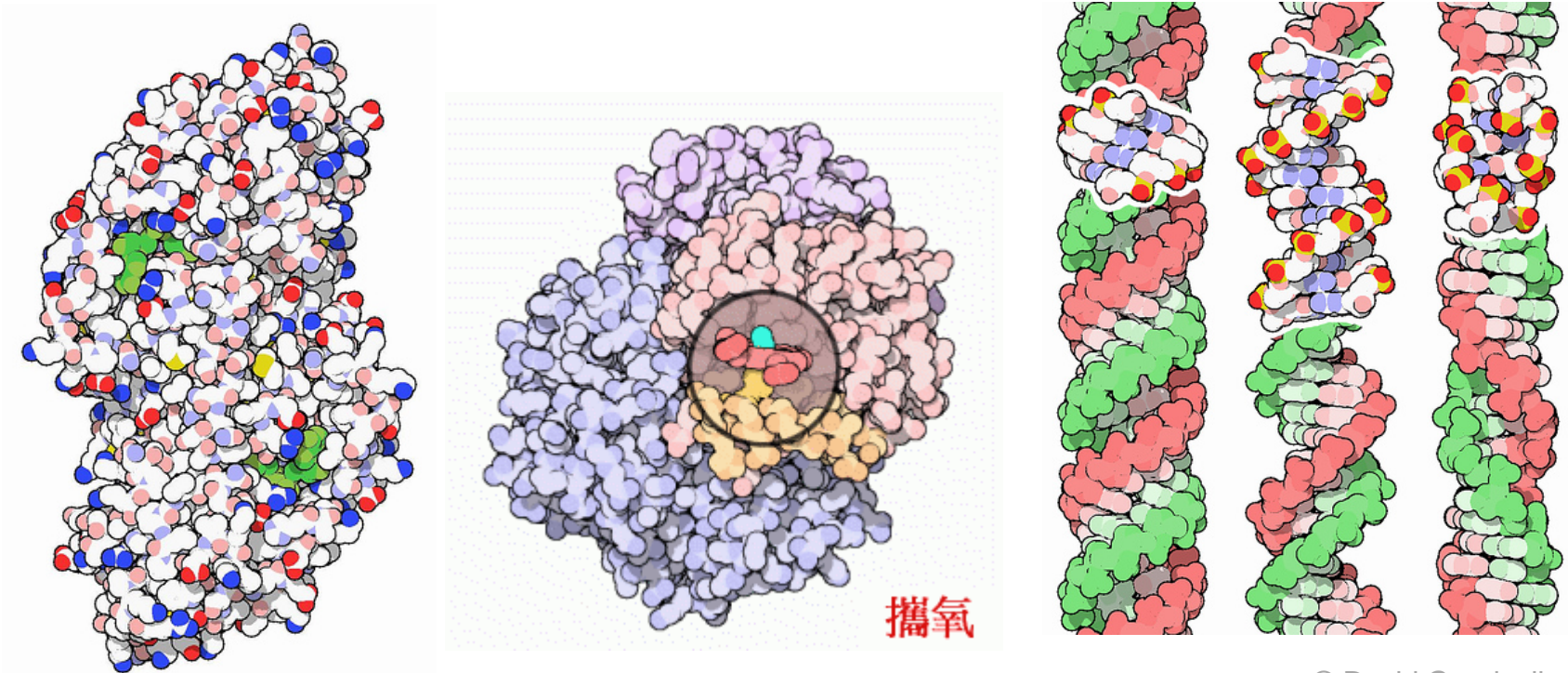


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Nature uses atoms as building blocks for (bio)molecules

... bottom – up approach



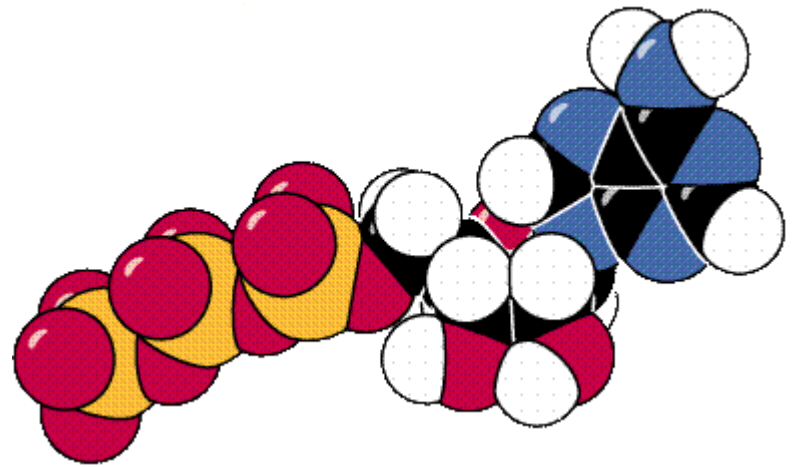
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„There is plenty of room at the bottom“

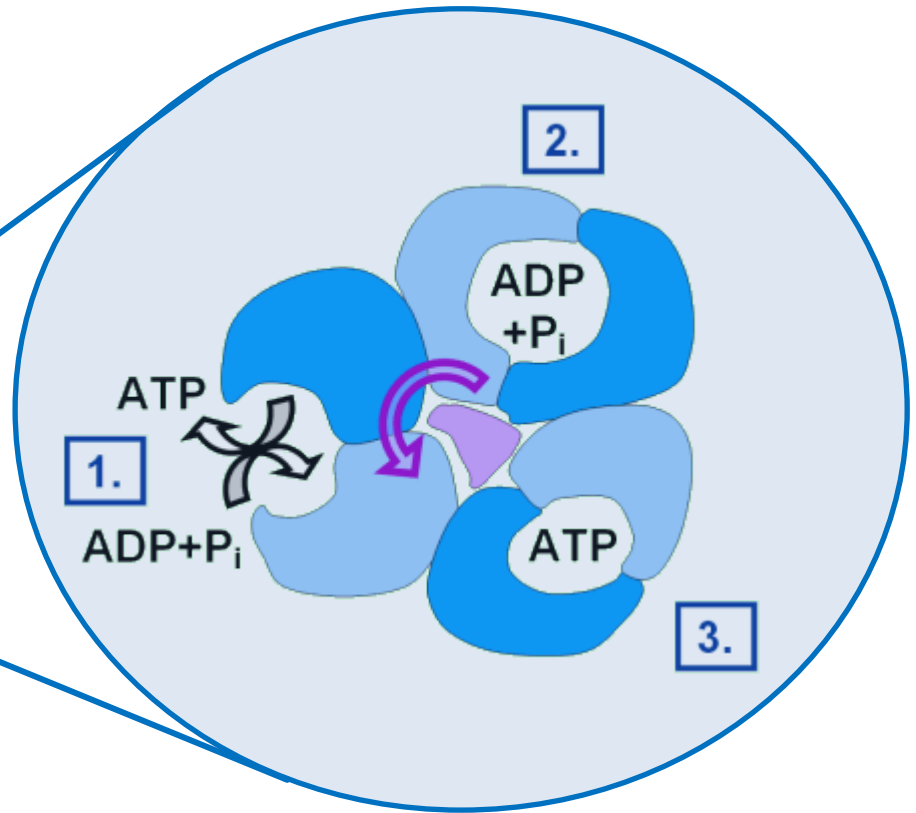
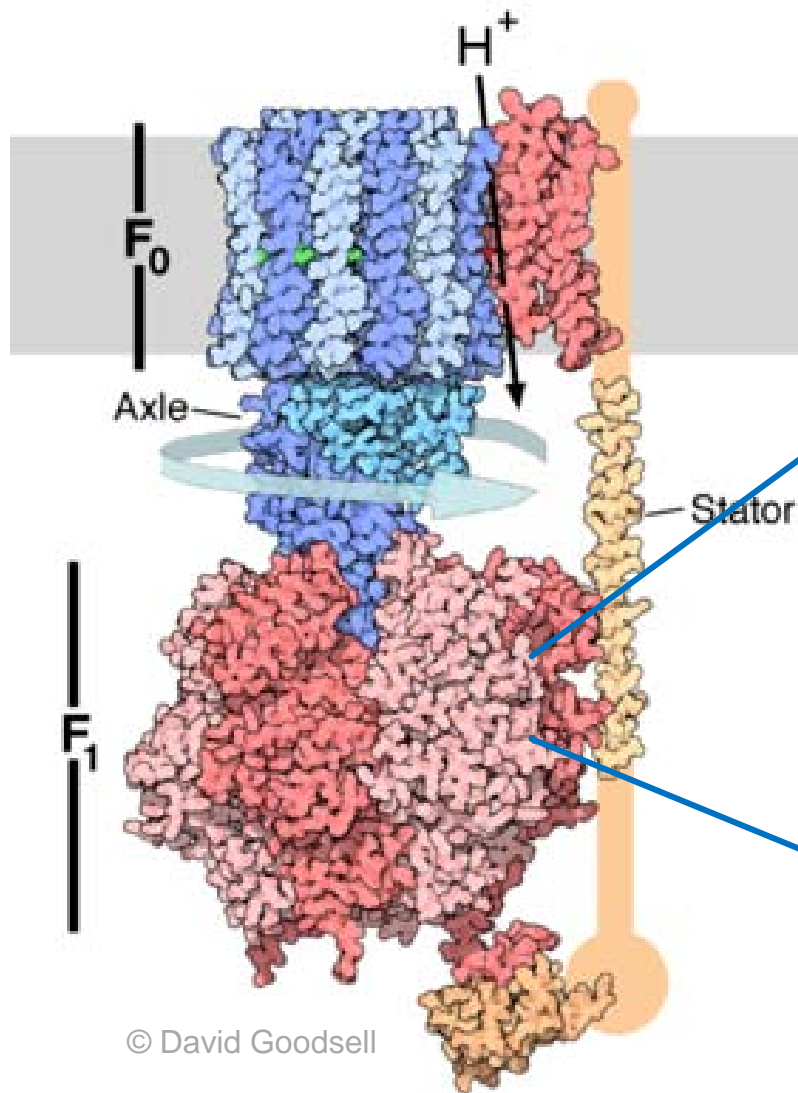
Richard Feynman, 1959

I now want to show that there is plenty of room.

I will not now discuss how we are going to do it, but only what is possible in principle — in other words, what is possible according to the laws of physics.



Example : ATP synthase



Proton pump H⁺ drives “nanomotor” that drives ADP + P_i → ATP

Agenda

What I will do in this lecture ...

Electrons in solids

Confinement : from 3D to 0D

Coulomb effects at the nanoscale

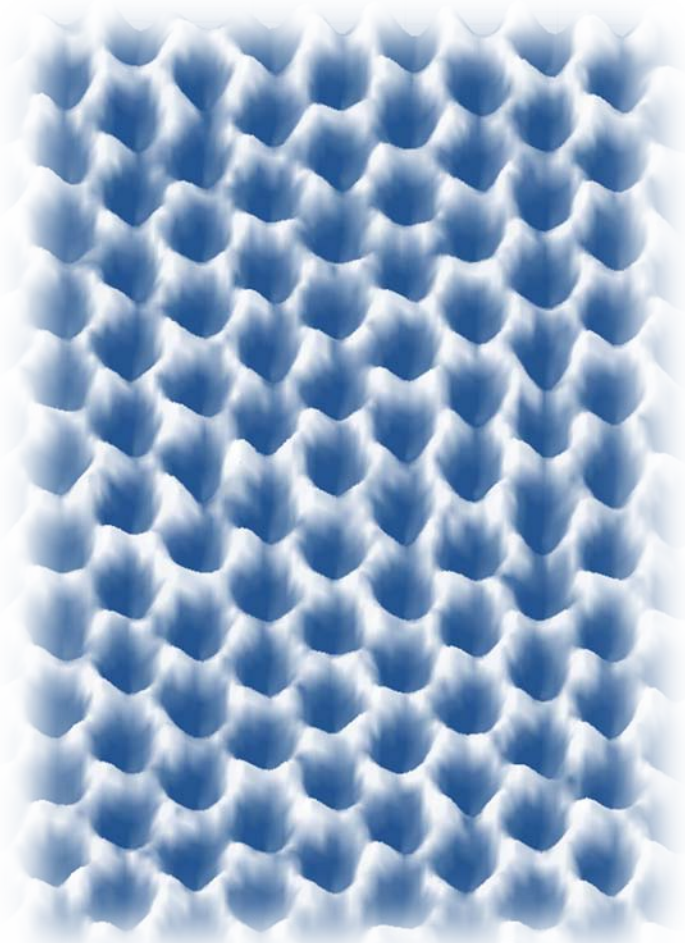
How quantum are nanostructures ?

*Single nanosystems, optics at the nanoscale, nanomagnetism and spintronics,
forces, heat & fluids at the nanoscale*

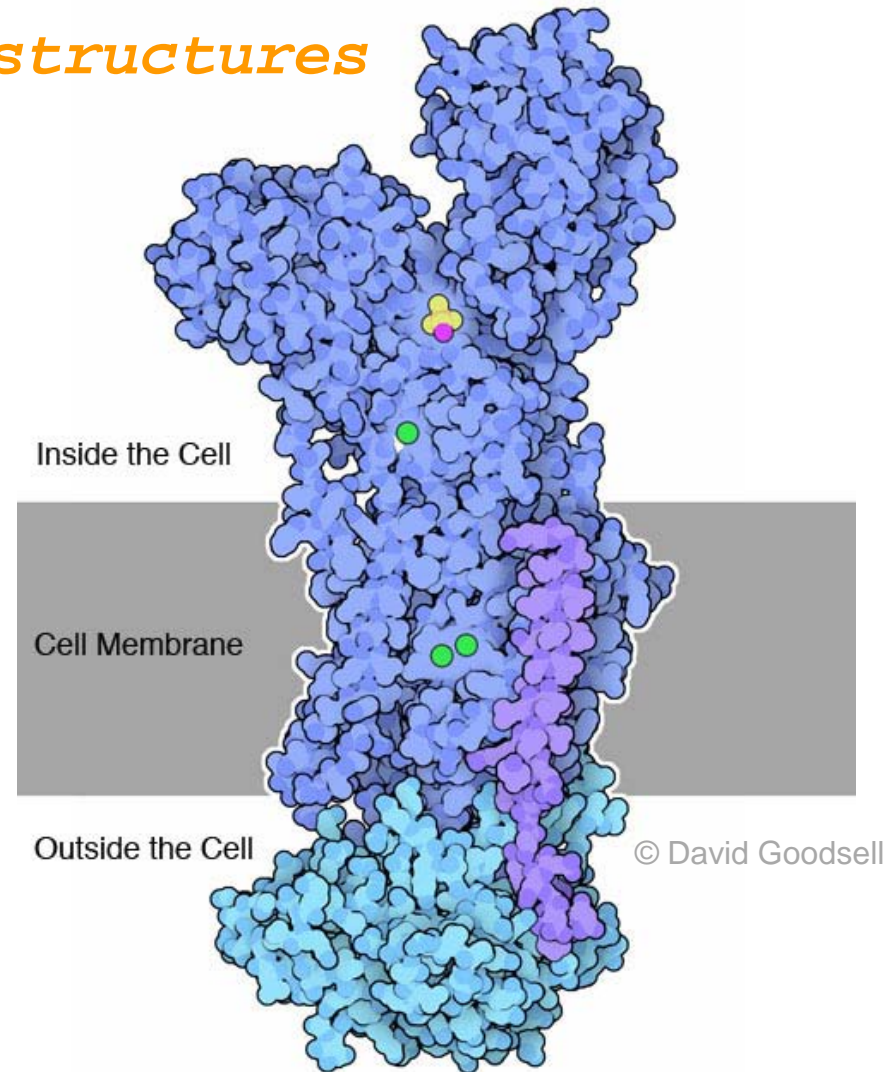
My scientific background ...

*I am a theoretical physicist working in condensed matter physics, interested in
plasmonic nanoparticles, semiconductor quantum dots & ultracold atoms*

Charge transfer in nanostructures



*(Nano)crystals:
electrons delocalized
information transfer through electrons*



*(Bio)molecules:
electrons localized in bonds
information transfer through ions*

Quantum mechanics: Free particle

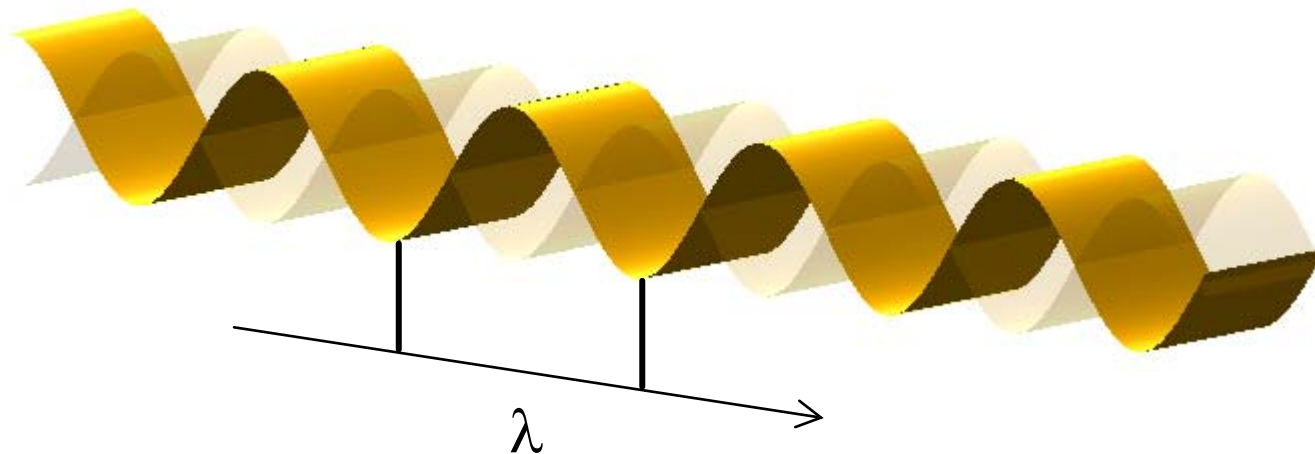
Schrödinger equation for free particle

$$-\frac{\hbar^2 \nabla^2}{2m} \psi(x) = E \psi(x)$$

de Broglie wavelength $\lambda = h / p$

High momenta (energies) correspond to small wavelengths

$$\psi(x) = e^{i k x}, \quad p = \hbar k = \frac{h}{\lambda}$$



Quantum mechanics: Free particle

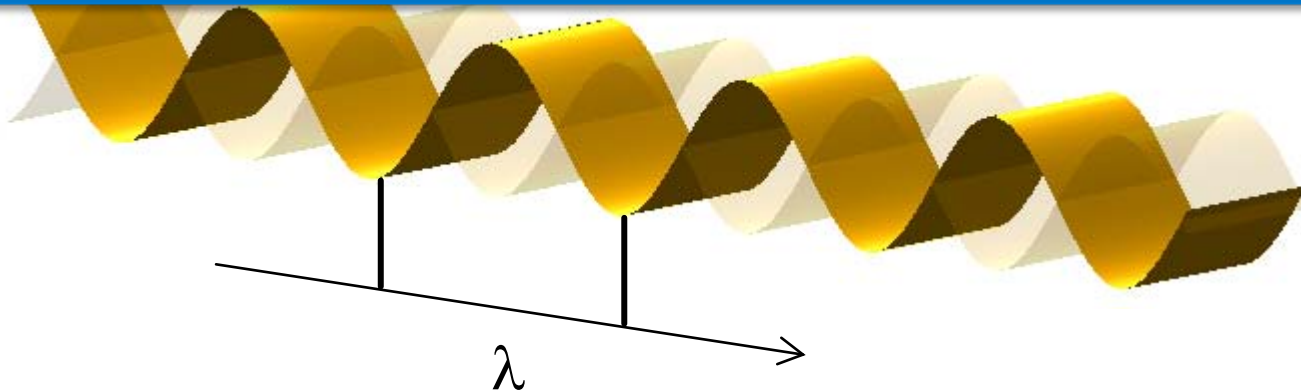
Schrödinger equation for free particle

$$-\frac{\hbar^2 \nabla^2}{2m} \psi(x) = E \psi(x)$$

Finite differences

Coupling to left and right „neighbours“

$$\nabla^2 \psi(x) \approx \frac{\psi(x + \Delta x) - 2\psi(x) + \psi(x - \Delta x)}{(\Delta x)^2}$$



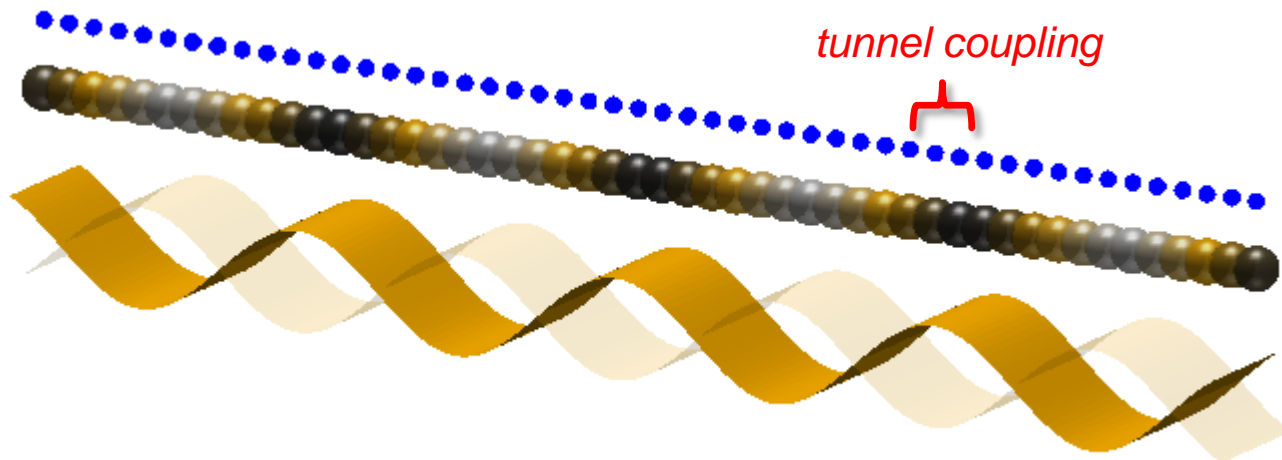
Tight binding model

Wavefunction of electron in a linear chain of atoms

$$\Psi(x) = \sum_{\ell} C_{\ell} \underbrace{\phi(x - \ell a)}_{\text{localized atomic orbital}} = \sum_{\ell} \underbrace{e^{ik\ell a}}_{\text{plane wave modulation}} \phi(x - \ell a)$$

Tight-binding model for tunnel – coupled atoms in 1D

$$\epsilon_0 C_{\ell} + t \left(C_{\ell+1} + C_{\ell-1} \right) = E C_{\ell}$$



Tight binding model

Wavefunction of electron in a linear chain of atoms

$$\Psi(x) = \sum_{\ell} C_{\ell} \underbrace{\phi(x - \ell a)}_{\text{localized atomic orbital}} = \sum_{\ell} \underbrace{e^{ik\ell a}}_{\text{plane wave modulation}} \phi(x - \ell a)$$

Tight-binding model for tunnel – coupled atoms in 1D

$$\epsilon_0 C_{\ell} + t (C_{\ell+1} + C_{\ell-1}) = E C_{\ell}$$

Energy dispersion

Relation between frequency and wavelength

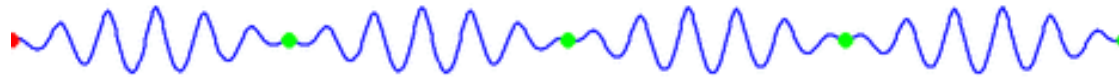
$$E(k) = \epsilon_0 - 2|t| \cos ka$$



Energy dispersion

Energy dispersion determines how a wavepacket propagates

$$v_g = \frac{d\omega}{dk} = \frac{1}{\hbar} \frac{dE(k)}{dk}$$



© wikipedia

● phase velocity

● group velocity

Energy dispersion for tunnel – coupled atoms in 1D

$$E(k) = \epsilon_0 - 2|t| \cos ka \longrightarrow \text{const} + |t|a^2 k^2$$

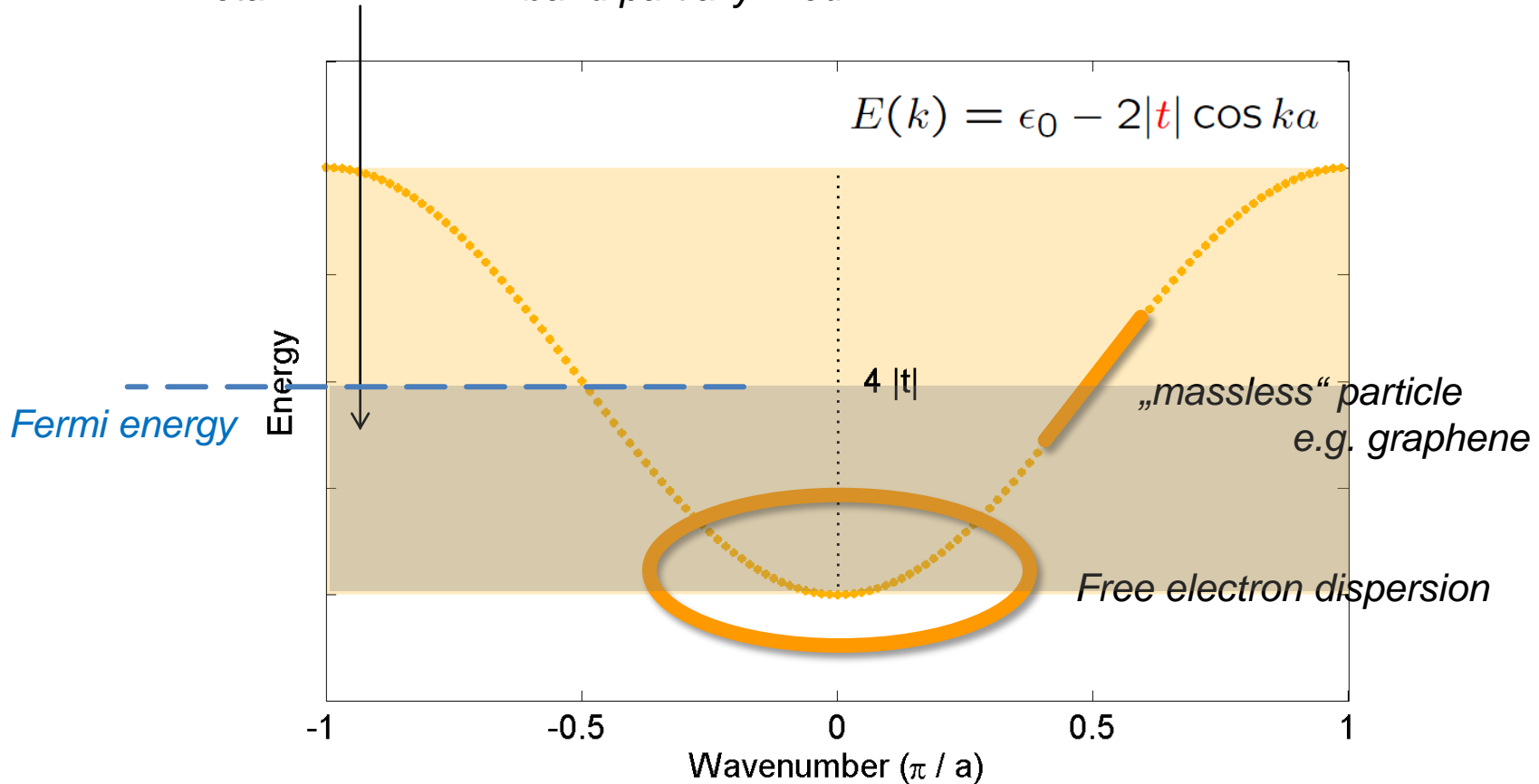
For long wavelengths (small k values) the dispersion is similar to that of a free electron, however, with an effective mass which is governed by the hopping t

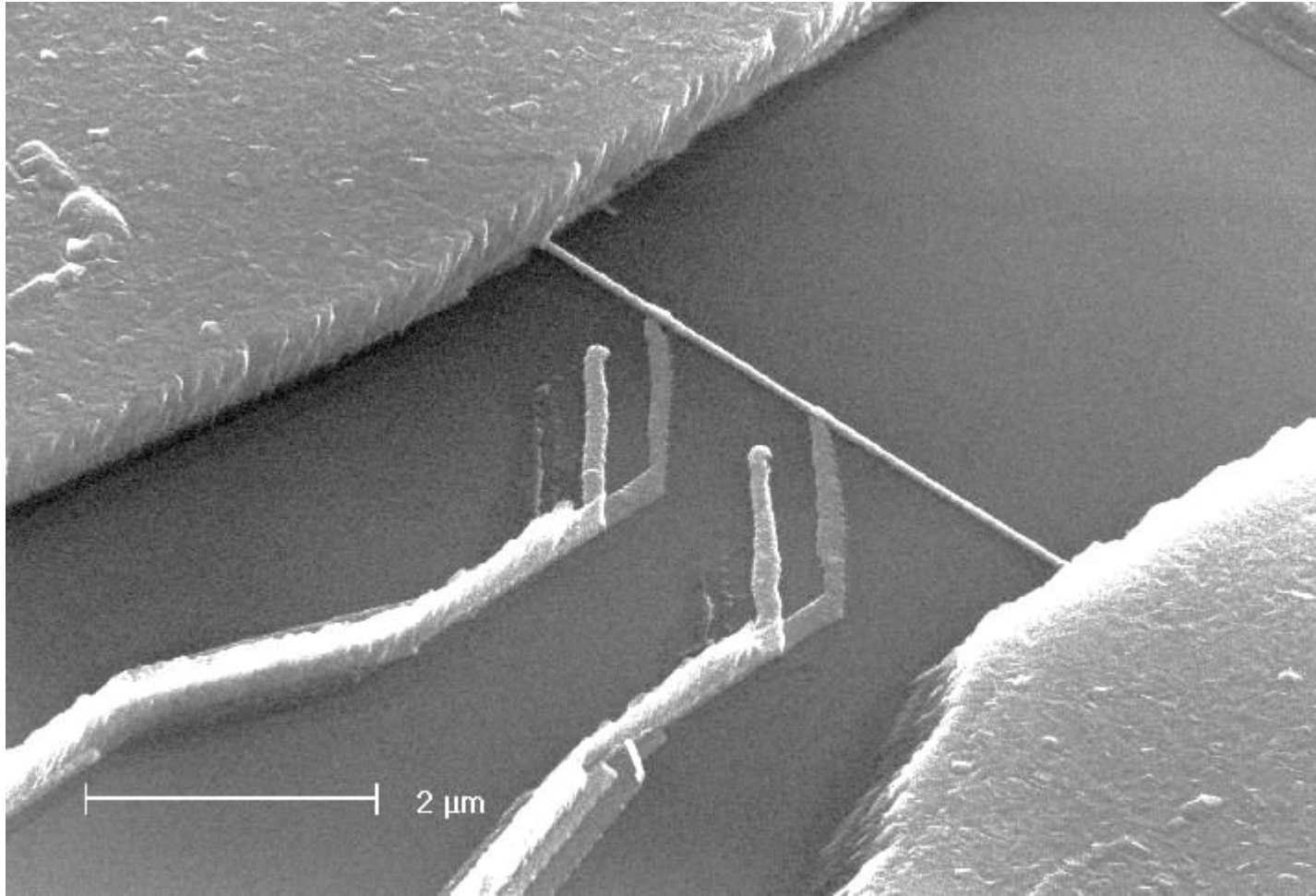
Energy band

Number of k states depends on number of atoms in the chain

Semiconductor ... no or only a few states of band filled

Metal ... band partially filled





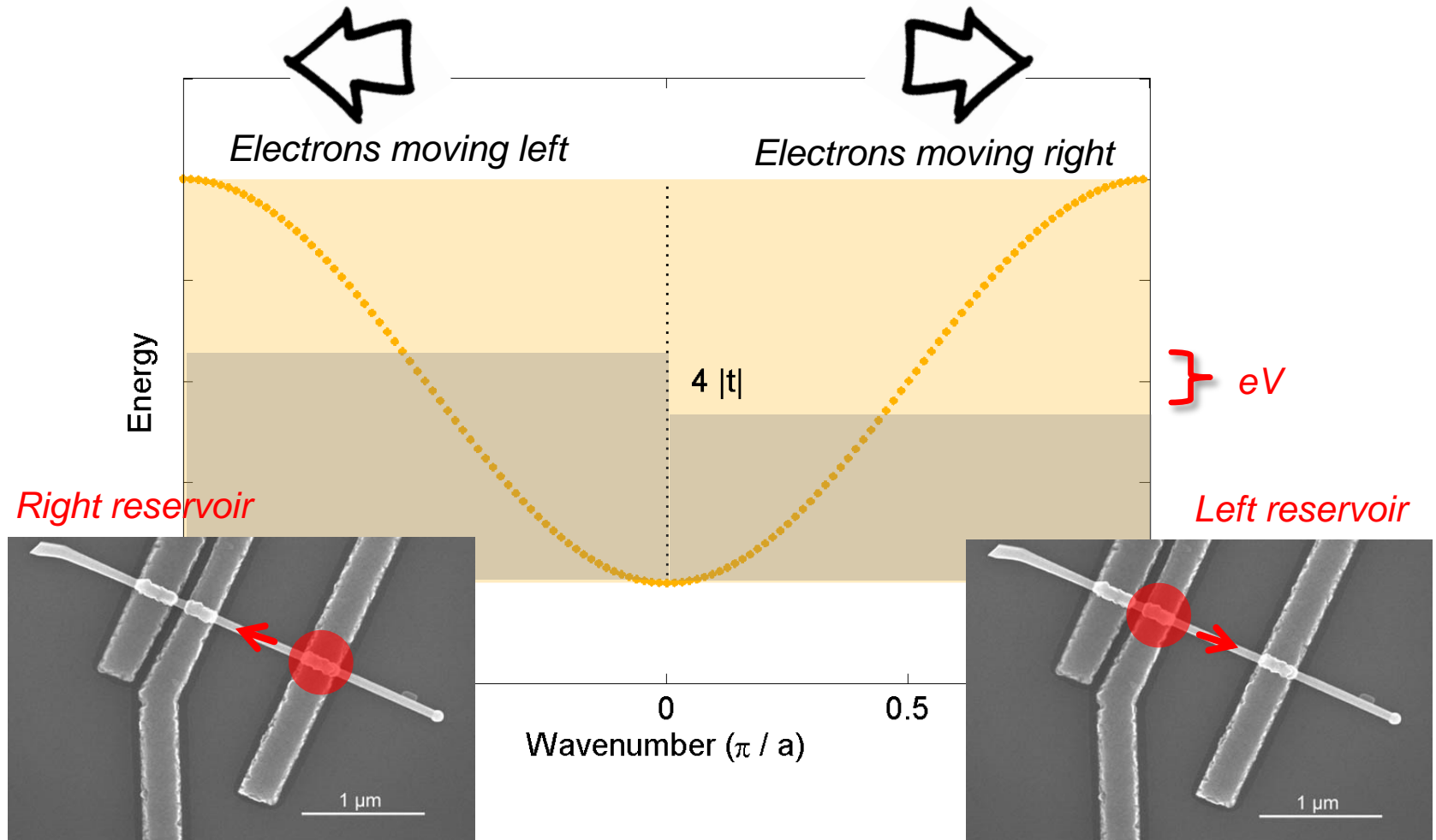
© quantronics, Sacley

Resistance of a ballistic nanowire

Transport through a nanowire

Nanowire connected to contacts

Short nanowire ... ballistic transport



Current through a nanowire

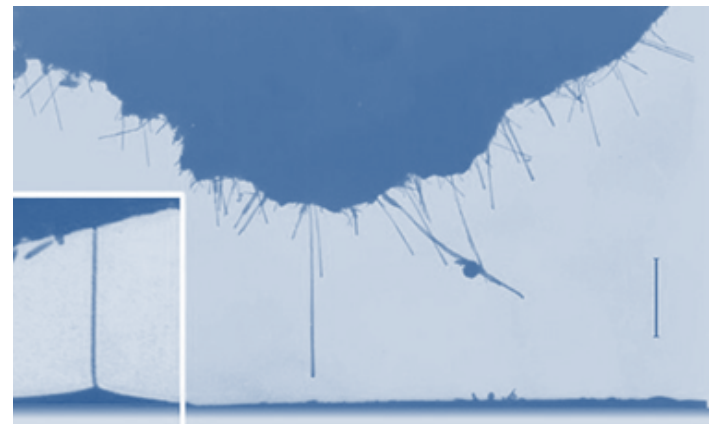
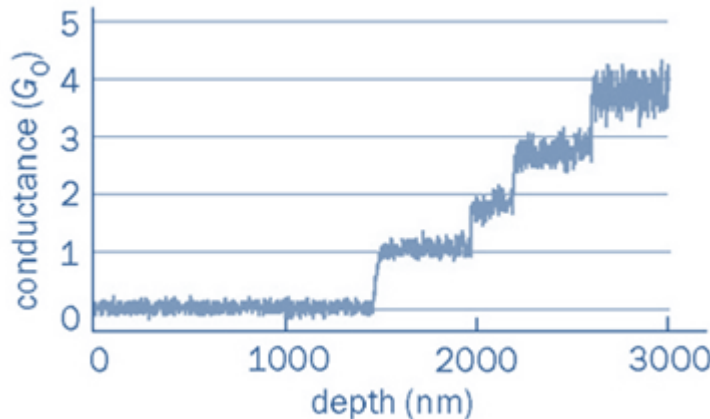
Current = spin x (electron density) x (sum of electron velocities)

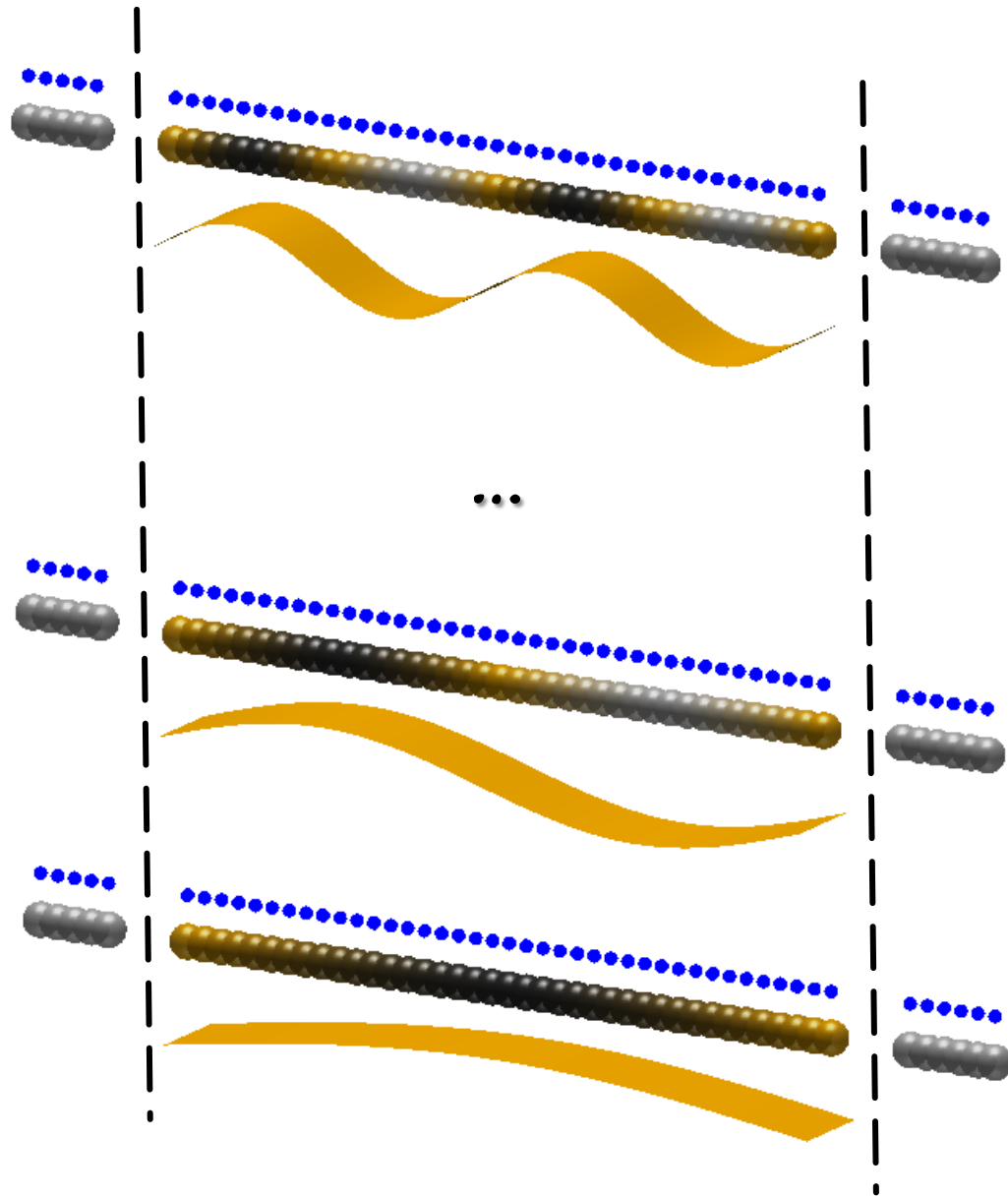
$$\begin{aligned} I &= \frac{2e}{L} \sum_k v_k \\ &= \frac{2e}{L} \frac{L}{2\pi} \int dk \frac{1}{\hbar} \frac{\partial E(k)}{\partial k} = \frac{2e}{h} \int_{E_F}^{E_F + eV} dE = \frac{2e}{h} eV \end{aligned}$$

Resistance R and conductance $G = 1/R$ depend only on natural constants

Conductance quantization

$$G_0 = \frac{2e^2}{h}, \quad h/e^2 \approx 25 \text{ k}\Omega$$





Quantum confinement: From 3D to 0D

Particle in a box

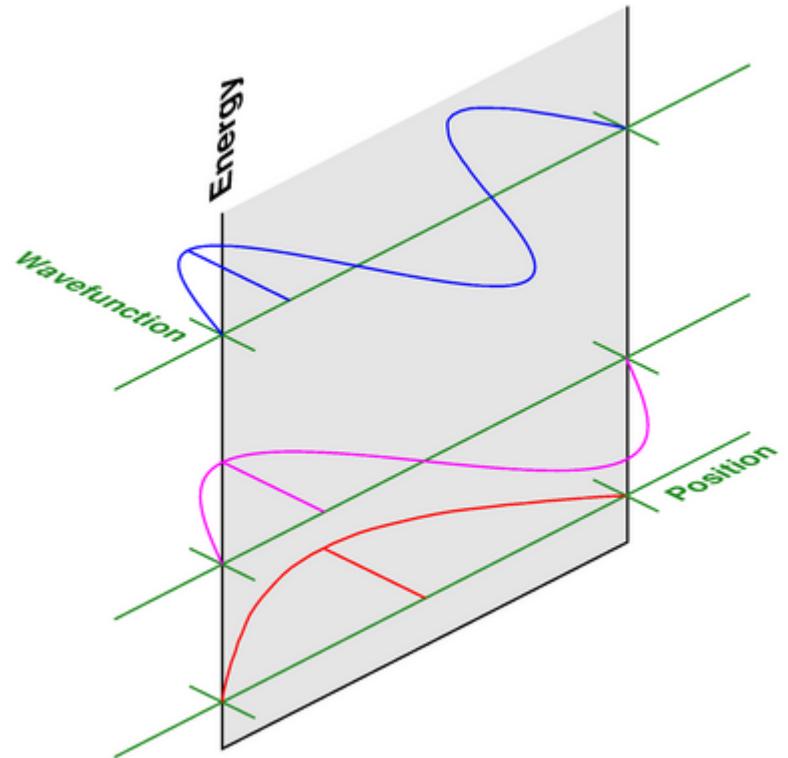
Motion of particle confined in a box

$$\psi(x) = \sin kx, \quad kL = n\pi$$

Energy quantization

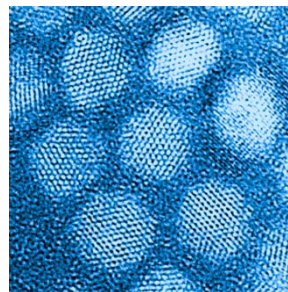
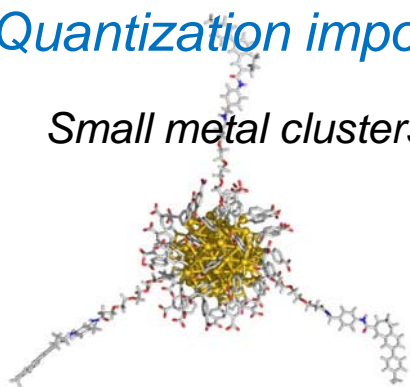
Confinement results in discrete energy levels

$$E_n = \frac{\hbar^2 k^2}{2m} = \frac{\hbar^2 \pi^2 n^2}{2mL^2}$$



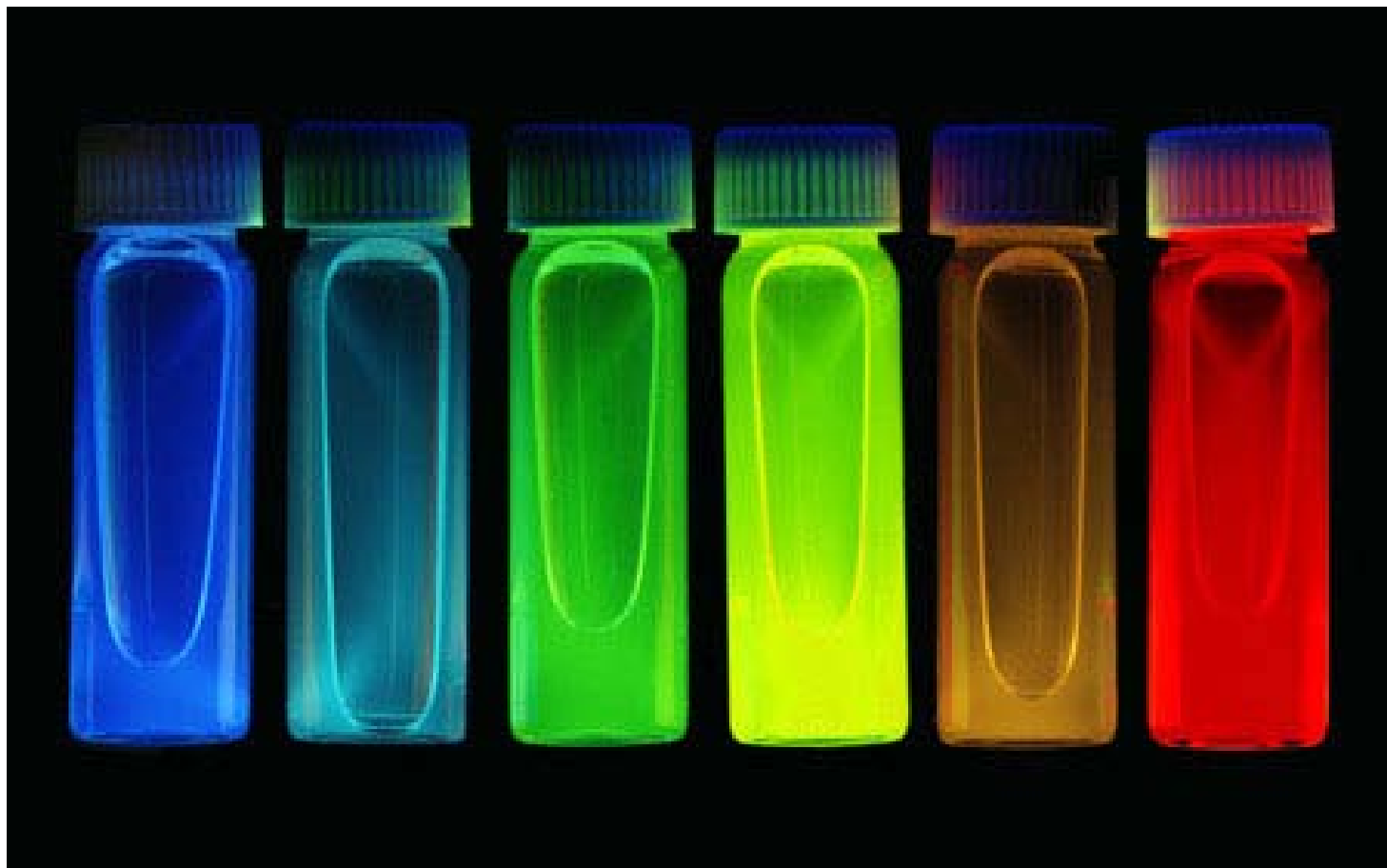
Quantization important if de Broglie wavelength comparable to NP size

Small metal clusters ($\lambda \sim \text{nm}$)



Semiconductor nanocrystals





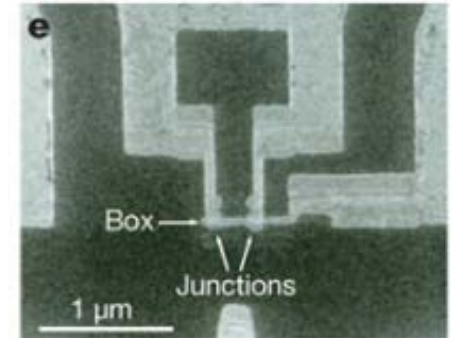
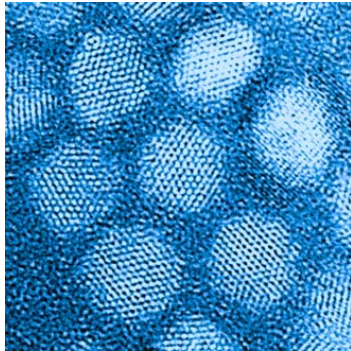
Small dots



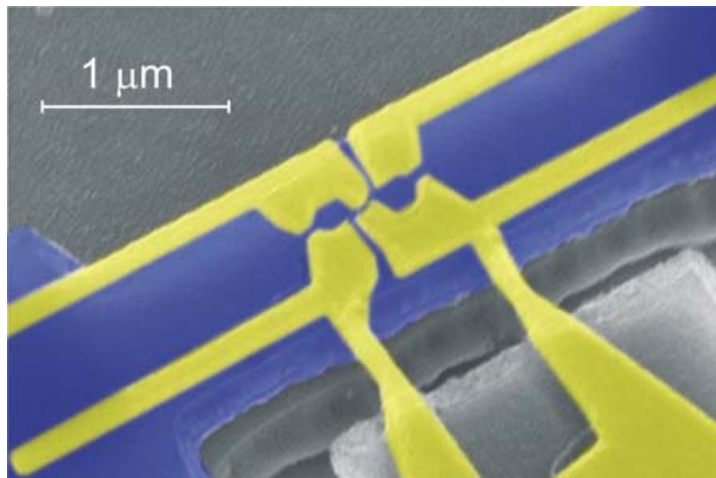
Large dots

How to confine electrons ?

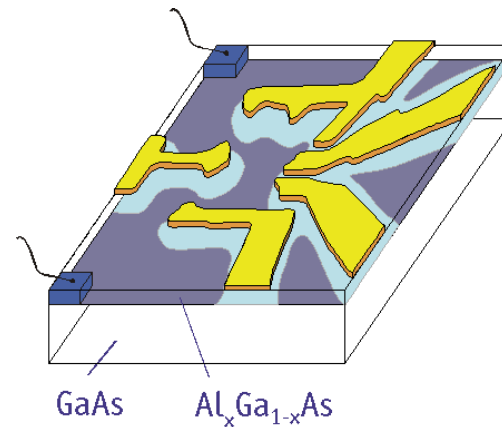
Structural confinement



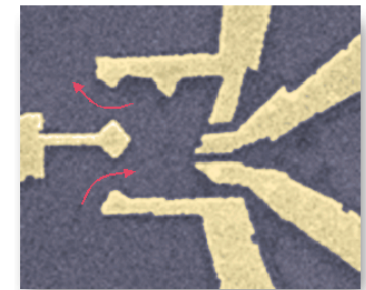
Gate control



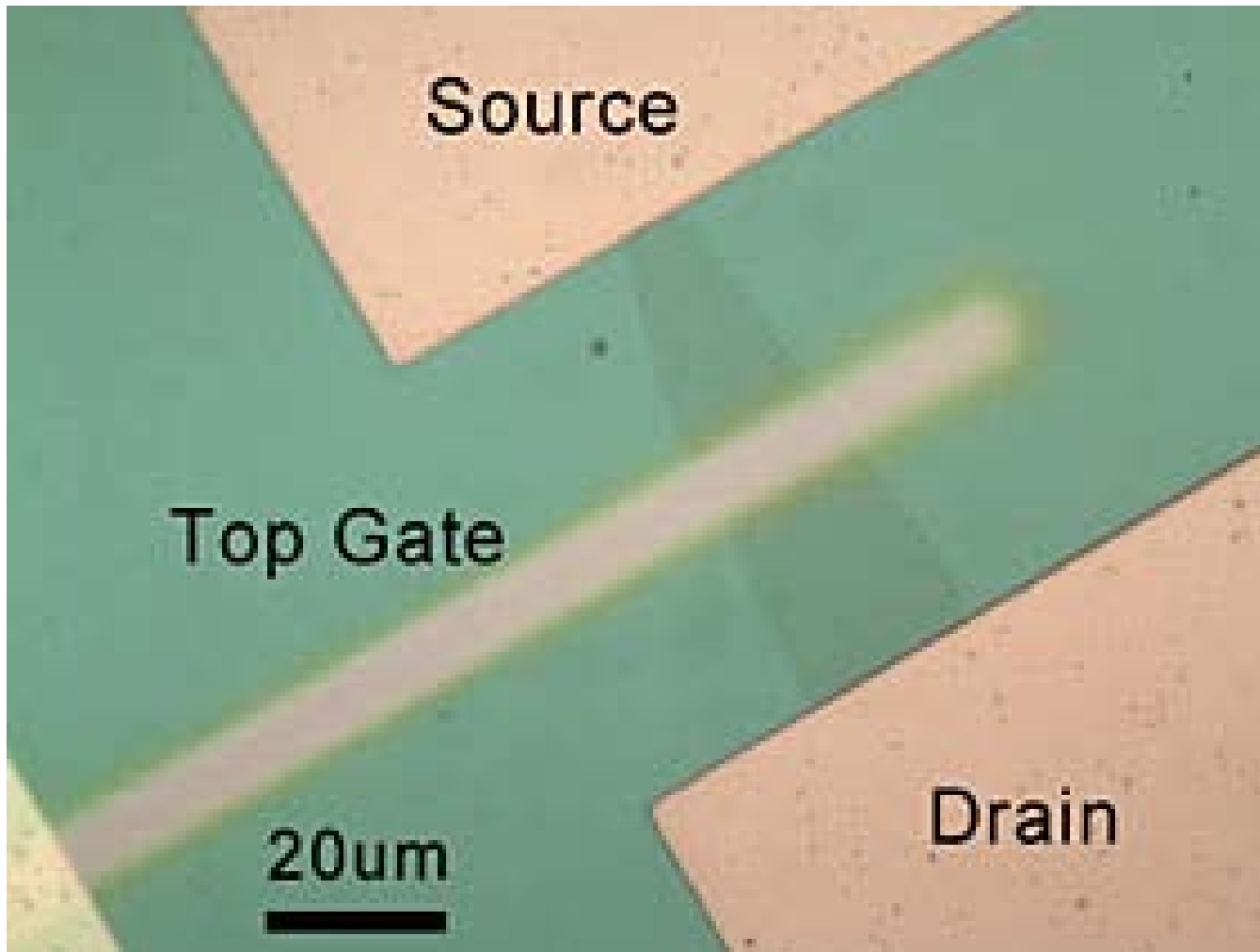
© www.nano.physik.uni-muenchen.de



© marcus lab, Harvard



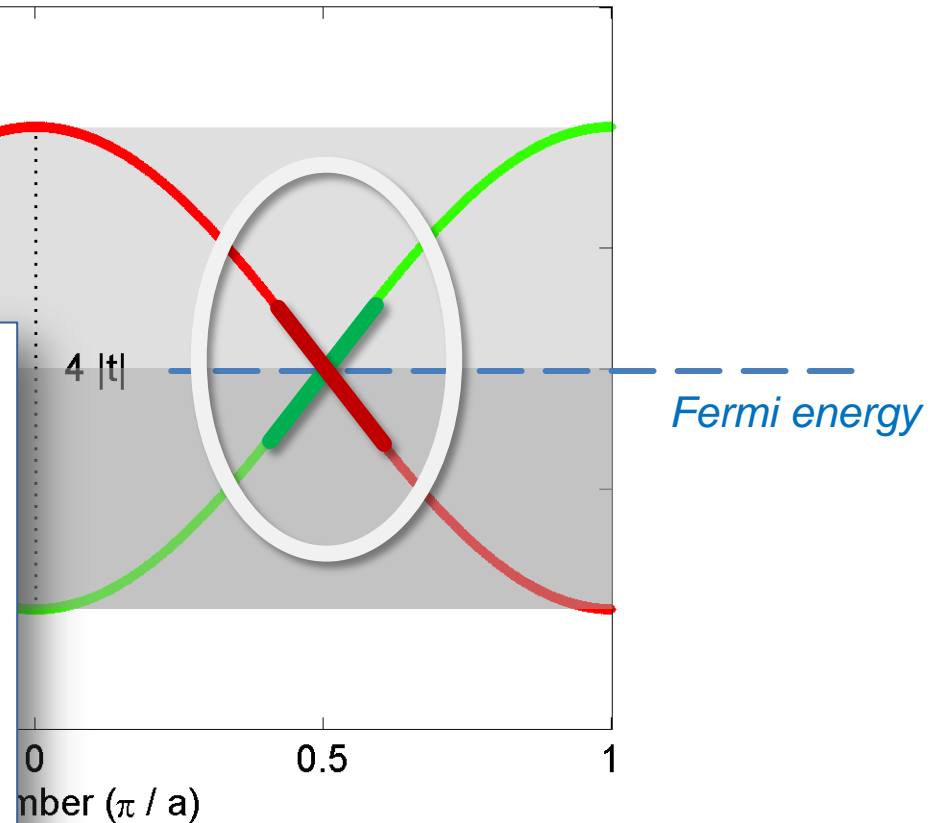
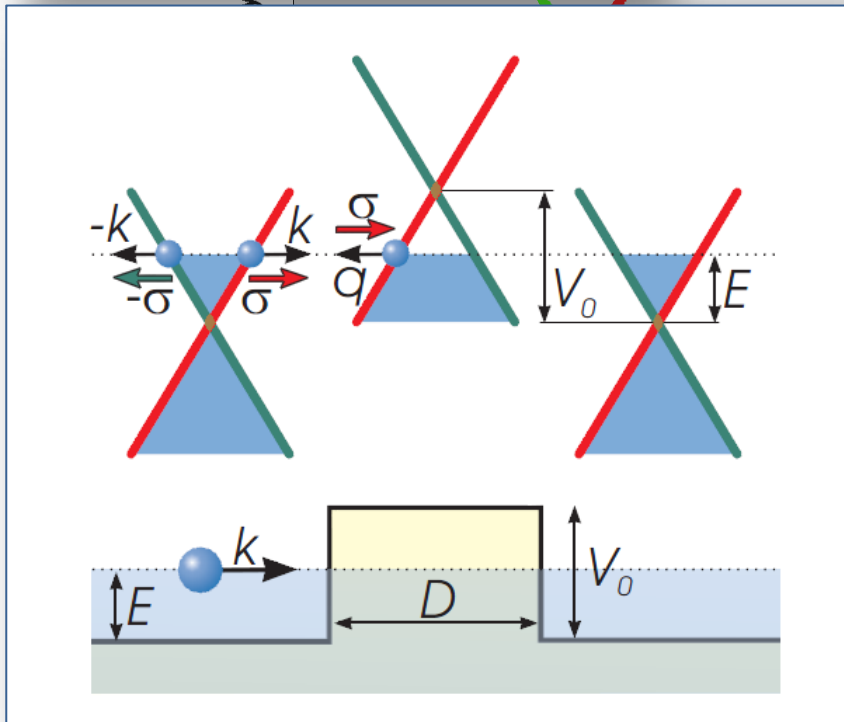
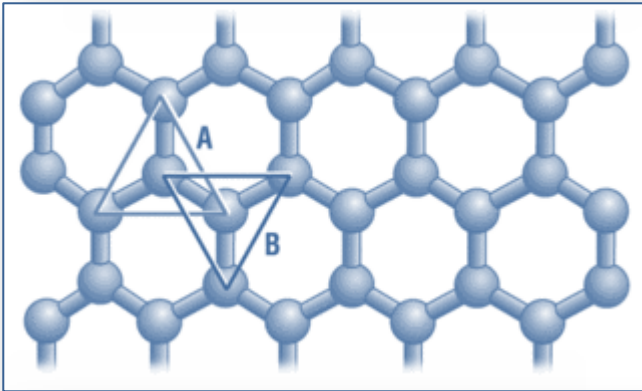
1 μm



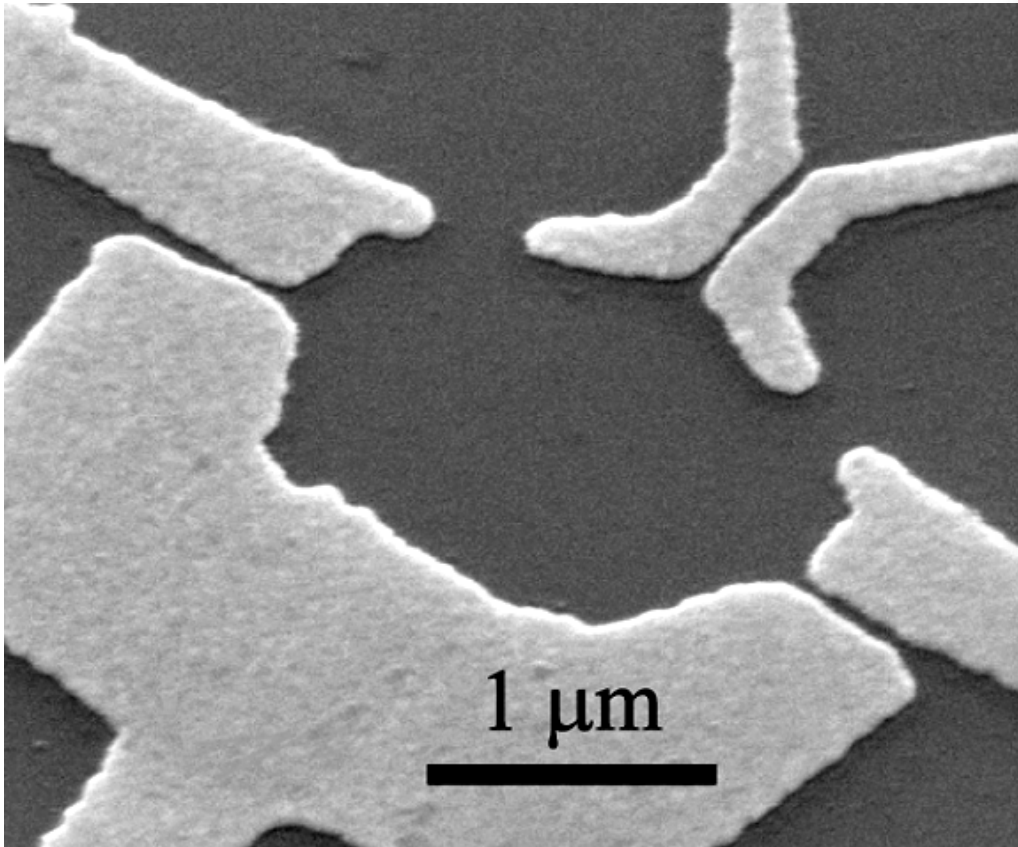
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Electron confinement in graphene

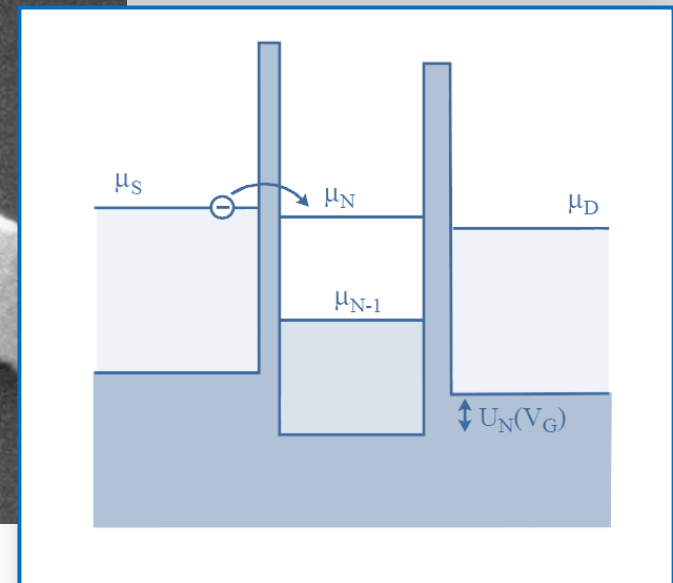
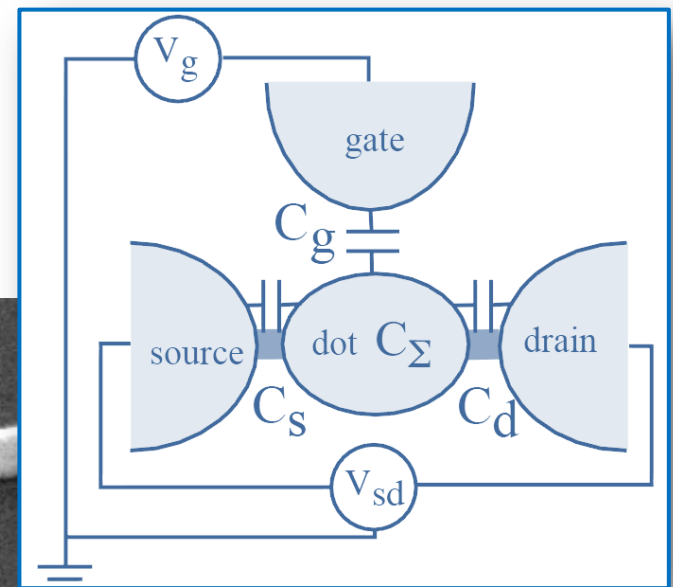
Electron confinement in graphene



No confinement in graphene with gates !!!
Confinement through nanoribbons,
double layer graphene



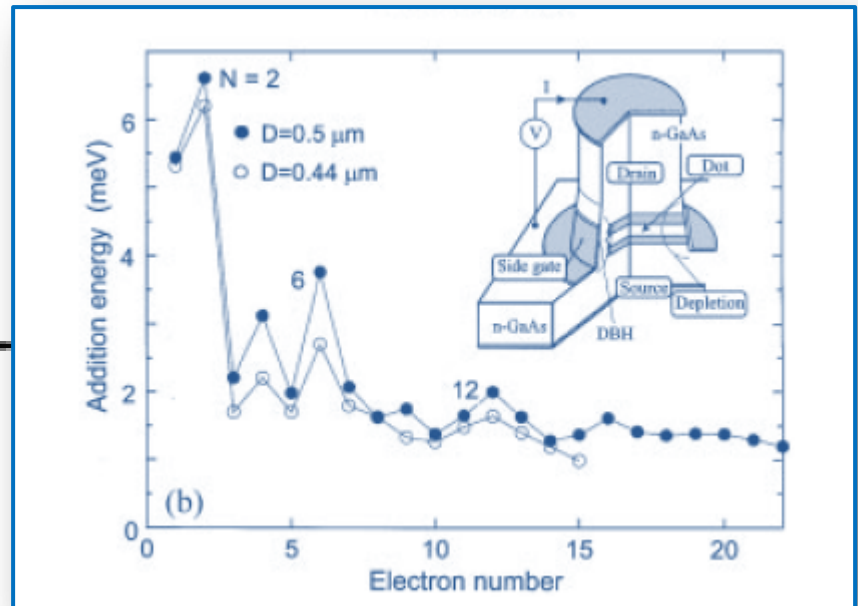
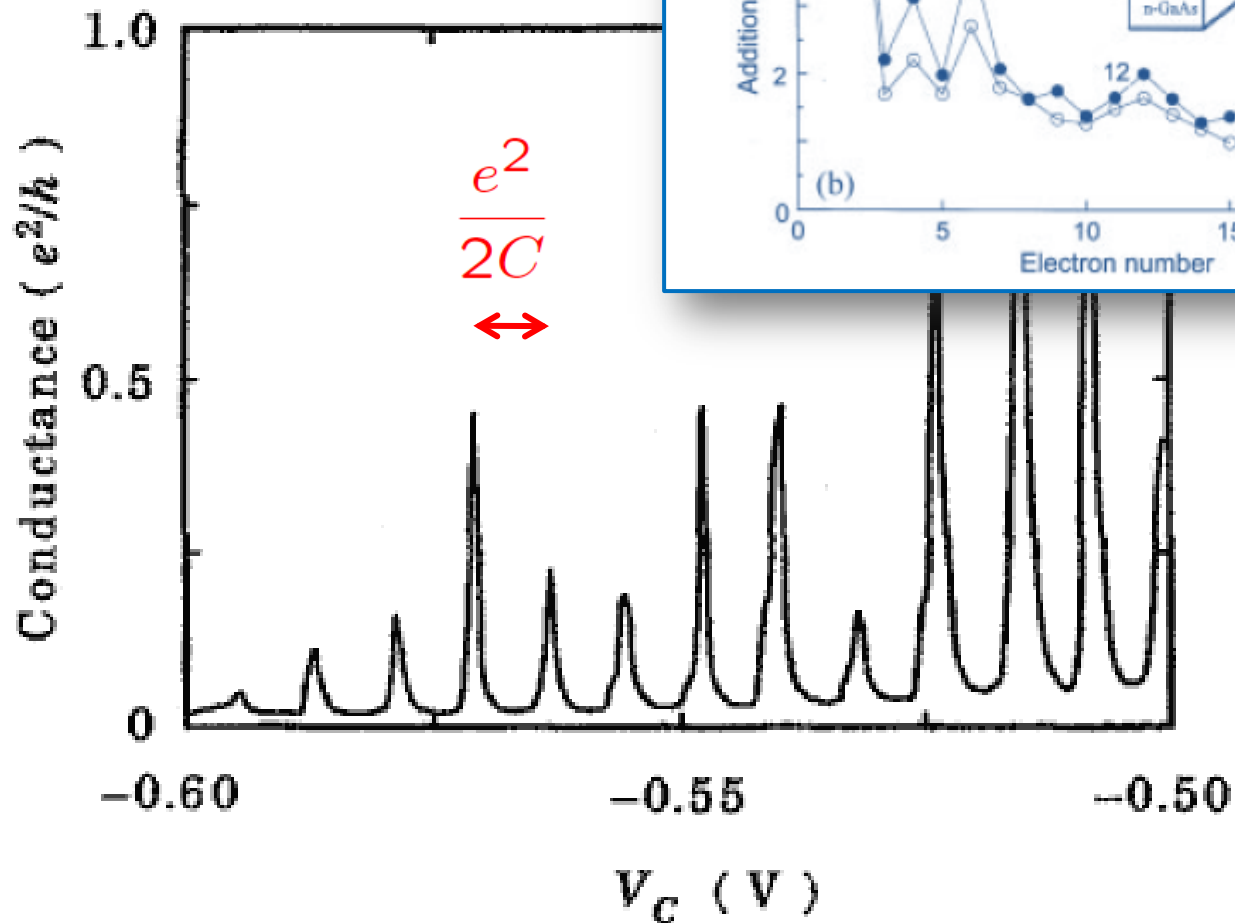
© www.unibas.ch



Electron tunneling through a QD

Coulomb blockade

Fine structure of Coulomb oscillations provides information about shell structure



Tarucha PRL 96

Coulomb blockade

Charge fluctuations to dot should be sufficiently small

$$(N - \langle N \rangle)^2 \ll 1$$

Temperature should be sufficiently low

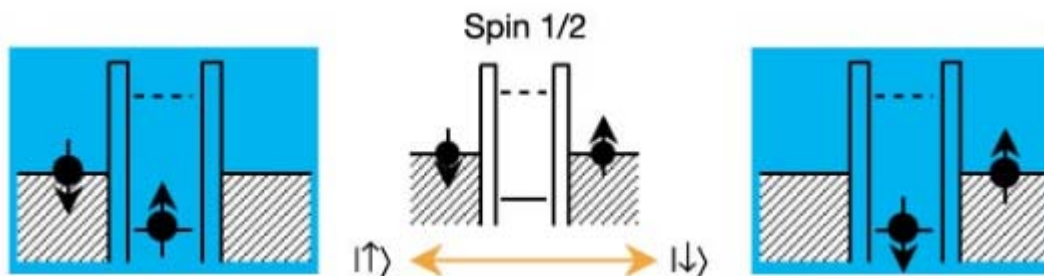
$$\frac{e^2}{2C} \gg k_B T$$

Tunnel coupling should be sufficiently small – high tunnel resistance

$$\Delta E \Delta t \approx \left(\frac{e^2}{2C} \right) \times (R_T C) > \frac{\hbar}{2}$$

$$R_T > \frac{\hbar}{e^2} \sim 25 \text{ k}\Omega$$

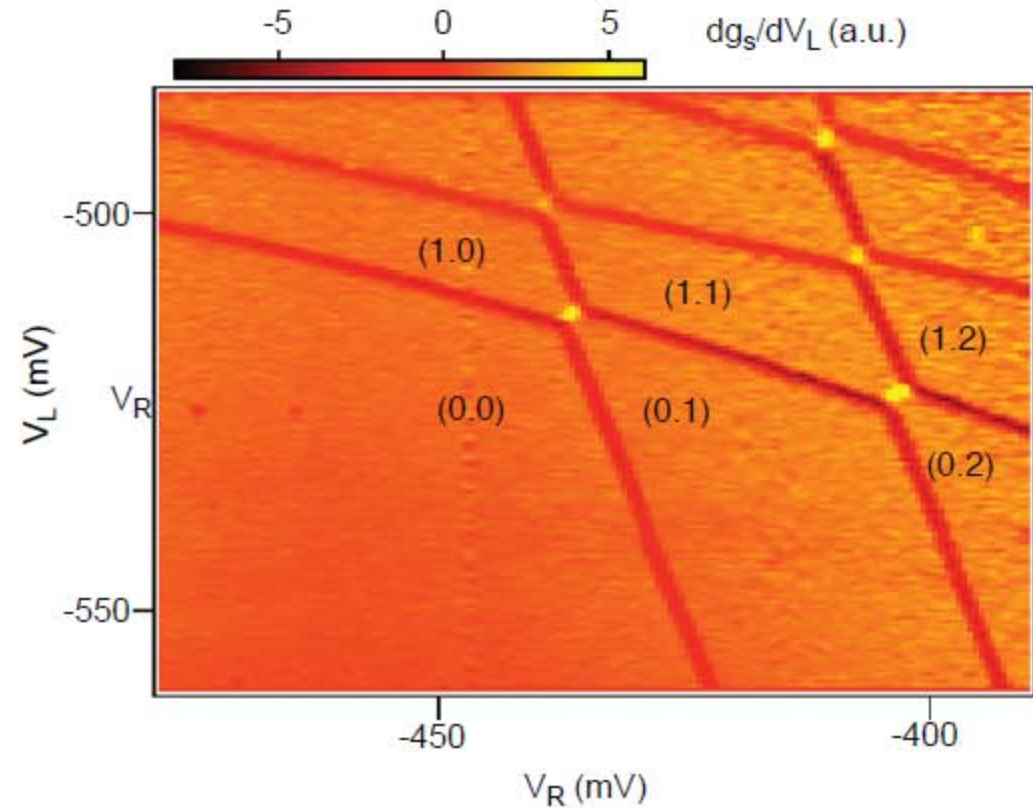
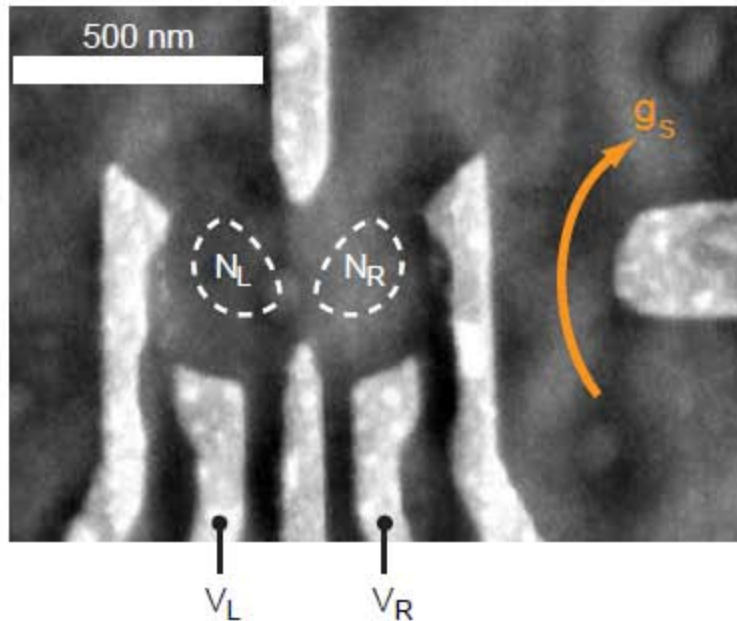
Other effects become important at low temperatures (e.g. Kondo)



Coulomb blockade diamond

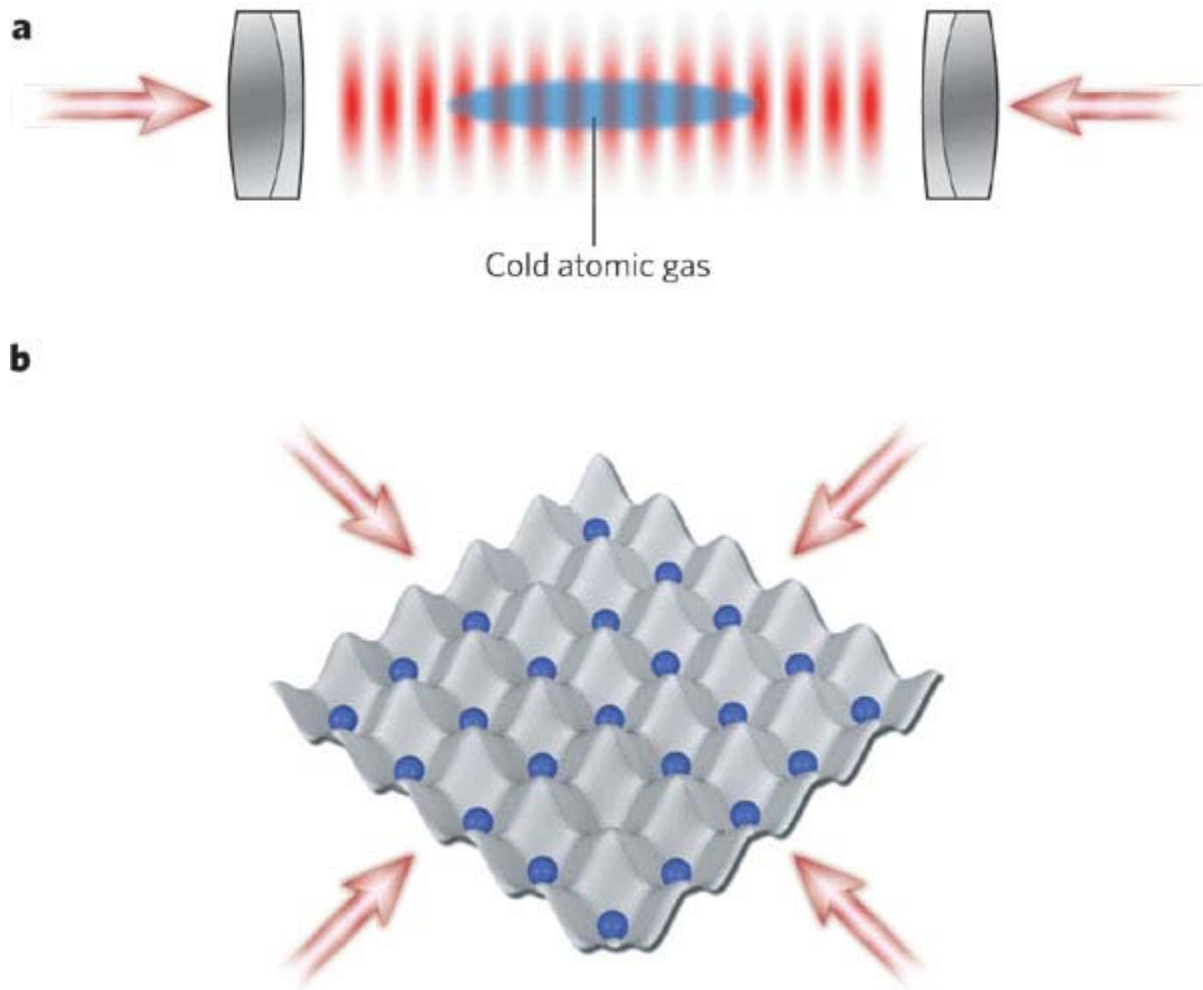
Variation of different voltages allows control and spectroscopy of states

Marcus lab, Harvard



Double quantum dot states: competition between tunneling and Coulomb repulsion U

$t \gg U$... electrons delocalized over structure
 $U \gg t$... electrons localized in separate wells

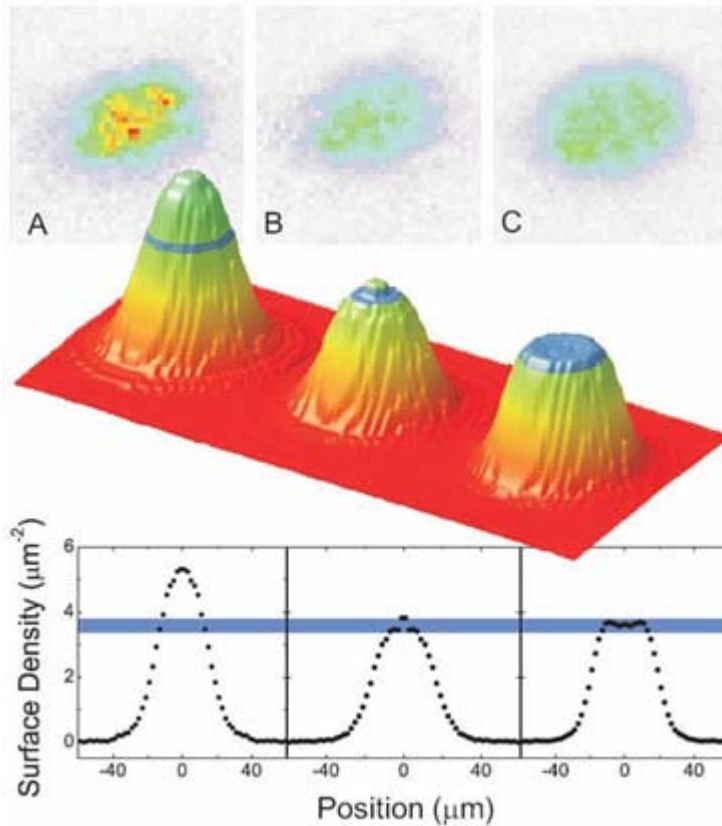


*Atomic lattice:
control of tunneling and repulsive interaction*

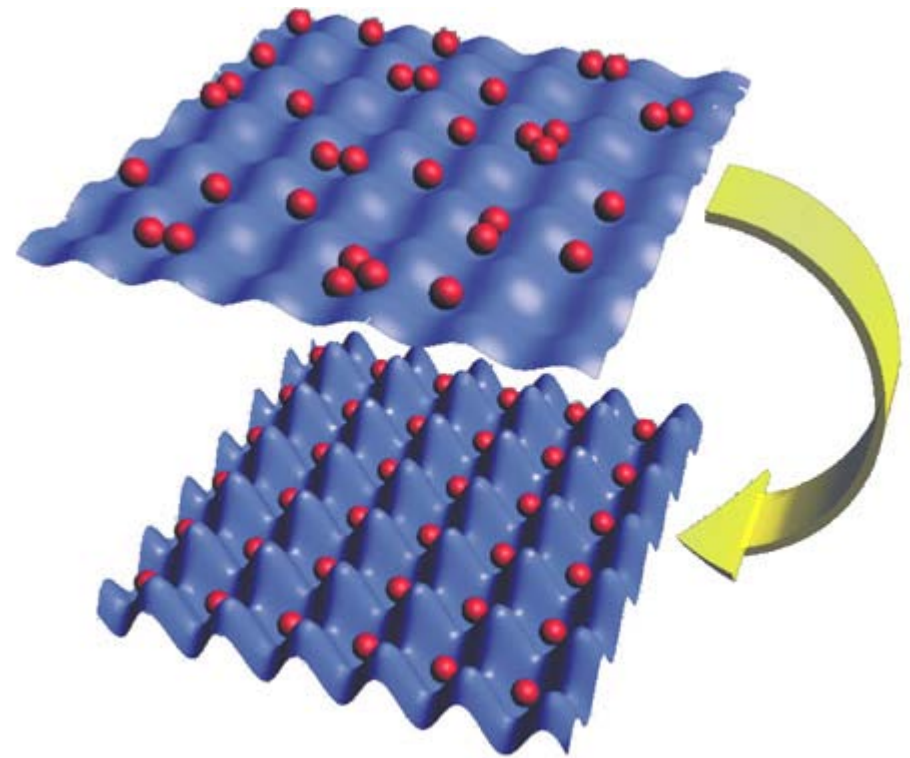
Delocalization vs. localization

Variation of t and U : transition between superfluid and Mott insulator phase

Density at one lattice site

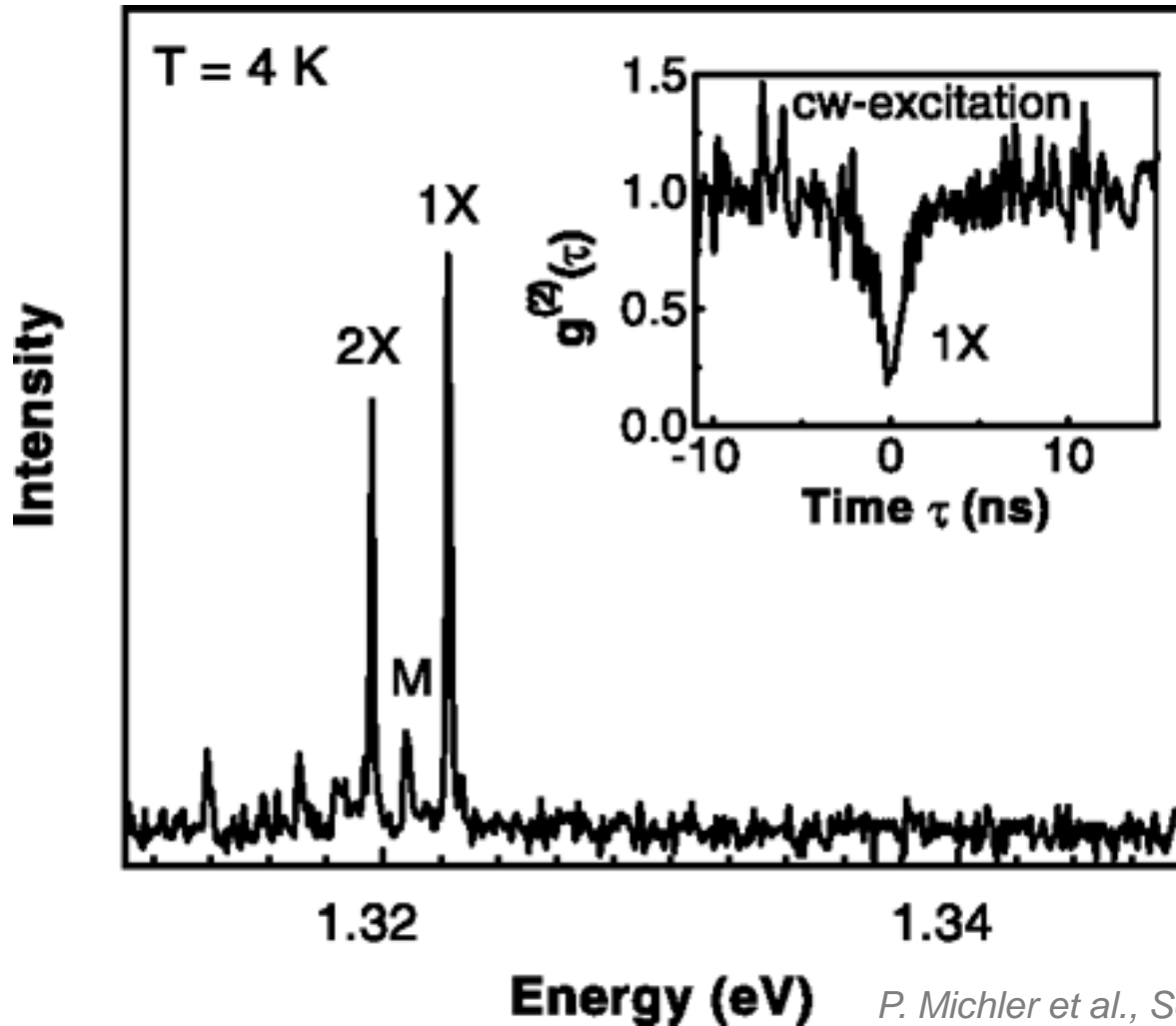


Transition from $t \gg U$ to $U \gg t$

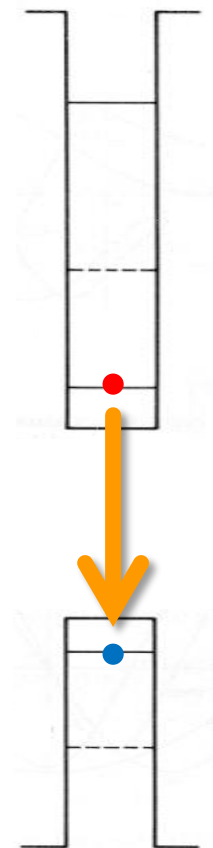


Nathan Gemelke et al., *Nature* **460**, 995 (2009).

Excitons



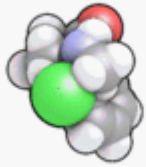
Electrons



Holes

P. Michler et al., Science 290, 2282 (2000).

Exciton = Electron-hole pair + Coulomb attraction



Molecular orbitals

How quantum is the nanoworld ?



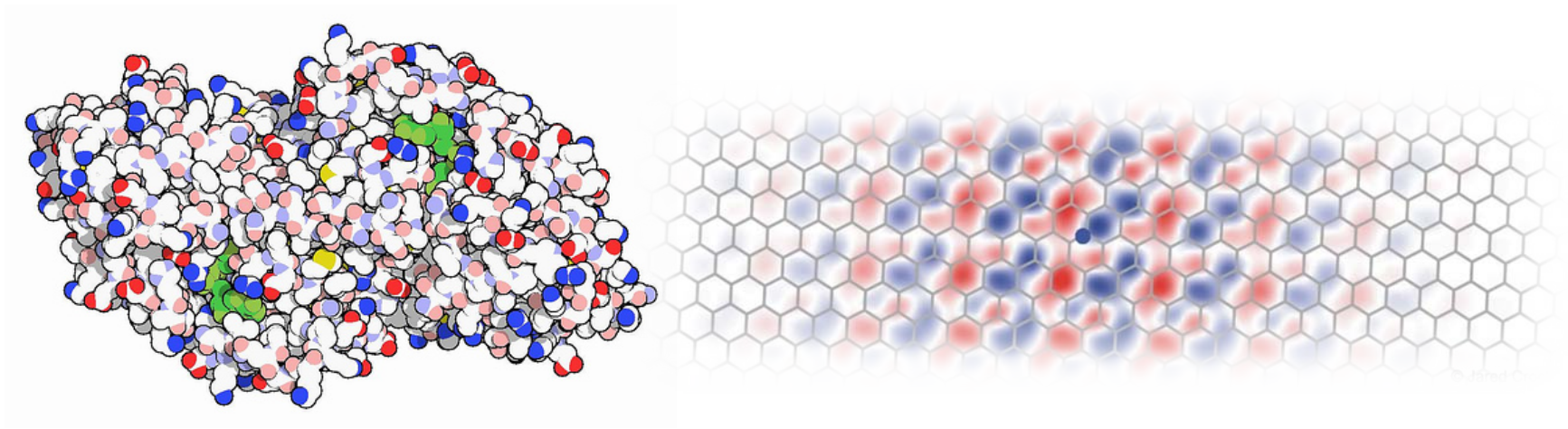
Superposition

Eigenstates

System in contact with its environment

$$H = H_S + H_{\text{env}} + H_{\text{int}}$$

Eigenenergies and eigenstates E_i, ϕ_i



Wavefunctions can be complicated – this does not matter ...

Superposition of eigenstates

Tunnel – coupled quantum dots

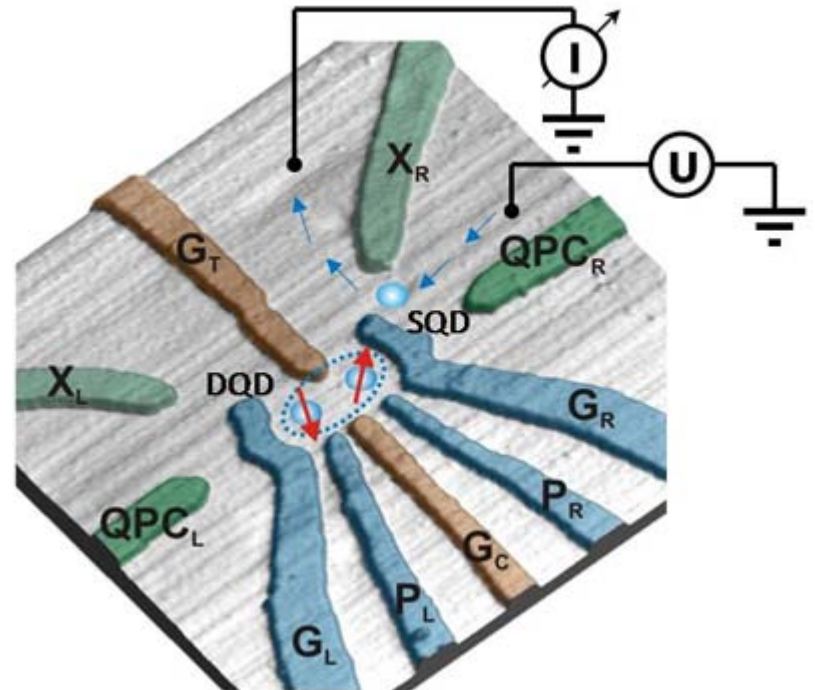
Hamiltonian of QDs

$$H_S = \begin{pmatrix} \epsilon_0 & t \\ t & \epsilon_0 \end{pmatrix}$$

Eigenstates

$$E_{\pm} = \epsilon_0 \pm |t|$$

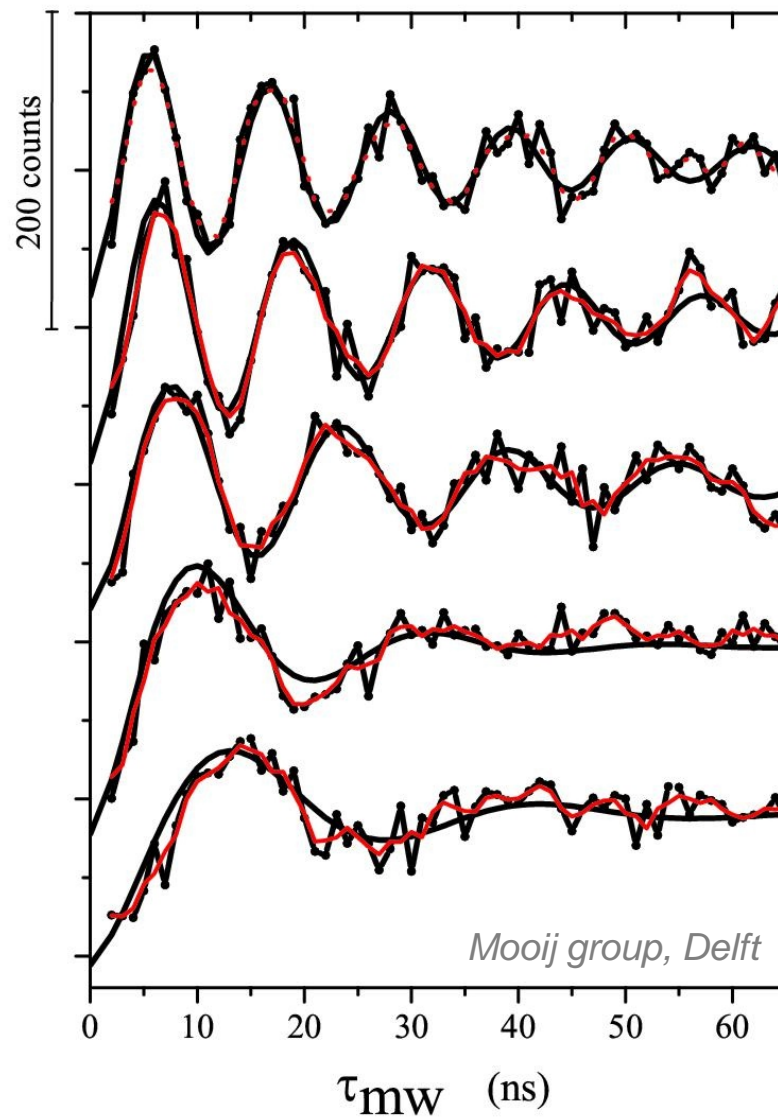
$$\phi_{\pm} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ \pm 1 \end{pmatrix}$$



Time evolution of superposition state

System tunnels between left and right well

$$\Psi(\tau) = \frac{1}{2} \left[\begin{pmatrix} 1 \\ 1 \end{pmatrix} e^{it\tau} + \begin{pmatrix} 1 \\ -1 \end{pmatrix} e^{-it\tau} \right] = \begin{pmatrix} \cos t\tau \\ i \sin t\tau \end{pmatrix}$$



Population oscillations are damped

Decoherence

von – Neumann measurement principle

Eigenstates of measurement apparatus

$$A \phi_i = \lambda_i \phi_i$$

Wavefunction collapse

$$\Psi = \sum_i C_i \phi_i \longrightarrow (\lambda_k \text{ with probability } |C_k|^2) \longrightarrow \Psi = \phi_k$$

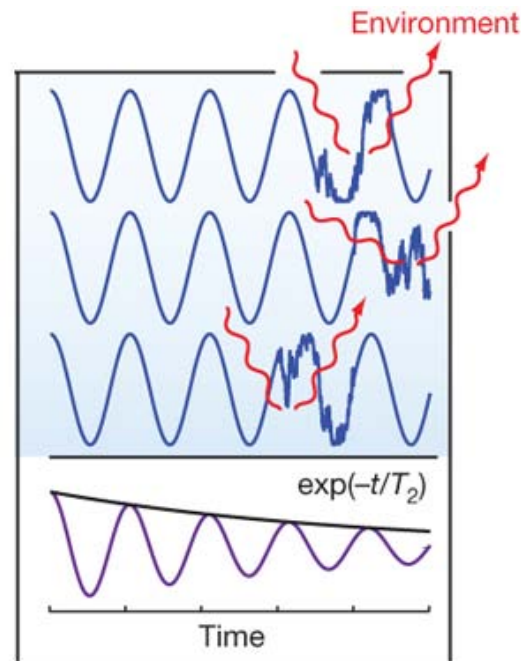
Environment

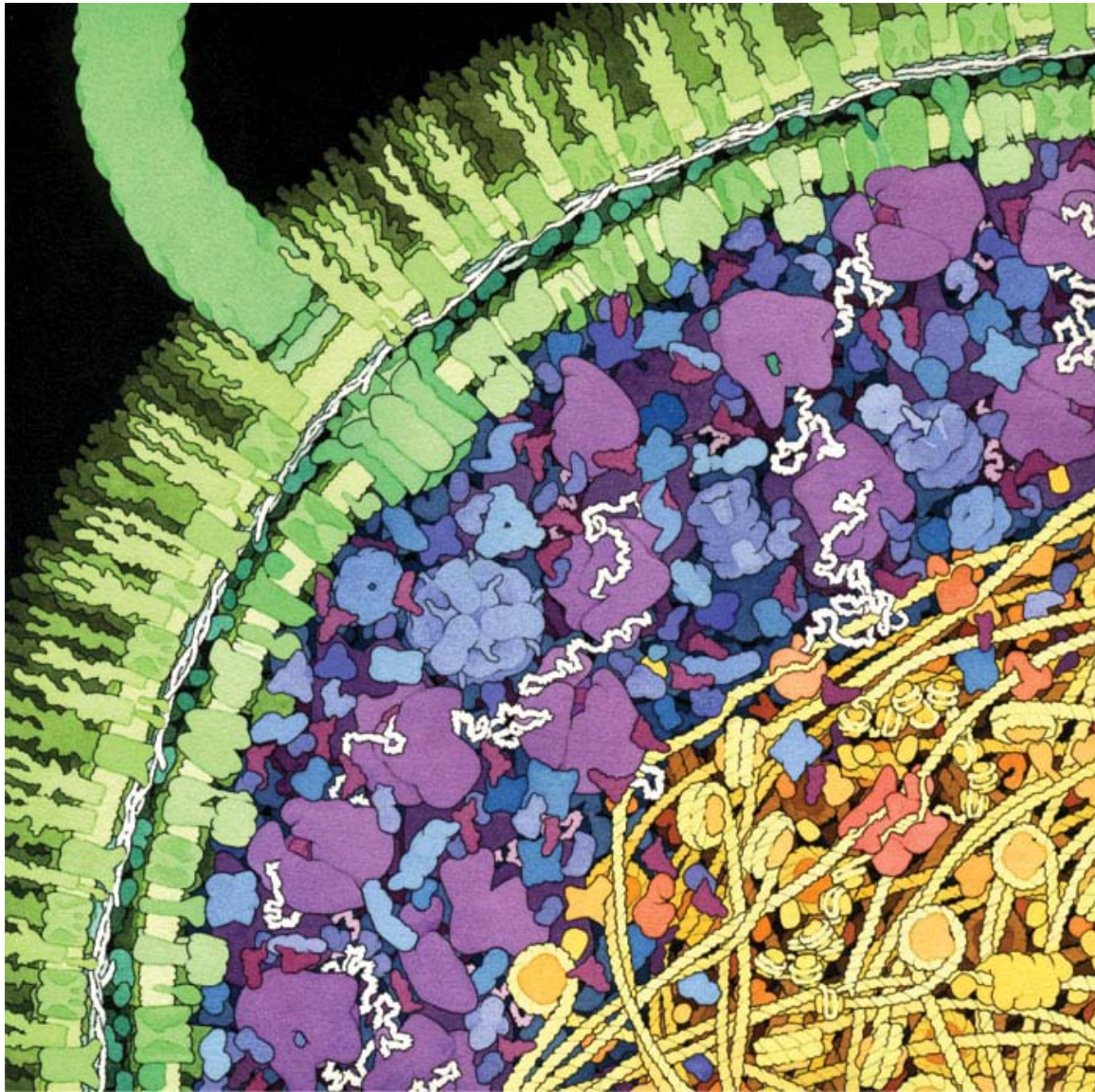
Also coupling to phonons, light, molecules etc. leads to decoherence

Good qubits are well protected from the environment

*Photon, electron spin, nuclear spin,
NV centers in (nano)diamond,
flux or phase qubits in superconductors, ...*

*T. D. Ladd et al., Nature **464**, 45 (2010).*





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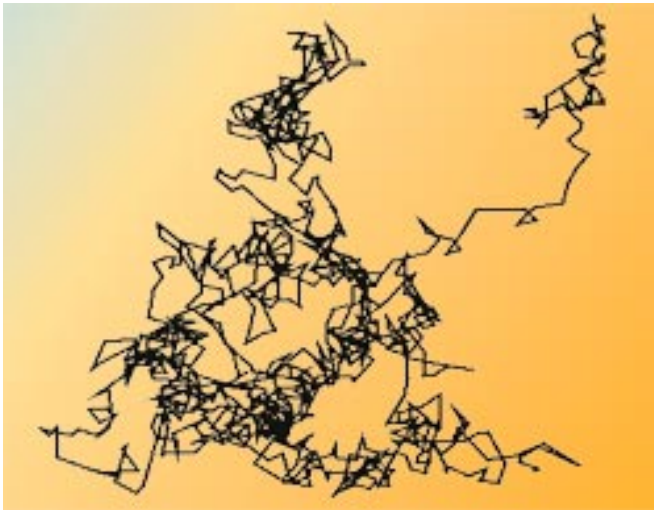
Bio machines are not very quantum ...

Life needs temperature

Brownian motion

Molecules, proteins in cells propagate through Brownian motion

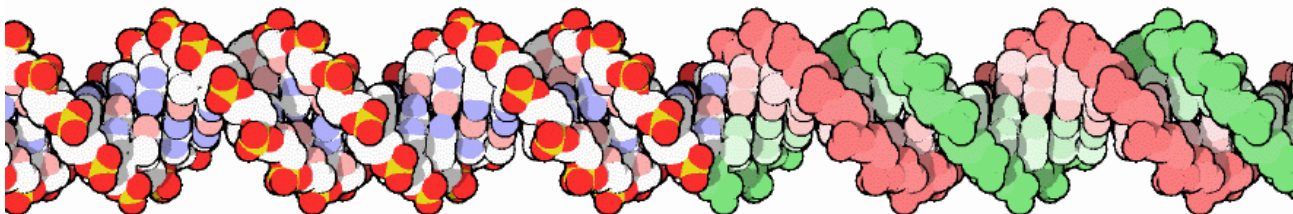
If the cell is small enough, two molecules will find each other on a timescale of seconds



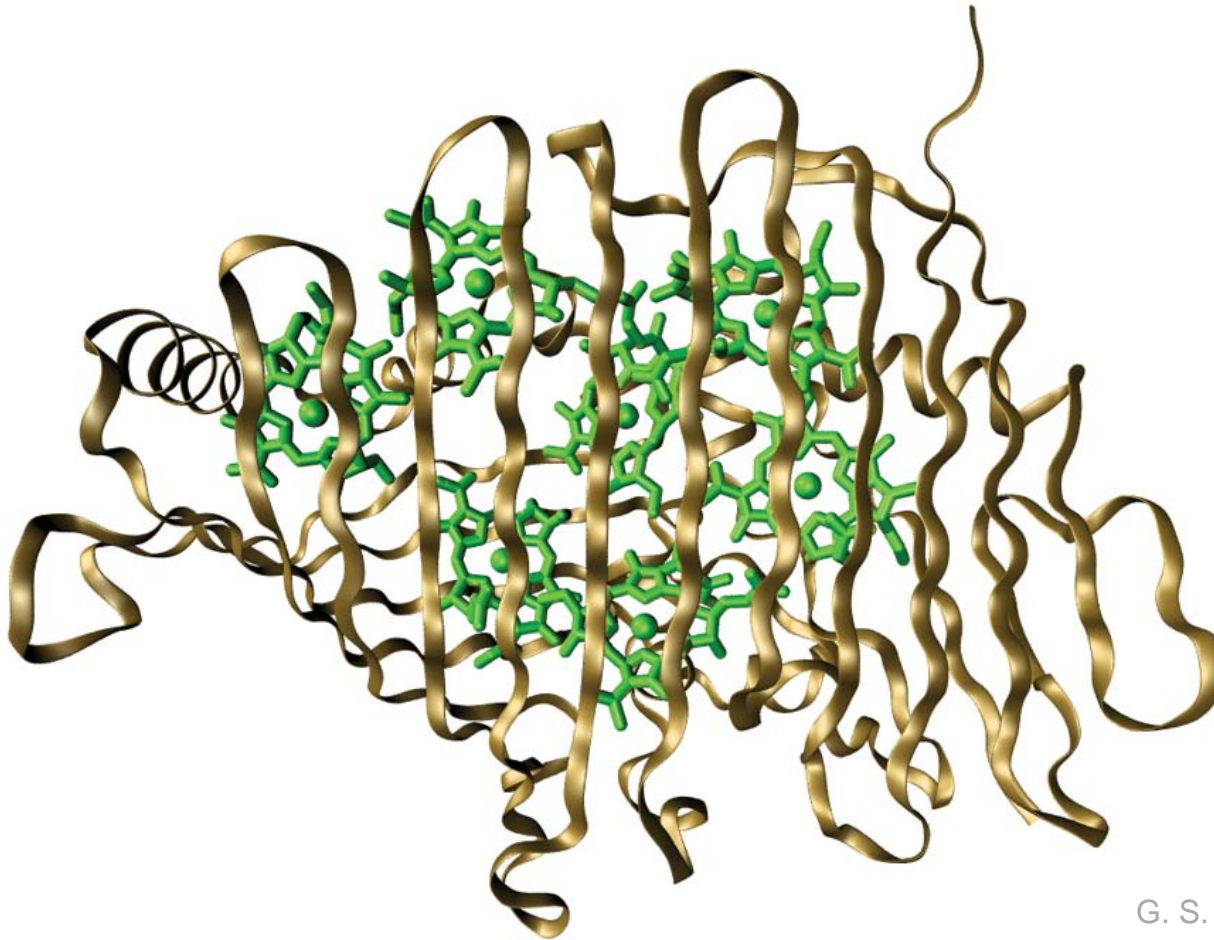
Thermal activation

Many processes in a cell require temperature,

e.g., DNA is usually close to the melting point



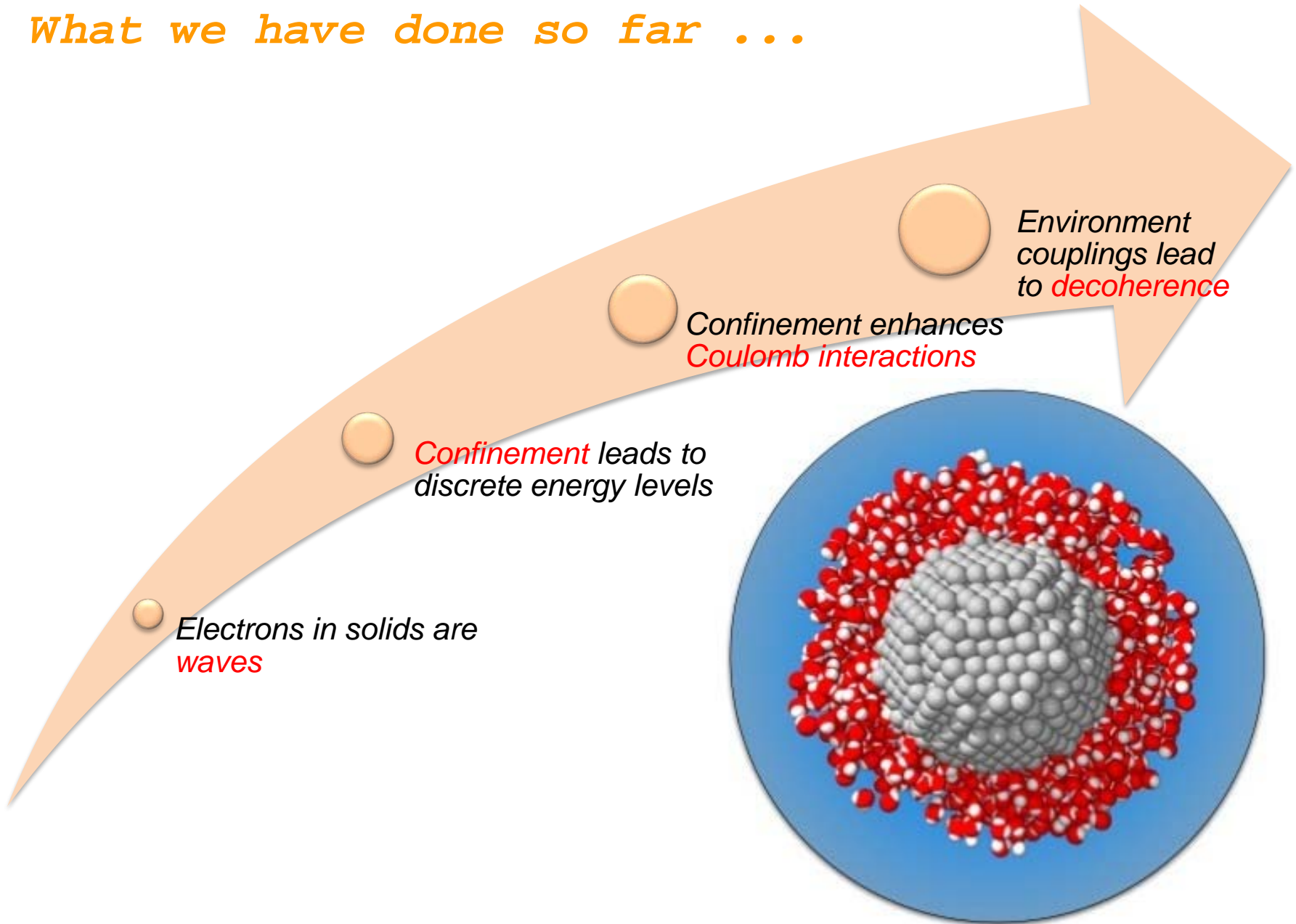
Quantum coherence in photosynthesis



G. S. Engel et al., Nature 446, 782 (2007).

The Fenna–Matthews–Olson complex helps green sulphur bacteria to perform photosynthesis. A quantum algorithm known as 'quantum walk' might be behind the remarkably efficient energy transfer between the light-collecting antennae and the reaction centre, where, ultimately, the photon energy is transformed into chemical energy.

What we have done so far ...



Nanoscience: Fundamentals and basic properties
Nanoscience: Fabrication and characterization methods
From atoms to the nanoscale
Nanostructures for photonics

Ulrich Hohenester
Harald Plank
Matti Manninen
Lorenzo Pavesi

Quantization in two-dimensional metallic systems
Carbon-based nanosystems

Milorad Milun
László Forró

Dispersion of nanoparticles
Supramolecular approach to nano-structured systems
Life at the nanoscale

Nikola Kallay
Mladen Zinic
Simon Scheuring

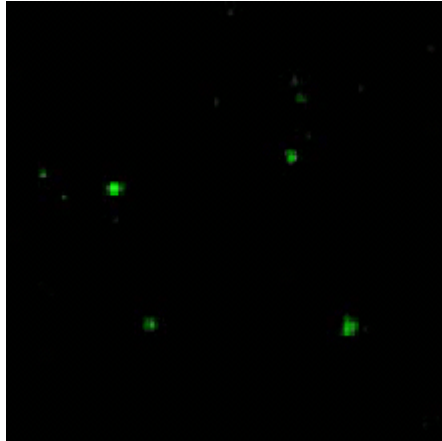
Biological physics and soft materials
Pharmaceutical nanotechnology: Drug delivery & targeting

Ilpo Vattulainen
Andreas Zimmer

What is missing ...

Single nanosystems

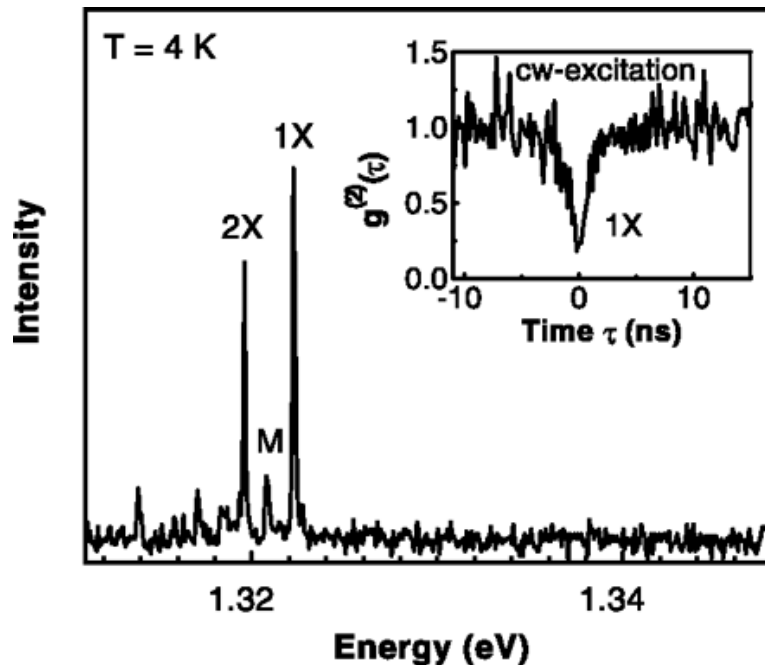
How do we know that we are measuring single systems ?



Colloidal dots exhibit „blinking“ where the dot turns between bright and dark periods on a second timescale.

This is due to charging and decharging of traps.

www.uni-ulm.de



Photon statistics tells us whether we are investigating a single system or not:

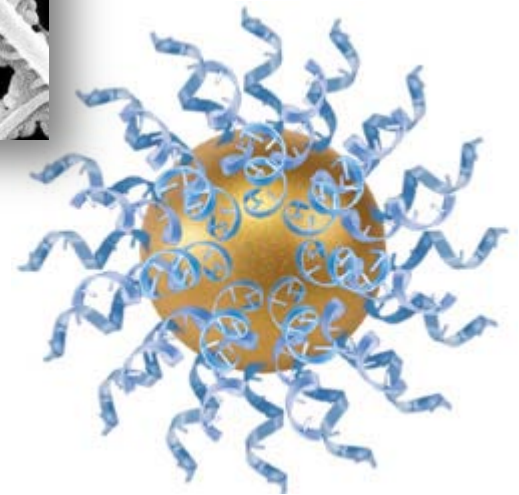
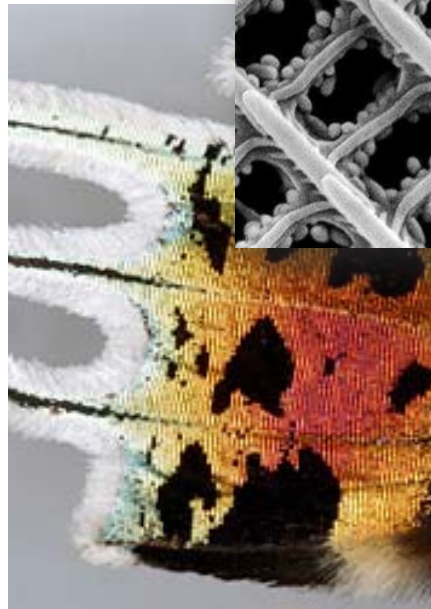
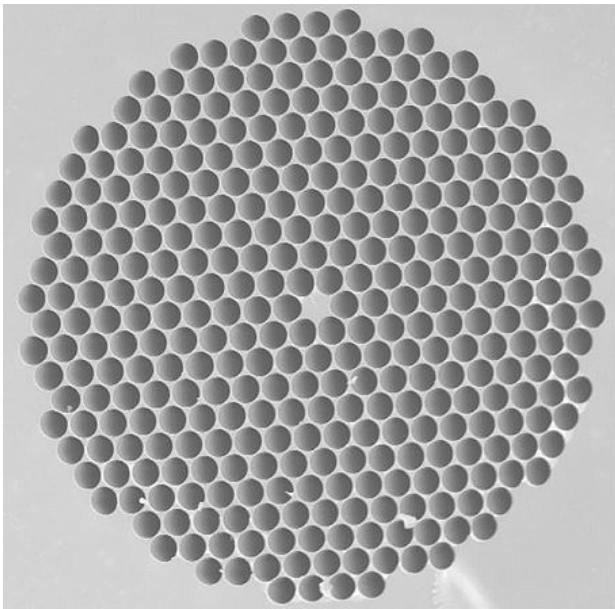
Once a photon is detected it takes a while to „reload“ the quantum emitter.

As result, two photons never arrive at the same time (photon antibunching).

P. Michler et al., Science **290**, 2282 (2000).

Optics at the nanoscale

Optics ($\lambda \sim \mu\text{m}$) and nanostructures have a mismatch of dimensions

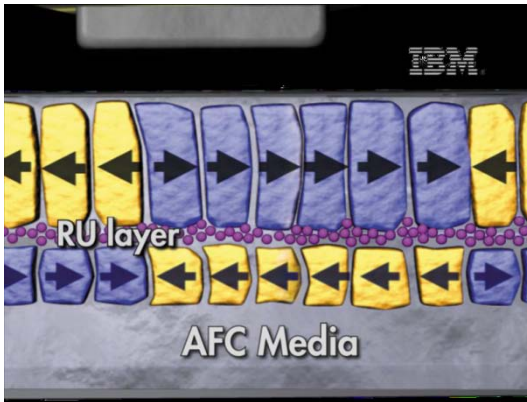


Photonic crystals allow the confinement of light on a micrometer length scale and to strongly enhance light matter interactions.

In plasmonics light is bound to metallic nanoparticles by exciting surface plasmons.

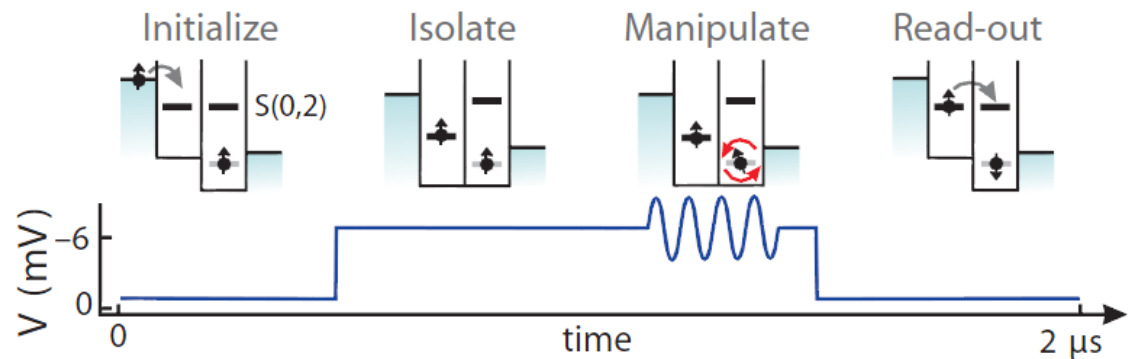
Nanomagnetism & spintronics

Spin couples only weakly to the solid state environment and thus provides an ideal means for storing (quantum) information.



(Nano)magnets are used in hard disks to store information.

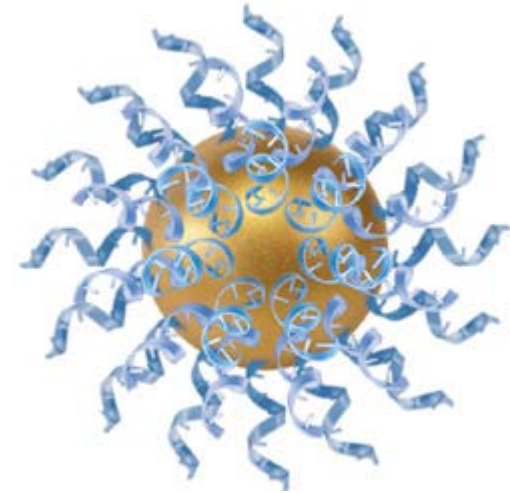
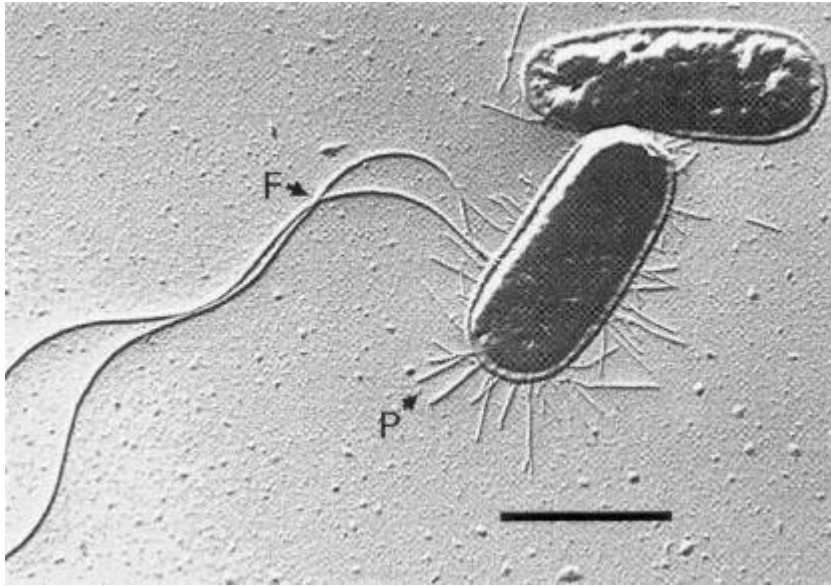
For small magnets there is a competition between bulk and surface effects, and it becomes difficult to suppress thermal flipping.



Spin qubits are possible candidates for building blocks of quantum computers.

Much progress has been made recently in order to manipulate the spins and to suppress decoherence (due to phonons and nuclear spins).

Forces, fluids, heat at the nanoscale



Forces at the nanoscale are dominated by intermolecular and van der Waal forces. Gravity plays (usually) no role.

Nanoscale fluid mechanics has to account for the motion of single molecules. Due to the strong forces, an *Escherichia coli* bacterium in water comes to a complete halt on a length scale of sub-nanometers.

Heat transfer at the nanoscale is a challenge for miniaturized nanodevices and presently constitutes one of the major roadblocks of computer industry.